Measurement and CFD prediction of heat transfer in air-cooled disc-type electrical machines

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Abstract—Accurate thermal analysis of axial flux permanent magnet (AFPM) machines is crucial in predicting maximum power output. Stator convective heat transfer is one of the most important and least investigated heat transfer mechanisms and is the focus of this paper. Experimental measurements were undertaken using a thin-film electrical heating method, providing radially resolved steady state heat transfer data from an experimental rotor-stator system designed as a geometric mockup of a through-flow ventilated AFPM machine. The measurements are compared with computational fluid dynamics (CFD) simulations using both 2D axisymmetric and 3D models. These were found to give a conservative estimate of heat transfer, with inaccuracies near the edge and in the transitional flow regime. Predicted stator heat transfer was found to be relatively insensitive to the choice of turbulence model used in the CFD simulations.

I. INTRODUCTION

Disc type electrical machines such as the axial flux permanent magnet (AFPM) machine offer high torque density and high efficiency in a compact package and are of great interest for applications such as electric and hybrid vehicles and portable generator sets [1]. Their electromagnetic design is well understood, but far less research has been undertaken on thermal aspects. This is despite the fact that torque density is usually limited by maximum temperature. Since the stator temperature that is achieved depends on the amount of specific internal heat generation and the convection heat transfer from the stator surface, an understanding of the latter is essential in machine design.

Significant research, e.g. [2], has been undertaken on the thermal modelling of radial flux (cylindrical) electrical machines. However, the air flow within a radial flux geometry is completely different to the air flow within a disc type machine, and the convective heat transfer correlations which are relevant to the former case cannot be applied to the latter. Recent work on the thermal aspects of disc type machines [3]–[5] has tended to focus on one-dimensional lumped parameter (LP) networks to represent both the solid domain and the fluid domain. These are fast to solve and widely used in electrical machine design. However, the LP method is only as good as the input correlations used for thermal contact resistances, convective heat transfer coefficients and air flow modelling and therefore CFD and finite element analysis (FEA) are being increasingly applied to investigate the thermal design of electrical machines in more detail, combined with experimental validation.

For readers unfamiliar with the thermofluids analysis of electrical machines, our recent review paper ‘Air-gap convection in rotating electrical machines’ [6] may be consulted for a general overview of the subject and introduction to the non-dimensional analysis of heat transfer data. This includes worked examples demonstrating the application of experimental heat transfer correlations in machine design.

AFPM machines are inherently more three dimensional in nature than radial flux machines and the air flow in the rotor-stator gap sees an expanding cross sectional area from inside to outside, unlike in a radial flux geometry. All authors comment that suitable stator convective heat transfer coefficients could not be found in the literature, and therefore they either apply rotor correlations (which are likely to lead to an over-optimistic assessment of heat transfer), or use CFD simulations to predict heat transfer coefficients. Few studies have applied CFD to AFPM machines. Airoldi et al. [7], [8] undertook CFD modelling of the fluid flow in an AFPM machine, finding good correspondence between CFD and experiment for mass flow rates and temperatures, although a limited experimental data set is presented.

We have recently reported direct experimental measurements of stator heat transfer in a rotor-stator system, relevant to AFPM machines, using a flat rotor and flat stator as an idealised geometry [9], [10]. Heat transfer in the form of non-dimensional Nusselt number was measured at stator radii 0.6 < r/R < 1., at three gap ratios relevant to disc type electrical machines. Transition from laminar to turbulent flow was observed to begin at rotational Reynolds numbers Reθ > 3ε5. It was also shown that the ingress of ambient air at the periphery of the stator has a significant effect on stator heat transfer.

In this paper, measurements are compared with CFD simulations using both 2D axisymmetric and 3D models. The heat
transfer results have been non-dimensionalised using various dimensionless groups. This means that they can be applied more universally, for example to machines with different diameters. The groups are as follows: rotational Reynolds number $Re_\theta$, Nusselt number $Nu$, gap ratio $G$ and non-dimensional air mass flow rate $C_w$. These are defined as follows:

\[
Re_\theta = \frac{\omega R^2}{\nu}
\]

\[
Nu = \frac{h R}{k}, \quad Nu = \frac{\bar{h} R}{k}
\]

\[
G = \frac{g}{R}
\]

\[
C_w = \frac{\dot{m}}{\mu R}
\]

where $R$ is the rotor outside radius, $\omega$ is the rotor speed, $\nu$ is the air kinematic viscosity at ambient temperature, $h$ is the convective heat transfer coefficient, $k$ is the air conductivity at ambient temperature, $g$ is the axial gap distance between rotor and stator surfaces, $\dot{m}$ is the air mass flow rate and $\mu$ is the dynamic viscosity. Also, radial position is non-dimensionalised to $r/R$.

An AFPM machine in the simplest configuration consists of a rotor disc adjacent to a stator disc. The air flow in the gap between such a rotating and a stationary disc can be divided into two regimes (see [6]): Batchelor flow, where there is a rotating core of fluid between separate laminar or turbulent boundary layers; and Stewartson flow, where the tangential velocity drops away from the rotor surface to nearly zero at the stator surface, with no core rotation. The condition at the outside edge of the machine determines the flow type. Batchelor flow is observed in fully enclosed machine systems where a recirculation of fluid from rotor to stator occurs at the periphery. In systems which are open and through-flow ventilated, Stewartson flow may be seen. There is a smooth transition from one flow type to the other, as discussed by Poncet et al. [11], depending on the amount of through-flow. This may vary from one type of AFPM machine to another depending on whether the machine is fully enclosed or through-flow ventilated.

Stator heat transfer has been investigated experimentally by Owen et al. [12], Bunker et al. [13] and Yuan et al. [14], as well as in CFD simulation by Iacovides and Chew [15]. However to date only a very limited range of parameters have been investigated. Generalised stator convective heat transfer correlations that might be applied in the design of AFPM machines are not available in the literature.

II. EXPERIMENTAL RIG

Given the wide variation in available geometries of AFPM machines, it was decided in the present work to focus mainly on a simplified through-flow ventilated system with a flat rotor and a flat stator. Real electrical machines are more complex than this, but studying this simpler system allows comparison with historical work on rotor-stator systems and provides a basic understanding of stator convective heat transfer, as well as tending to give a conservative estimate of stator heat transfer. A brief exploration of the effect of rotor protrusions, usually permanent magnets, on the air flow has also been undertaken.

An experimental rig was constructed to measure stator heat transfer, consisting of a 471 mm diameter rotor driven by a servo motor, and an adjacent heated stator surface allowing direct measurement of stator heat transfer, with 14 channels of spatial resolution and a measurement accuracy of about ±8%. The measurement technique used a thin-film electrical heating method and is fully described in [9], [10] including photographs and drawings. An exploded view of the experimental system is shown in figure 1.

Two rotor configurations were tested: a flat rotor (R1), and a rotor with 16 protrusions designed to mimic the magnets on an AFPM machine (R2), shown in figure 2. The protrusions act like crude fan blades on a centrifugal fan. The axial gap ratio $G$ between rotor and stator was adjustable from 0.01 to 0.09 by insertion of accurately machined spacers. Air was pumped by the spinning of the rotor, from an inlet at the stator centre to four exits at the edge. The air mass flow rate was measured using a calibrated bellmouth entry.
III. CFD Model

Computational fluid dynamics is concerned with the application of numerical methods to solve the partial differential equations governing fluid flow (conservation of mass, conservation of momentum and conservation of energy). The commercial CFD software Ansys CFX was used in the present study. Rotor-stator flows such as those found in AFPM machines exhibit a number of phenomena which are challenging for CFD simulation, such as rotation, confinement, heat transfer, separation, transition from laminar to turbulent flows, and turbulence.

It has been found [16] that 2D axisymmetric CFD simulations are able to capture the important characteristics of rotor-stator flow. Since 2D models are substantially faster to solve, but give useful results, their use in the present work allowed a number of air flow speeds and gap sizes to be investigated. Subsequent 3D CFD modelling was then informed by the 2D results but only one gap size was investigated. In order to predict the air mass flow rate correctly, modelling of the air inlet geometry could not be neglected, and this was only possible using the 2D model. Because the inlet geometry was not modelled in 3D, the inlet total pressure boundary condition used in the 3D model had to be derived from the 2D model results. (Total pressure, sometimes called stagnation pressure, is the sum of the static pressure and the dynamic pressure in the fluid.)

Table I gives a brief summary of the various CFD simulations that were undertaken.

<table>
<thead>
<tr>
<th>TABLE I CFD SCENARIOS</th>
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</thead>
<tbody>
<tr>
<td>Gap ratio</td>
</tr>
<tr>
<td>Outer edge</td>
</tr>
<tr>
<td>Turbulence</td>
</tr>
<tr>
<td>Rotor</td>
</tr>
</tbody>
</table>

One quarter of the entire rotor-stator domain was modelled in 3D for rotor R1, since there are four air exits in the experimental rig. The inlet geometry was not modelled, instead the domain begins at a radius of 38.1 mm; this radius was chosen since it is the point where the curved inlet from the bellmouth and pipe comes to an end. Figure 4 shows the 3D modelled fluid domain in the context of the experimental rig. Whether the flow is laminar or turbulent has a large influence on the stator heat transfer and therefore assumptions must be made about transition from laminar to turbulent flow. A key challenge is that in this type of system, both laminar and turbulent flows may co-exist in one simulation and this is very difficult to model numerically. Based on work that has been undertaken on ‘free rotor’ flows [18], it was decided initially to assume the air was completely laminar for simulations below 600 rpm and fully turbulent for speeds of 1800 rpm and above. Between these speeds, both fully turbulent SST modelling and transition modelling were attempted using the Langtry and Menter $\gamma-\theta$ transition model [19] which is incorporated into CFX. Transition modelling allows laminar and turbulent flows to co-exist in a simulation, and was attempted for rotor R1.

In all simulations it was assumed that air was an ideal gas with constant viscosity, thermal conductivity and specific heat capacity. At the temperatures and speeds of interest these properties do not vary considerably and do not have a large affect on the parameters of interest.

Figure 3 shows the simulated 2D fluid domain, superimposed on a drawing of the experimental rig. The air inlet geometry was modelled excluding the bellmouth itself (which is expected to have low losses).
protrusions (R2), mimicking the permanent magnets of an APFM machine with gap ratio 0.0106. CFX-mesh was used for the meshing of the 2D geometries. There were approximately 40 elements across the gap in the axial $z$-direction and approximately 100,000 elements in total. Meshing for the 3D geometry with rotor R1 was accomplished using Ansys ICEM to produce a fan-shaped regular hexahedral mesh with inflated layers on the rotor and stator with approximately 500,000 elements. Figure 5 shows a close-up of a part of this mesh and it can be seen how the mesh becomes very fine near the top and bottom surfaces where the rotor and stator are located. Meshing for R2 was accomplished using Ansys v12 meshing software to produce an irregular mesh with inflated boundary layers with approximately 425,000 elements. Grid independence tests were undertaken at $Re_{\theta} = 9.6e5$ to investigate the effect of grid size on $Nu(r)$ by comparing 2D meshes both with 89,000, 105,000 and 141,000 nodes in the case of $G = 0.0106$, and 103,000, 118,000 and 154,000 nodes in the $G = 0.0212$ case respectively. There was negligible variation in $Nu(r)$ with respect to grid size in both cases. Solver controls were specified as (1) a convergence criterion and (2) a domain balance criterion. The convergence criterion was that the maximum residual should be less than 1e-4. A domain imbalance (of momentum and enthalpy) of less than 1% was also specified as a requirement. In general, 2D and 3D simulations converged well to these conditions in both laminar and turbulent cases, with the maximum residuals usually less than 1e-5 and sometimes approaching 1e-6.

IV. EXPERIMENTAL RESULTS

Figure 6 shows measured average stator heat transfer versus rotational Reynolds number for various gap sizes using R1 (flat rotor). Both graphs show the same data, with the top graph showing convective heat transfer coefficient whereas the bottom graph shows non-dimensionalised data (Nusselt number). Higher speed tests were conducted at two gap sizes $G = 0.0106, 0.0212$ as shown.

The boundary conditions for rotor R1 (flat) are given in table II. In the case of the 3D simulations, the inlet total pressure was decreased to a negative value to reflect losses in the inlet. In the simulations using rotor R2, the inlet mass flow rate was specified directly from experimental results, instead of specifying inlet total pressure. Additionally, R2 simulations used a rotating reference frame for the fluid domain, with boundary conditions specified in relation to this.

Grid independence tests were undertaken at $Re_{\theta} = 9.6e5$ to investigate the effect of grid size on $Nu(r)$ by comparing 2D meshes both with 89,000, 105,000 and 141,000 nodes in the case of $G = 0.0106$, and 103,000, 118,000 and 154,000 nodes in the $G = 0.0212$ case respectively. There was negligible variation in $Nu(r)$ with respect to grid size in both cases. Solver controls were specified as (1) a convergence criterion and (2) a domain balance criterion. The convergence criterion was that the maximum residual should be less than 1e-4. A domain imbalance (of momentum and enthalpy) of less than 1% was also specified as a requirement. In general, 2D and 3D simulations converged well to these conditions in both laminar and turbulent cases, with the maximum residuals usually less than 1e-5 and sometimes approaching 1e-6.

### TABLE II

**BOUNDARY CONDITIONS USED FOR R1 SIMULATIONS**

<table>
<thead>
<tr>
<th>Boundary</th>
<th>Condition</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inlet</td>
<td>$p_{total} = 0 \text{ Pa}$, $T = 293 \text{ K}$</td>
</tr>
<tr>
<td>Outlet</td>
<td>$p_{static} = 0 \text{ Pa}$</td>
</tr>
<tr>
<td>Rotor</td>
<td>No-slip rotating wall</td>
</tr>
<tr>
<td>Stator</td>
<td>No-slip stationary adiabatic wall</td>
</tr>
<tr>
<td>Heater</td>
<td>No-slip stationary isothermal wall (333 K)</td>
</tr>
</tbody>
</table>

The average heat transfer results can be correlated in the turbulent regime according to a power law:

$$ Nu_{turb} = ARe_{\theta}^B $$

(5)
The constants $A$ and $B$ are given in table III; these are valid in the range $Re_\theta \geq 5.19c5$ for the data shown. All values of $B$ are similar, $B = 0.673 \pm 0.028$. Values of $A$ differ according to gap size $G$.

**TABLE III**

<table>
<thead>
<tr>
<th>G</th>
<th>A</th>
<th>B</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0106</td>
<td>0.0790</td>
<td>0.640</td>
</tr>
<tr>
<td>0.0127</td>
<td>0.0888</td>
<td>0.633</td>
</tr>
<tr>
<td>0.0170</td>
<td>0.0406</td>
<td>0.682</td>
</tr>
<tr>
<td>0.0212</td>
<td>0.0315</td>
<td>0.691</td>
</tr>
<tr>
<td>0.0297</td>
<td>0.0347</td>
<td>0.679</td>
</tr>
<tr>
<td>0.0467</td>
<td>0.0234</td>
<td>0.712</td>
</tr>
</tbody>
</table>

In the laminar regime ($Re_\theta \leq 3e5$), the correlation is expected to have the same functional form i.e. $Nu_{lamin} = ARe_\theta^B$. However, there were a limited number of measured data points in this regime (only four per gap ratio) and additionally the situation is complicated by the non-adiabatic rotor condition (discussed below). Nonetheless the results are approximately correlated according to table IV.

**TABLE IV**

<table>
<thead>
<tr>
<th>G</th>
<th>A</th>
<th>B</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0106–0.0127</td>
<td>14.02</td>
<td>0.204</td>
</tr>
<tr>
<td>0.0170</td>
<td>7.249</td>
<td>0.252</td>
</tr>
<tr>
<td>0.0212–0.0297</td>
<td>2.359</td>
<td>0.336</td>
</tr>
<tr>
<td>0.0467</td>
<td>0.739</td>
<td>0.434</td>
</tr>
</tbody>
</table>

The measured heat transfer results for rotor R2, shown in figure 7, may be correlated by a linear equation in the range $7.4e4 \leq Re_\theta \leq 5.9e5$ as follows:

$$Nu = 0.00067 \times Re_\theta + 118 \quad \text{for } G=0.0212$$

$$Nu = 0.00062 \times Re_\theta + 110 \quad \text{for } G=0.0106$$

Note that these results must be applied with great caution since they are only valid in the range of Reynolds numbers and gap ratios described, and exclusively for through-flow ventilated machines having geometrically similar rotors to R2, viz. 16 magnet poles (8 pole pairs) with magnet inner to outer radius ratio of 0.66. Adjacent magnets are separated by radial slots which are $3.5^\circ$ in size.

V. Comparison and Discussion

A. Flat Rotor (R1)

CFD simulations using the R1 geometry showed a Stewartson flow profile in the laminar regime, but a Batchelor profile with core rotation in the fully turbulent regime. At low speeds a radially inbound flow recirculation at the stator was observed in all simulated configurations, but at higher speeds this is only prevalent at $G > 0.0212$. The simulated temperature profiles in general show the fluid temperature increasing with radius as the fluid is pumped across the heated region. The turbulent thermal boundary layers are much thinner than the laminar layers. The influence of ambient temperature air at the periphery can be seen at both gap ratios, particularly near the edge where there is a drop in fluid temperature near the stator. This is much more prevalent at the larger gap ratio, in both laminar and turbulent results. Some features of the velocity profiles are illustrated in figure 8. This figure shows the non-dimensional radial component of fluid velocity on the left, and the tangential component on the right, versus non-dimensional axial position across the gap. Referring to the left hand figure, it can be seen that near the rotor the fluid is flowing outwards, whereas near the stator it is actually flowing inwards. The right hand figure shows that there are separate boundary layers in the fluid near the rotor and stator respectively, with a rotating core of fluid in the middle. In general, there is a distinct difference between the laminar and turbulent regimes, but the non-dimensionalised turbulent profiles are all quite similar across different speeds.

![Fig. 7. Average heat transfer coefficients and Nusselt numbers, rotor R2](image)

![Fig. 8. Velocity profiles at $r/R = 0.99$, $G = 0.0212$; $z^*$ gives the non-dimensional axial position, equalling zero at the rotor and one at the stator](image)
of ambient temperature air. Average measured heat transfer decreases with increased gap size, although there is a small increase from $G = 0.0106$ to $G = 0.0127$ due to the slightly greater ingress of ambient temperature air at the periphery. Transition from laminar to turbulent flow is observed at $Re_\theta > 3 \times 5$, but this is only pronounced at gap ratios $G < 0.02$ as shown in figure 6.

The correspondence between radially resolved heat transfer measurements vs. CFD is good at low speeds (laminar) and $G = 0.0212$. At gap ratio $G = 0.0106$ low speed correspondence is less good and most of the experimental heat transfer results are higher than the CFD predictions by approximately 50%. This is probably because the CFD boundary condition assumption of an adiabatic (no heat transfer) rotor becomes invalid at low rotational speeds and small gap sizes, where in experiments there is significant heat transfer into the aluminium rotor resulting in higher measured heat transfer.

It was found that the fully turbulent regime CFD simulations tended to always over-predict the air mass flow rate through the system compared with experimental measurements. This is probably because the total pressure loss from ambient conditions through the bellmouth and entry into the rotor-stator gap in the experimental rig is higher than predicted using CFD. As a result of this, a number of fully turbulent CFD simulations were re-run using the experimentally measured mass flow rates as inlet boundary conditions so that heat transfer could be compared in a like-for-like manner. Figure 9 shows the resulting comparison. As can be seen, the simulated results are now further from the measurements. The reason for the discrepancy is due to edge effects as will now be discussed.

![Figure 9](image)

**Fig. 9.** $G = 0.0106$ comparison CFD and experiment

Figure 10 shows a comparison of the radially resolved predictions at $G = 0.0106$ and $Re_\theta = 9.6 \times 5$ with the experimentally determined inlet mass flow, using the baseline Reynolds stress model (BSLRSM), SST model with and without curvature correction (SST curv. corr.) and $k-\epsilon$ model, in both 2D and 3D (blocked periphery) cases. As can be seen, choice of turbulence model does not have a significant influence on heat transfer predictions. In the region $0.6 < r/R < 0.85$ the match between CFD and experiment is quite close. In the region $0.85 < r/R < 1$ all results deviate substantially from the experimental measurements and this is the cause of the deviation seen in the average results. It is generally accepted that modelling of edge effects is difficult; this deviation is probably caused by the differences in geometry at the boundary in the CFD model compared with the experimental rig.

![Figure 10](image)

**Fig. 10.** $G = 0.0106$ comparison CFD & experiment at $Re_\theta = 9.6 \times 5$

The radially resolved comparison results for $G = 0.0212$ at this speed showed a closer correspondence to experiment than the smaller gap ratio particularly in the region $0.85 < r/R < 1$. In the transitional regime, the correspondence between CFD and experiment is not as good as in the fully turbulent regime. Transition modelling does not conclusively provide a better fit.

The primary focus of this paper is stator heat transfer. However, it is informative to compare the stator heat transfer results with the expected heat transfer on the flat surface of the rotor R1. Rotor heat transfer is a well-researched subject and a number of correlations have been published, generally in the form of a power law $Nu = ARe^{\beta}$ relating average rotor heat transfer to rotational Reynolds number. The correlations that are most relevant here are those of Boutarfa and Harmand [20]. If these are compared against the stator heat transfer results given here, it may be seen that in general the stator heat transfer is lower than the rotor heat transfer. The reason is as follows: the heat transfer is dominated by the temperature gradient in the air adjacent to the rotor or stator surface, which in turn is dominated by $\partial V_\theta / \partial z$, the velocity gradient of the tangential velocity component in the axial direction. In the case of through-flow ventilated machines, the subject of this paper, this is higher at the rotor surface compared to the stator surface, because angular momentum is imparted by the machine to the air, which is then expelled from the machine.

### B. Rotor with protrusions (R2)

The CFD simulated non-dimensional velocity and temperature profiles in the gap for rotor R2 were found to be similar in some respects to the profiles obtained for R1. For example, the turbulent tangential velocity profiles exhibited core rotation in the gap, but the laminar profiles showed no core rotation. However, the radial velocity profiles showed a very different flow pattern to R1. It was found that the main route for radial outflow of fluid was in the slot between protrusions and only
a small amount of fluid flows out near the rotor underneath the protrusions; this agrees well with the simulation results of Airoldi et al. [8]. The streamlines, figure 11, show that fluid is entrained into the channel between magnets/ protrusions and flung outwards.

The experimentally measured results for R2 show that the gap ratio seems to have much less effect on the heat transfer than for R1. Additionally, the clear regime change from laminar to turbulent flow at $Re_θ > 3e5$ that occurs with R1 cannot be seen for R2; transition probably occurs at a much lower rotational speed.

A comparison between measured results for R1 and R2 shows that at a comparable speed, average heat transfer with R2 is about 20–30% higher than R1. This result is similar to the CFD comparison but slightly less marked, figure 12.

VI. CONCLUSIONS

This work has compared CFD simulations with experimental measurements of stator heat transfer in a rotor-stator disc system relevant to AFPM machines, with two rotor types. It was found in general that stator heat transfer is always lower than rotor heat transfer. It was also found that CFD modelling is relatively insensitive to the choice of turbulence model for this problem, but accuracy in modelling boundary conditions is very important. There is some comfort to be gained in the result that the CFD is generally conservative. Investigation of the effects of outlet geometry and magnet geometries in the form of rotor protrusions is an area where further research is needed. Correlations have been given for average stator heat transfer in a range of conditions; these should be useful to AFPM machine designers in providing conservative estimates of stator heat transfer.

Finally, it is suggested that cooling might be enhanced through: increased surface roughness, increase air throughflow rate, use of a small gap size ($G < 0.02$), using protruding magnets and evaporative cooling or water cooling. At high speeds however many of these approaches will lead to increased aerodynamic drag (windage) on the machine which may result in a significant efficiency decrease.

VII. ACKNOWLEDGEMENTS

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REFERENCES


