

Growth of myelin figures from parent multilamellar vesicles

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Abstract. We examine the formation and growth of isolated myelin figures, microscale multilamellar tubules, from isotropic micellar solutions of an anionic surfactant. Upon cooling, surfactant micelles transform into multilamellar vesicles (MLVs), whose contact is found to trigger unidirectional growth of myelins. While the MLV diameter grows as $d_{MLV} \propto t^{1/2}$, myelins grow linearly in time $L_M \propto t^1$, with a fixed diameter. Combining time-resolved small angle neutron scattering (SANS) and optical microscopy, we demonstrate that the microscopic growth of spherical MLVs and cylindrical myelins stems from the same molecular mechanism, namely the surfactant exchange from micelles into curved lamellar structures at a constant volumetric rate. This mechanism successfully describes the growth rate of (non-equilibrium) myelin figures based on a population balance at thermodynamic equilibrium.

Keywords. Vesicles, SANS, Myelin, Self-assembly, Surfactant, Liquid crystal.

Synthetic amphiphilic molecules yield intricate self-assemblies, akin to natural phospholipid-based structures in biological membranes, hence providing opportunities for unravelling the complex dynamics and mimicking functionalities of living matter². Elongated, multilamellar, concentric structures of surfactant bilayers, with repeat spacing of a few nm, have attracted special interest due to their resemblance to the striking tubular insulation which encapsulates the axon in neurons, called the myelin sheath^{3–6}. Mimics of myelin figures are typically obtained by bringing a concentrated lamellar phase of a (synthetic or natural) surfactant or lipids in contact with a dilute aqueous solution, as shown in Fig. 1a. Such contact-dilution and immersion experiments provide a simple approach to examine the formation of myelins^{7–12}, and several theories considering diffusion-driven processes^{13–15} and water and surfactant influx mechanisms^{13,16–19} have been proposed to describe the initiation and growth of myelin figures from planar lamellar structures. Resulting experimental observations and analyses are, however, impacted by the geometric, hydrodynamic and physico-chemical complexities arising from the interaction and entanglement between the closely packed lamellar tubes, significant hydration and surfactant gradients. Consequently, direct examination of the formation of isolated myelins under defined thermodynamic conditions has remained challenging^{9,20,21}.

Here, we investigate the growth of isolated myelin figures from multilamellar vesicles (MLVs) of an anionic surfactant, Sodium Linear Alkylbenzene Sulfonate (NaLAS)^{1,22}, formed spontaneously through a thermally-induced phase transformation, see SI for more detail. In a contact-dilution experiment (Fig. 1a), a concentrated NaLAS lamellar phase **A** is diluted in water, and yields a region of populated tubular lamellar structures **B** at its interface, followed by an area covered with an isotropic

micellar phase **I** **C**. Both the planar and tubular lamellar structures appear birefringent and are easily distinguishable from the isotropic solution by polarised microscopy. The dilution occurs at a constant temperature, depicted by a horizontal arrow in Fig. 1a, corresponding to a transition from a mixed liquid crystalline (here lamellar) and isotropic micellar phase to the dilute isotropic micellar phase. For a wide range of surfactant concentration, an inclined temperature-concentration phase boundary separates the micellar (**I**) and the mixed micellar and lamellar liquid crystalline (**I** + **LC**) phases, thus permitting the crossing of this phase boundary at *fixed* surfactant concentration through cooling, as shown in Fig. 1b.

Upon cooling a micellar solution of NaLAS at 10 wt% $< c < 25$ wt%, a fraction of the NaLAS micelles¹ spontaneously forms MLVs, which coexist with the remaining micellar phase in the solution, see Fig. 1b and SI-video1. Under weak sub-cooling conditions (i.e. within $\lesssim 4^\circ\text{C}$ of the phase boundary), the secondary nucleation and growth of the concentric LC phase, at the interface of an existing MLV, is found to initiate the growth of isolated myelin figures as shown in Fig. 1b, see SI-video2. In absence of external stimuli (concentration/temperature gradient or flow fields), these myelin figures are initiated at the point of discontinuity in the curvature generated at the junction of parent MLVs (Fig. 1b). As the myelins grow over time, the boundaries of the parent MLVs remain unchanged, in contrast to the continuously growing diameters of other MLVs in the solution (Fig. 1b). The process is reversible, as myelins can be dissolved back into the micellar phase through heating the solution, see Fig. SI2. Similar growth of isolated long tubular filaments upon cooling has been occasionally observed in suspensions of multilamellar droplets^{17,23–26}. In this letter, we show that growth rate of such out-of-equilibrium tubular lamellar structures is controlled by the thermodynamic equilibrium of **I** + **LC** phases, and occurs through re-arrangement of surfactant molecules from the source micellar self-assemblies into the lamellar

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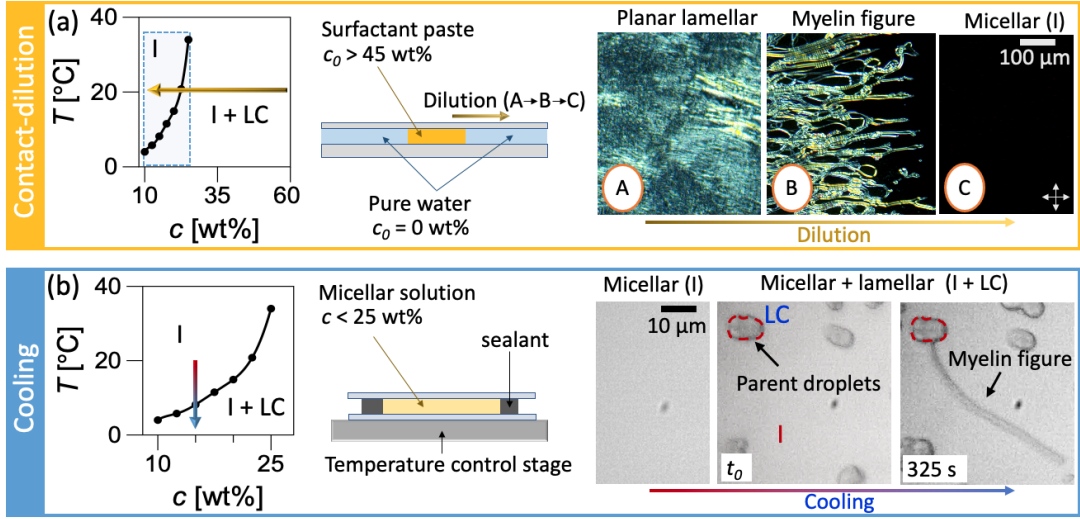


FIG. 1. Growth of myelin figures of NaLAS surfactant in water induced by (a) contact-dilution and (b) cooling experiments. (a) A droplet of aqueous NaLAS mixture $c > 45$ wt% is exposed to pure water at room temperature; the temperature-concentration phase diagram depicts the dilution pathway. Cross-polarised microscopy images show the evolution of the planar lamellar phase (A) as it develops tubular elongated features (B) that extend towards the isotropic micellar phase (C). (b) A droplet of micellar solution of NaLAS is sandwiched between cover slips and sealed around its perimeter. Upon cooling at fixed concentration (here $c = 15$ wt%), a population of micelles transforms into a lamellar phase, spontaneously forming isolated multilamellar vesicles (MLVs), liquid crystalline (LC) droplets. Secondary nucleation on the surface of MLVs yield the formation of long slender tubular structures. Refer to Khodaparast *et al.*¹ for more details on the equilibrium phase boundary between I and I + LC phases of NaLAS.

structures.

To investigate the microscopic growth and accompanying molecular assembly of the isotropic (micellar) and liquid crystalline (MLV and myelin) structures, we perform a series of time-resolved optical microscopy and small angle neutron scattering (SANS) experiments. For optical microscopy measurements, a droplet of the isotropic solution is sandwiched between two cover slips and placed on a thermally controlled stage for bright-field and cross-polarised analyses. An adhesive ring is placed around the droplet to minimise evaporation. SANS experiments in various cooling cycles are performed on the LARMOR diffractometer (ISIS, UK) with a polychromatic neutron beam (with wavelength $\lambda = 0.9$ -13.3 Å) and sample-to-detector distance of 4.1 m, yielding a momentum transfer range of approximately $0.005 < Q < 0.6$ Å⁻¹.²⁷ See Supplemental Material for more information on the experimental settings. Fig. 2a shows a characteristic isotropic (I) micellar solution (at $T = 30$ °C and NaLAS concentration $c = 22.5$ wt%) which is transparent in visible light and exhibits no birefringence; the corresponding SANS profile exhibits a broad peak (at $Q \simeq 0.1$ Å⁻¹), associated with the shape and structure factor of the charged ellipsoidal micelles¹. Decreasing the temperature to $T_f = 0$ °C, corresponding to sub-cooling the solution by $\Delta T \simeq 20$ °C according to phase boundary in Fig. 1, results in the formation of two microscopically distinct LC patterns shown in Fig. 2b: (i) at high cooling rates (here 50 °C/min), a large number of relatively monodisperse microscale LC droplets appear, with birefringence indicative of concentric multilayered vesi-

cles (MLVs). Real-space images of the internal structure of the MLVs are captured using transmission electron microscopy, see Fig. S4. Rapid cooling allows bypassing the intermediate equilibrium states, and MLVs are formed after the final temperature (here 0 °C) has been reached; (ii) at low cooling rates ($\Delta T/\Delta t \leq 1$ °C/min), a small number of isolated, large MLVs form initially, and subsequently become sites for secondary nucleation. A relatively large population of myelin figures form at the location of non-matching curvatures of the initial and secondary droplets. Slow cooling yields continuous formation and growth of MLVs and myelin figures within the solution exposed to constant temperature drop at the rate of $\frac{\Delta T}{\Delta t} = 0.5$ °C/min. While the two LC structures obtained in (i) and (ii) are microscopically distinct, the nanoscale SANS scattering patterns obtained at similar conditions are effectively identical with an overlapping Bragg peak position, associated with the bilayer d-spacing of $d_s \approx 30.2$ Å (Fig. 2b). In both cases, the LC phase coexists with the isotropic micellar phase (I) whose scattering profile spans across the intermediate Q range. SANS measurements at different cooling rates, demonstrate that within the coexisting I + LC region, an equilibrium population ratio is established between the I and LC phases, which is solely determined by the final equilibrium temperature T_f and surfactant concentration c , regardless of the thermal history and cooling pathway.¹ Furthermore, formation of larger MLVs and myelin figures in slow cooling experiments, suggests that weak sub-cooling is essential to achieve polydispersity and myelin growth, see Fig. S5. We note that the scattering inten-

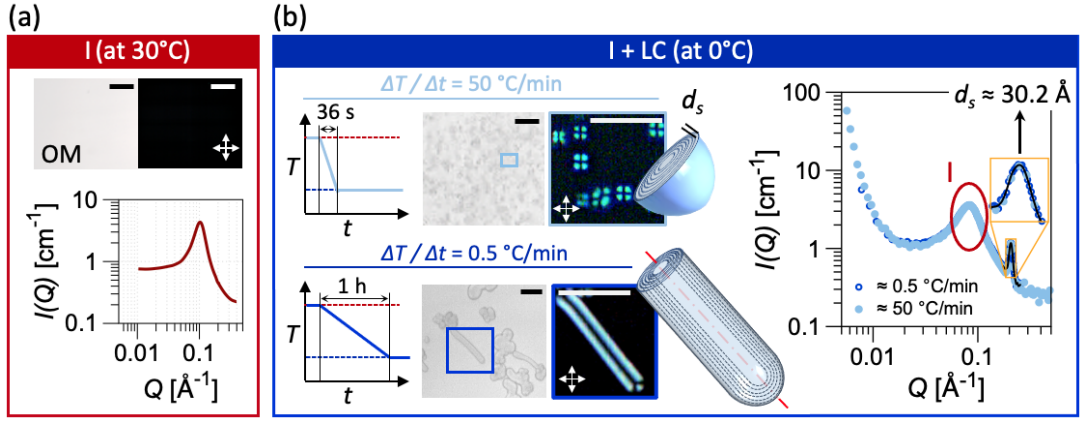


FIG. 2. Micro and nanoscale analyses of the LC structures formed upon cooling the aqueous solution of 22.5 wt% NaLAS. (a) At 30 °C, micellar solution (phase I) appears transparent and black in optical and polarised microscopy, with a SANS profile characteristic of charged ellipsoidal micelles. (b) At 0 °C, relatively monodisperse multilamellar (birefringent) droplets nucleate when the solution is cooled rapidly ($> 10^\circ\text{C}/\text{min}$), while mixed population of larger MLVs and myelin figures are obtained when the solution is cooled slowly ($< 1^\circ\text{C}/\text{min}$). SANS measurements of both solutions at 0 °C exhibit a clear Bragg peak located at $Q \approx 0.208 \text{ \AA}^{-1}$, corresponding to bilayer spacing of $d_s \approx 30.2 \text{ \AA}$. The lamellar LC phase coexists with the micellar phase (phase I + LC), manifested by the micellar scattering profile with peak at $Q \approx 0.08 \text{ \AA}^{-1}$. Scale bars correspond to 10 μm . Equilibrium saturation temperature of the solution at 0 °C is approximately 21 °C, providing $T_s - T_f = 21^\circ\text{C}$.

sities vary slightly in the low- Q region, as expected from the formation of distinct microscale aggregates in slow and fast cooling tests. The growth of MLVs and myelin figures upon cooling is reversible and heating returns the solution to the micellar phase, see Fig. S2 and SI-video1.

We next report on isothermal experiments in which the micellar solution is rapidly quenched (at $50^\circ\text{C}/\text{min}$) to reach a series of temperature T_f and held isothermally. T_f is chosen to be close to the phase boundary to provide weak sub-cooling and larger population of myelin figures. Isothermal experiments allow us to eliminate thermal diffusion as the potential driving mechanism for growth of myelins in our system¹⁴. The geometric evolution of the myelins and MLVs with time is examined as a means to elucidate the underpinning growth mechanism. Most previous studies reported power laws $L_M \propto t^{0.5}$ for radial ensemble growth of myelin figures in contact dilution experiments^{9,10,16,28}. Notable exceptions to this trend include the linear growth $L_M \propto t$ of individual myelins observed by cooling a mixed surfactant solution reported by Toquer *et al.*²³, and in droplet drying experiments reported by Zou and Nagel^{17,18}. In our isothermal experiments at fixed surfactant concentration, we find that while the diameter of MLVs grows with square root of time, $d_{MLV} \propto t^{0.5}$, the length of myelin figures follows $L_M \propto t^1$ with an effectively unchanged base diameter d_M (Fig. 3). This scaling holds for considerable time, close to the point at which temperature-dependent population balance between I and LC phases is reached. The distinct evolution of the spherical MLVs and cylindrical myelins, with an *identical* bilayer structure and thermodynamic driving force, suggests that the dimensionality of the microscale geometry of the LC structure might determine the scaling with time.

Previous time-resolved small angle scattering analy-

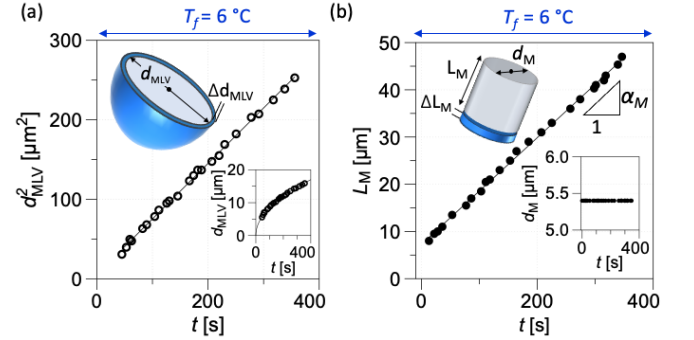


FIG. 3. Isothermal growth of MLVs and myelin figures at $T_f = 6^\circ\text{C}$ ($T_s - T_f = 2^\circ\text{C}$) for $c = 15 \text{ wt}\%$. (a) The diameter of the MLVs (d_{MLV}) increases with $t^{1/2}$. MLVs grow through accumulation of thin bilayer shells. (b) Myelin figures grow linearly in length L_M through accumulation of thin discs, maintaining an unchanged diameter (here $d_M = 5.4 \pm 0.3 \mu\text{m}$).

ses have suggested that spherical MLVs grow through accumulation of effectively two-dimensional uni-lamellar shells^{1,29–31}, here yielding an outward radial growth of the droplets that is clearly observable in optical analyses. The volumetric growth unit of MLVs is thus estimated by $\Delta V_{MLV} = \pi d_{MLV,t}^2 d_s$ as a function of time, where $d_{MLV,t}$ is the time-dependent MLV diameter and d_s is the constant shell thickness, set by the bilayer spacing (Fig. 3a). Myelin figures, however, maintain their initial cross-sectional diameter unchanged, while growing one-dimensionally in length. Therefore, volumetric growth unit of myelins at any time instance yields $\Delta V_M = \frac{\pi}{4} d_M^2 \Delta L_{M,t}$, highlighted in bright blue color in Fig. 3b, where $\Delta L_{M,t}$ is the axial unit growth. Our ex-

perimental data presented in Fig. 3 show that the rates of increase for $d_{MLV,t}^2$ and $\Delta L_{M,t}$ are constant in time, thus suggesting that growth of both structures is affected by a constant volumetric inflow, *i.e.* $\frac{\Delta V}{\Delta t}$ is constant. The linear growth of myelin figures observed here, suggests a cross-sectional growth through the root,¹⁷ as opposed to growth via absorption of surfactant on the external cylindrical body of the structure suggested by Pratibha and Madhusudana which yields an exponential growth.²⁵

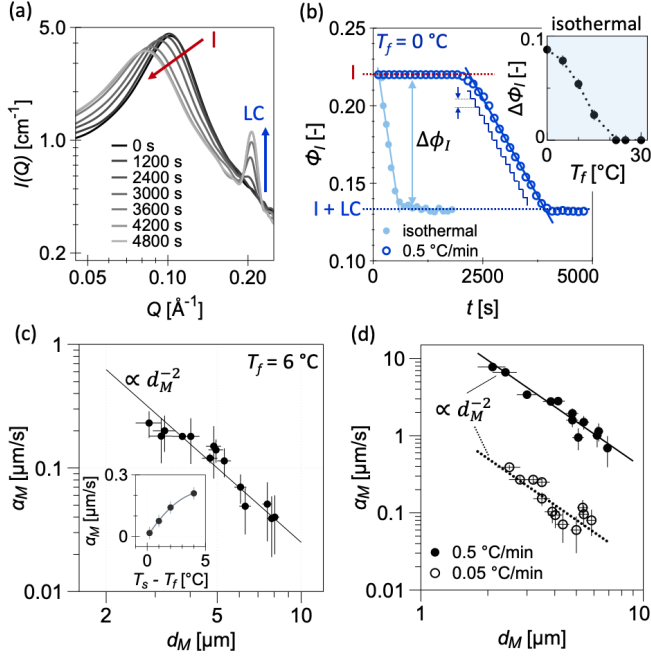


FIG. 4. Conversion from the micellar to the LC phase upon cooling. (a) Time-resolved SANS scattering data for 22.5 wt% NaLAS solution, cooled from 30 °C down to 0 °C at 0.5 °C/min. (b) The volumetric concentration of micelles Φ_I decreases linearly in time upon phase transformation affected by cooling. Horizontal red/blue dotted lines depict equilibrium volumetric concentration of micelles in the I/I+LC phases at 30 °C/0 °C. $\Delta\Phi_I$ is the difference between the equilibrium volumetric concentration of micelles. The inset shows the reduction in $\Delta\Phi_I$ as the final equilibrium temperature T_f increases. (c) The rate of the linear temporal growth of the myelin figures α_M at a given thermodynamic state ($c = 15$ wt%, $T_f = 6$ °C) is inversely proportional to d_M^2 . Reducing T_f in independent isothermal experiments, accelerates the growth of myelin figures, plotted versus $T_s - T_f$, where T_s is the saturation temperature at $c = 15$ wt%. (d) α_M obtained in slow cooling experiments performed at 0.05 and 0.5 °C/min. Higher cooling rates result in faster growth of myelin figures, while in both measurements $\alpha_M \propto d_M^{-2}$.

The growth of both MLVs and myelin figures occurs by promoting a conversion from the micellar to the lamellar phase upon cooling, which can be quantified by time-resolved SANS, see an example in Fig. 4a. Monitoring the evolution of the scattering profile arising from the micellar and lamellar structures, the volumetric concentration loss of the micellar phase Φ_I during this transformation can be readily computed, as shown in Fig. 4b.

See more details in the Supplemental Material. **Significantly, the loss in volumetric concentration of micelles is largely linear in time, corroborating that a constant volumetric inflow of surfactant controls the growth rate of both MLVs and myelin figures.** All quantitative data on the growth of myelin figures and MLVs presented here are collected during the linear conversion period. Governed by molecular diffusion, the linear conversion trend slows down as the solution approaches equilibrium (Fig. 4b), see the SI for comparison between growth rates at the main linear and late stage of the material conversion. The magnitude of the final equilibrium volumetric concentration of the micellar phase is defined by T_f , regardless of the cooling history. As discussed earlier, rapid cooling allows monitoring the transformations that occur at the final temperature T_f as the result of solution exposure to total $\Delta\Phi_I$ (Fig. 4b). Expectedly, $\Delta\Phi_I$ obtained in isothermal experiments increases at lower final equilibrium temperature T_f , see the inset in Fig. 4b. The constant volumetric growth of myelins imposes a reduction in the myelin growth rate α_M (defined as the proportionality constant, $L_M \equiv \alpha_M t$) as the myelin base diameter d_M increases, at given c and T_f . Isothermal measurements presented in Fig. 4c show not only a reduction in α_M for thicker myelin figures, but also a clear power-law correlation $\alpha_M \propto d_M^{-2}$ as expected from the volumetric argument above. In line with SANS analyses, the myelin growth rate increases as deeper level of sub-cooling (larger $T_s - T_f$ and $\Delta\Phi_I$) are reached, see the inset in Fig. 4c. In contrast, slow cooling rates impose gradual transformation through exposure to a series of relatively weaker sub-cooling and $\Delta\Phi_I$ (Fig. 4b). Under such conditions, the rate of transfer from the micellar to the lamellar phase is impacted by the rate of cooling. Optical microscopy measurements of myelin growth during continuous cooling at constant rates (Fig. 4d) show that increasing the cooling rate by an order of magnitude leads to similar enhancement in growth rate of myelin figures. Similar to isothermal measurements, the myelin growth rate at a fixed concentration inversely scales with d_M^2 (Fig. 4d).

In conclusion, we identify the transfer of surfactants molecules, from micelles to lamellar structures, as the mechanism governing the temporal growth of both MLVs and myelin figures. While myelins are non-equilibrium structures¹⁷, we find that their growth kinetics can be described by a simple geometric argument and finely tuned by the thermodynamic driving force between equilibrium states, here traversed by temperature changes. Our measurements indicate no significant bilayer spacing change during myelin growth, and therefore the mechanism proposed²⁰ for myelin growth from planar lamellar structures based on compensation in curvature energy is not applicable to our system. In static conditions, myelins figures in our system grow at the non-matching curvature contact points of primary and secondary MLV droplets. By contrast, under hydrodynamic shear stress, we find myelins to spontaneously grow from single droplets maintaining the parent droplet diame-

ter, thus acquiring hemispherical caps on both ends, see Fig. SI7. **Linear elongation of myelin figures with a constant cross-sectional diameter suggests that they grow via an inflow of surfactant molecules through their root,¹⁷ as opposed to absorption on their cylindrical interface.²⁵ The question of what initiates the growth of the isolated myelin figures observed here remains to be answered through further investigations.** Overall, our findings demonstrate that precise knowledge of thermodynamic equilibrium phases in surfactant solutions, and associated transition kinetics, is essential to mechanistically describe and control the formation and dynamics of these fascinating amphiphilic self-assemblies.

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