1	[Title Page]
2	
3	
4	
5	
6	A Novel Data-Driven Framework Based on BIM and Knowledge Graph for
7	Automatic Model Auditing and Quantity Take-off
8	
9	Hao Liu ^a , Jack C.P. Cheng ^{a,*} , Vincent J.L. Gan ^{b,*} , Shanjing Zhou ^c
10	
11	^a Department of Civil and Environmental Engineering, The Hong Kong University of
12	Science and Technology, 999077, Hong Kong.
13	^b Department of the Built Environment, National University of Singapore, 117566,
14	Singapore.
15	^c Centre for Systems Engineering and Innovation, Department of Civil and Environmental
16	Engineering, Imperial College London, London, SW7 2AZ, UK.
17	*Corresponding authors.
18	Email: cejcheng@ust.hk (Jack Cheng); vincent.gan@nus.edu.sg (Vincent Gan)

19 ABSTRACT

Model auditing is a critical step before conducting Building Information Modeling (BIM)-20 based Quantity Take-off (QTO) because these models may contain various human errors 21 22 and mistakes, leading to insufficient semantic information and inconsistent modeling style in BIM models. The traditional object-oriented approach has difficulties in representing 23 24 unstructured BIM data (e.g., interrelationships), while rule-based methods involve tremendous human efforts to develop rule sets, lacking flexibility for different 25 26 requirements. Therefore, this study aims to establish a novel data-driven framework based on BIM and knowledge graph (KG) to represent unstructured BIM data for automatic 27 inferences of auditing results of BIM model mistakes. It starts by establishing a BIM-KG 28 data model via identifying required information for auditing purposes. Subsequently, BIM 29 30 data is automatically transformed into the BIM-KG representations, the embeddings of which are trained using a knowledge graph embedding model. Automatic mechanisms are 31 32 then developed to utilize the computable embeddings to effectively identify mistake BIM elements. The framework is validated using illustrative examples and the results show that 33 34 100% mistake elements can be identified successfully without human intervention.

35

36 Keywords:

Building information modeling, Quantity take-off, BIM information quality, BIM modelauditing, Knowledge graph embedding

39

40 1. INTRODUCTION

Quantity take-off (QTO) is a process of recognizing measurement items, obtaining 41 42 dimensional information, and calculating the items in units such as areas and volumes from construction documents [1]. It plays a significant role in a construction project since it 43 44 affects multiple important tasks throughout the project lifecycle, such as the estimation of preliminary cost in early design, preparation of the bill of quantities for project tendering, 45 46 and material procurement in construction [2,3]. Traditionally, QTO is time-consuming and error-prone as it requires professional quantity surveyors to manually interpret 2D design 47 drawings and calculate the results based on predefined rules in the measurement standards 48 [4–6]. With the development of Building Information Modeling (BIM) techniques, this 49

process has been revolutionized because quantities can be automatically extracted from 3D models together with the geometric attributes [5]. Therefore, the BIM-based QTO can provide more automatic and accurate estimation of material quantities, greatly reducing human effort and errors in estimations [5,7,8].

In order to obtain accurate quantities that are compliant with measurement 54 standards under the BIM-based method, BIM models need to be created in a consistent 55 way according to specifications on modeling styles and semantic information [9–11]. Fig 56 1 illustrates how the inconsistent modeling styles can impact quantities from BIM models: 57 because the geometric representations are different, the output quantities are different for 58 the beam (and the slab) in the two modeling styles shown in Fig 1 (a) and (b). According 59 to the Hong Kong Standard Method of Measurement [12] (HKSMM) where the major 60 61 measurement logic is similar to that in commonwealth countries (the UK, Singapore, etc.), either may be correct, depending on the concrete grade information. As shown in Fig 2, if 62 63 the beam has a different concrete grade than the slab, it is measured through the slab (i.e., $b \times l \times h_1$; otherwise, it is measured to the soffit of the slab (i.e., $b \times l \times h_2$). In this case, 64 65 all the beam-suspended slab joints should be created in either of the ways but consistently 66 to enable easy adjustments for the output quantities to achieve accurate QTO. For instance, if all the beam-suspended slab joints in the BIM model are created in the way shown in Fig. 67 1 (a), accurate beam quantities can be obtained by simply making 0 or $b \times l \times (h_1 - h_2)$ 68 adjustments for all the beams according to the concrete grade information after extracting 69 the quantities (i.e., $b \times l \times h_1$) from the BIM model. Otherwise, if there are multiple 70 modeling styles (e.g., the styles shown in Fig 1 (a) and (b)) for such beam-suspended slab 71 72 joints, it would be time-consuming to make adjustments for the beams created in different ways. In addition, as Fig 2 shows, BIM models should contain sufficient semantic 73 74 information such as concrete grade so that the calculation logic can be determined successfully in the BIM-based QTO process. 75



Fig 1. Inconsistent modeling styles for a beam-suspended slab joint (adopted from [13])

CLASSIFICATION TABLE	MEASUREMENT RULES		
 18. Suspended slabs 19. Coffered and troughed slabs 	m ³	 ³ 1. Horizontal 2. Sloping ≤ 15° 3. Sloping > 15° 	M.12 The measurement of suspended slabs is taken across columns and beams, except where the columns or beams are of a different mix.

78

79

Fig 2. Part of the HKSMM descriptions for measuring slab quantities [12]

Nevertheless, it is not uncommon to see different BIM modelers using different 80 methods of modeling in practice [3,14], resulting in different modeling styles for the same 81 82 thing, regarding the precedencies between elements in different parts of the building and making the output quantities troublesome to adjust. In addition, they are not as aware of 83 84 the importance of the required information in BIM models for QTO as quantity surveyors are [15]. Thus, the BIM models may not contain all the necessary information for 85 86 determining the measurement logic in the standards [16]. Therefore, it is necessary to audit BIM models against agreed specifications to ensure a consistent modeling style and 87 88 sufficient semantic information in the BIM model before conducting BIM-based QTO.

However, the proper representation of unstructured BIM data for model auditing is still a matter of concern. BIM information is stored in an object-oriented and parametric manner, indicating that a BIM model is assembled by different elements with different sets of properties [17,18]. Such object-oriented representations are implicit when expressing the unstructured interrelationships between elements [19]. An example of different

precedencies and topological relationships between building elements regarding their 94 95 modeling styles is shown in Fig 1. The second challenge concerns the utilization of the representation of unstructured BIM data for automatic BIM model auditing. The specified 96 requirements are buried in various texts. Heavy human intervention is required to align 97 them with the BIM data so as to identify elements that are not modeled appropriately. Thus, 98 an automatic way that utilizes BIM data to identify the mistake patterns is needed to reduce 99 the considerable human effort in this process. As a semantic graph representation with 100 101 heterogeneous features, Knowledge Graph (KG) [20] provides new insights to express and process object properties and relationships explicitly and automatically. Previous studies 102 have leveraged such a representation for BIM model information management [21-24], 103 104 demonstrating the potential of KG to analyze the rich semantics in BIM models. However, 105 the application of KG for BIM model auditing is still unmature.

Therefore, this study aims to develop a novel data-driven framework, with the aid 106 107 of BIM and KG, to automatically audit BIM models for the purpose of QTO. This includes the design of KG-based representation and transformation mechanisms to express 108 109 unstructured BIM data, as well as the development of BIM-KG data manipulation and inference mechanisms to determine auditing results efficiently for mitigating human 110 111 intervention. Since concrete structures are one of the most common structures and their quantities from BIM are vulnerable to the aforementioned modeling issues, this study 112 113 includes them as the scope of QTO-oriented BIM model auditing. Meanwhile, this study 114 focuses on auditing mistakes about semantic information (i.e., absent or inappropriate semantic attributes) and modeling style (i.e., inconsistent topological arrangements 115 between elements) considering that they are typical modeling concerns in BIM models 116 117 [9,15,25]. The proposed framework begins with the establishment of a BIM-KG data model 118 through identifying the required information to conduct BIM model auditing for QTO. Based on the BIM-KG data model, BIM data is transformed to the KG representations 119 automatically. Following this, manipulation mechanisms utilizing the transformed 120 representations are designed to efficiently identify the elements not in compliance with the 121 122 requirements. The performance of this proposed framework is validated using a set of BIM models with different kinds of mistakes about semantic information and modeling style. 123

The rest of the paper is organized as follows: Section 2 introduces related studies about BIM modeling specifications, attempts on BIM model auditing and using knowledge graph techniques for BIM. Section 3 describes the methodology part, including the BIM-KG data model, transformation, and utilization mechanisms to conduct BIM model auditing automatically, followed by the illustrative examples to validate its performance in Section 4. Finally, Section 5 presents the conclusion and future work.

130

131 2. RELATED WORK

As shown in Fig 3, previous studies are reviewed from two aspects in this section, 132 namely BIM model auditing and knowledge graph techniques for BIM. Section 2.1 133 introduces BIM modeling specifications about semantic information and modeling styles 134 135 to state the necessity and contents of auditing requirements. Section 2.2 focuses on existing methods to audit BIM models against the auditing requirements as well as their limitations. 136 137 Section 2.3 aims to review the uses of knowledge graph techniques in BIM to show the potential benefits of such techniques to the auditing. Finally, research gaps are identified 138 139 in a summary.



140 141

Fig 3. Overview of related work

142 2.1. BIM Modeling Specifications

The construction industry is dominated by official and/or recommended specifications to guide its activities and procedures [9]. Likewise, BIM models should be created having uniformity so as to prevent conflicts in downstream applications. To achieve this, administration organization/regulatory bodies in different areas issue various BIM

modeling specifications to regulate BIM modeling practice, some of which emphasize the 147 requirements on semantic information and modeling style in BIM models. The Standard 148 for Graphic Expression of Building Information Modeling [26] in China includes 149 general descriptions about the types of required semantic information and detailed 150 guidance about joining precedencies when modeling joints to regulate BIM model 151 expressions for different disciplines. Similarly, the Hong Kong Housing Authority issued 152 the Standard Approach of Modeling (SAM) [27] for creating structural BIM models with 153 emphasis on some semantic information in particular and explicit descriptions about 154 consistent BIM modeling methods. As for QTO, two BIM requirements [28,29] in Finland 155 specify the required semantic information (e.g., construction type, material type) and how 156 BIM models should be created consistently, especially for joining precedencies between 157 158 different building elements (e.g., "The joining of slabs and walls must be modeled such that 159 the slab ends to the surface of the load-bearing wall structure without extending inside it."), 160 in detail to ensure that BIM models meet necessary conditions for QTO purposes. In addition, the National BIM Standard-United States Version 3 (NBIMS-US V3) [30] 161 162 published by National Institute of Building Sciences in the US describes detailed exchange requirements from design to QTO (e.g., classification code, construction type) so that the 163 quantities can be generated from BIM models successfully. The BIM Model Information 164 Requirements for Quantity Take-off (BIM MIR for QTO) [31] from the Hong Kong 165 166 Institute of Surveyors also emphasizes the importance of semantic information in BIM 167 models and specifies the minimum information requirements (e.g., concrete grade) as well as basic modeling styles to ensure consistency for QTO (e.g., "Beam is defined as 168 169 horizontal element. The beams will not cut the vertical element. The geometry of beams is 170 joined with the slabs where the slabs take precedence."), supplemented with guidance on 171 extracting quantities in compliance with measurement rules. These specifications emphasis 172 and specify the requirements of semantic information and modeling styles for BIM models to support downstream tasks (e.g., QTO) and produce consistent results [26-31]. However, 173 174 the requirements are buried in texts. How to align them with BIM data to make sure BIM models follow these specifications is unclear and needs further investigations. 175

176

177 2.2. BIM Model Auditing

To tackle this problem, some software tools have been developed to audit BIM 178 models before the model delivery between different disciplines to ensure that the specified 179 180 requirements in the specifications are satisfied. For example, Solibri Model Checker [32] is widely adopted to check the required semantic data and geometry constraints (e.g., 181 spacing limit, clashing elements) in Industry Foundation Classes (IFC) models through 182 rigorous rule patterns set by domain experts. Similarly, through customizing rule sets, 183 Autodesk Model Checker for Revit [33] can check Revit models against the requirements 184 185 and generate compliance reports. On the other hand, various studies have explored ways to formulate systematic frameworks utilizing different software tools so that BIM model 186 auditing can be performed comprehensively. Zadeh et al. [34] proposed a framework to 187 assess the information conformance with owner requirements when using BIM models for 188 189 facility management (FM), and conducted testing by integrating different tools such as Solibri Model Checker and Revit Schedule. Cavka et al. [35] defined levels of owner's 190 191 operational requirements in the FM stage, including model structure, model content, and design compliance, and proposed ways to audit BIM models before handover mainly based 192 193 on Solibri Model Checker. Similarly, with the help of the Solibri Model Checker, Gholami 194 et al. [36] performed the quality checking of BIM models against the energy analysis 195 requirements such as architectural layout and general space check (e.g., space boundary). 196 Making use of customized checklists and queries on database systems such as Microsoft 197 Access, Donato et al. [37] assessed the information quality (e.g., adequacy, readability) of BIM models during the architectural design process. In short, these studies attempted to 198 199 audit BIM models with respect to the requirements on semantic data and geometry constraints, with predefined rule patterns that involve extensive human effort and external 200 201 software tools outside the BIM authoring software.

202

203 **2.3. Knowledge Graph for BIM**

A knowledge graph is a representation of facts using a graph-structured data model, which includes: 1) entities that are real objects or abstract concepts; 2) relationships between entities; 3) semantic descriptions denoting the meanings of the entities and relationships (e.g., type, property) [38]. It is referred to a graph due to the graph data structure [39] and a knowledge base for manipulation and inference based on the stored

facts [40]. The graph representation provides explicit expressions of entities and 209 210 relationships with rich semantics [41-43], and thus is more amenable to semantic pattern 211 recognition [44]. Such a representation technique has been explored to represent and analyze BIM information that inherently contains heterogeneous entities and relationships 212 for different purposes. For example, the graph representation can be used to express BIM 213 214 models for BIM data management. The semantic information and relationships (e.g., connectivity, containment) in BIM models can be represented using graph data models, 215 216 based on which flexible and efficient information queries can be achieved [21,22]. The flexibility of graph representation can also support generative building design. Through 217 representing spaces as entities and adjacencies as relationships, spatial layout designs can 218 219 be generated using graph transformations [45,46] and evolutionary algorithms [47]. 220 Moreover, some studies have explored the use of graph representations to validate BIM data against certain requirements. Pauwels et al [48] described a typical semantic rule 221 222 checking process by extracting related IFC information and making use of semantic web rules or Resource Description Framework (RDF) graphs to express rules. Zhong et al [49] 223 224 developed an ontology-based framework to support building environmental compliance 225 checking under BIM environment, where knowledge about BIM, environmental 226 information and building regulations is expressed in ontologies and SPARQL rules are 227 utilized to conduct the rule-reasoning process. Jiang et al [50] presented BIM models and 228 building codes in ontologies and developed mapping and checking rules to automatically 229 validate BIM data against ambiguous regulatory information. In short, these studies tried 230 to automate the BIM data validation process using ontological representations and rule-231 based reasoning techniques, which rely heavily on human experts to develop both graph 232 representations and rules.

In summary, BIM models need to have sufficient semantic information and consistent modeling style to enable a smooth BIM-based QTO process. There are some studies [34–37] trying to check such prerequisites from specifications and/or owner's requirements for BIM models. But their representations of BIM data are limited to an object-oriented approach and have difficulties in expressing and auditing the unstructured complex constraints (e.g., appropriate joining precedencies between different building elements) explicitly. Moreover, their ways of relying on external software tools and

predefined rule patterns to compare BIM data against the requirements are labor-240 241 consuming. A few studies have demonstrated the strength of graphs to represent and validate BIM information. However, a proper representation for auditing both semantic 242 information and modeling style is still lacking. On the other hand, existing studies are still 243 limited to a top-down approach that requires considerable effort from domain experts to 244 design both graph representations and validation rules. To address these problems, this 245 study proposes a semi-bottom-up framework that is driven by BIM data in compliance with 246 the requirements and proper BIM-KG representations to automatically identify 247 problematic BIM models. Proper BIM-KG representations and the transformation 248 mechanisms are designed to explicitly express unstructured BIM data in terms of semantic 249 information and modeling style. A knowledge graph embedding model is utilized to 250 251 transform the BIM-KG data into embeddings/vectors, based on which corresponding mechanisms are developed for automatic inferences of auditing results. 252

253

254 **3. METHODOLOGY**

255 Fig 4 presents an overview of the proposed methodology, with explanatory pictures 256 attached as examples for some key concepts and steps. Knowledge from QTO-related BIM 257 modeling specifications (e.g., BIM MIR for QTO [31]) is leveraged to identify the 258 requirements (e.g., requirements on semantics and topology aspects) for QTO-oriented 259 BIM model auditing. Following this, the BIM-KG data model is established to represent 260 relevant entities, attributes and relationships and the standard BIM model is defined as a 261 BIM model that has sufficient semantic information and consistent modeling style according to the requirements from relevant specifications. Based on the BIM-KG data 262 263 model, BIM model information of interest (e.g., semantic information, topological 264 arrangement relationship) that is needed to audit the identified requirements is automatically transformed from a standard BIM model to BIM-KG triples in the form of 265 266 <head, relation, tail> through attribute extraction and geometry manipulation. An improved knowledge graph embedding model (i.e., improved TransR) is then used to get 267 the embeddings of the standard BIM-KG triples. For the new BIM model to be audited, the 268 269 corresponding new BIM-KG triples are generated and their embeddings are obtained through contextual comparison between the standard BIM-KG triples and the new ones. 270

- Furthermore, the embeddings are utilized to score those new BIM-KG triples and automatically decide on the auditing results with respect to a self-determined proper threshold (i.e., a value that can clearly distinguish scores of correct and mistake BIM-KG
- triples / elements given that correct and mistake triples / elements have high and low scores,
- respectively). The rejected elements are returned to the BIM modelers for modification
- over several rounds until acceptance. Details of the methodology are described in following
- 277 subsections.



Fig 4. Overview of the proposed methodology framework

281 **3.1. BIM-KG data model**

282 **3.1.1. BIM-KG information requirements**

283 In this study, BIM Model Information Requirements for Quantity Take-off (BIM MIR for QTO) [31] by The Hong Kong Institute of Surveyors is selected as an example 284 BIM modeling specification for illustration. The requirements on semantic information and 285 consistent modeling style are common to most BIM modeling specifications. Regarding 286 the auditing scope, typical building elements (i.e., slab, beam, column, wall) are selected 287 for illustrative purposes. The requirements mainly cover two aspects: 1) consistent 288 modeling style. Fig 5 shows the requirements on the modeling style of beams as an example. 289 Vertical elements and slabs take precedence over beams. In essence, it shows the 290 requirements on the proper topological arrangement relationships between elements. 291 292 Different topological arrangements result in different contact situations between elements. For instance, the slab is in contact with the side and top of the beam when the beam and 293 294 slab take precedence, respectively (shown in Fig 1). Therefore, the topological contact relationships between elements are required to identify different modeling styles. In 295 addition, connectivity information is needed since elements are connected with each other 296 297 at the joints. 2) sufficient semantic information. To perform the QTO logic specified in the 298 measurement rules for these common concrete elements, elements should carry adequate 299 object information including concrete grade and construction type (e.g., horizontal/slope 300 etc. in the beam example shown in Fig 5).



301

Fig 5. Example requirements on modeling style of beams (description in the
specification: *Beam is defined as horizontal element. The beams will not cut the vertical element. The geometry of beams is joined with the slabs where the slabs take precedence.*) (adopted from [31])

307 3.1.2. BIM-KG representation

308 Based on the identified required information for QTO-oriented BIM model auditing, a BIM-KG data model is established to transform BIM data into KG triples with reference 309 to the IFC data model under IFC4_ADD2_TC1 [51]. Fig 6 shows how the nodes, relations, 310 311 and auxiliary information in the BIM-KG data model are mapped and established based on the identified information requirements for auditing in Section 3.1.1. For example, as 312 313 concrete grade information is needed for auditing, the nodes *element* and *concrete grade* and the relation *has_concrete_grade* are mapped from the entities *IfcBuildingElement*, 314 IfcPropertySet, and IfcRelDefinedByProperties specified in the IFC data model. Although 315 level information is not included in the required information for auditing, it can be utilized 316 317 to locate elements. Thus, level information is defined as auxiliary information in the *element* nodes. In addition to those nodes and relations that can be established in reference 318 319 to the IFC data model, the relation *contact_with* is introduced to associate face nodes (i.e., top, side, bottom) with element nodes so that the information about topological 320 321 arrangement relationships between elements mentioned in Section 3.1.1 can be captured 322 for auditing modeling styles. Of note is that the *element* entity can be a *real element* or 323 *empty* since elements and their faces may not join/contact with anything. To construct this 324 BIM-KG, triples in the form of *<head*, *relation*, *tail>* with auxiliary information (i.e., 325 levels of the elements) are generated from the BIM models, which will be introduced in next section. Table 1 lists some examples of triples under the defined BIM-KG data model. 326



	<element, element="" has_concrete_grade,=""></element,>	< beam_123 ¹ , has_concrete_grade, C30>
	<element, element="" join_with,=""></element,>	<beam_123<sup>1, join_with, slab_234¹></beam_123<sup>
	<element, has_surface,="" top=""></element,>	<beam_123<sup>1, has_surface, beam_top></beam_123<sup>
	<top, contact_with,="" element=""></top,>	<beam_top, contact_with,="" slab_234<sup="">1></beam_top,>
332	¹ : 123 and 234 are the unique identifiers of the el	ements and serve as suffixes to distinguish
333	different element instance entities	
334		

336 **3.2.** Automatic Transformation to KG

With respect to the BIM-KG data model in Fig 6, a transformation mechanism is 337 338 developed to automatically convert BIM data into BIM-KG triples to construct the BIM-KG. The details are illustrated in Fig 7 with *beam_123* as an example. First, the category 339 and ID information of the element are extracted to form a unique entity name. The semantic 340 341 attributes and joining elements are obtained to generate triples on semantic information and element connectivity such as *<beam_123*, *has_concrete_grade*, *empty>* and 342 *<beam_123, join_with, slab_234>*. The generation of triples related to the topological 343 contact information between elements is based on [13]. The faces of the element are 344 extracted and thickened on both sides (i.e., the extracted faces are extruded into solids, as 345 shown in Fig 7). Intersection checking is performed between the corresponding generated 346 347 solids and other elements to detect the elements in contact with the faces. As a result, triples such as *< beam_side*, *contact_with*, *slab_234>* and *< beam_side*, *contact_with*, *empty>* are 348 obtained. Finally, these triples form the base of the BIM-KG for model auditing. 349



Fig 7. Mechanism to transform BIM data to KG triples

354 3.3. Automatic BIM Model Auditing Based on KG

355 **3.3.1. Improved TransR model to obtain KG embeddings**

Based on the transformation mechanism described in Section 3.2, standard BIM-356 KG representations are generated from the standard BIM model. Then, auditing 357 mechanisms are developed to automatically determine the mistake elements in BIM models 358 based on the manipulation of the transformed BIM-KG representations. First, a knowledge 359 360 graph embedding model is utilized to train the embeddings for the entities and relations. Given a KG with a collection of triples $S = \{(h, r, t)\}$, where h is a head entity, t is a tail 361 362 entity, and r is the relation between them, knowledge graph embedding is a technique that converts the entities and relations into vectors (i.e., embeddings). By doing so, the 363 364 manipulation of KG entities and relations for downstream applications can be simplified to numerical computations while the inherent structure is preserved [52]. 365

There are many methods to obtain knowledge graph embeddings, among which 366 TransE and its variants are simple yet effective with good performance [53,54]. TransE 367 [55] is a pioneering and representative model for obtaining knowledge graph embeddings. 368 369 As shown in Fig 8, TransE iteratively optimize embeddings of entities and relations in the KG triples. More specifically, embeddings of entities and relations in the KG triples 370 (positive triples) are first initialized randomly. Then, entities and relations in the positive 371 triples are shuffled to get negative triples (i.e., triples that are unobserved in the KG). The 372 373 assumption in TransE is that the sum of embeddings of the head entity and relation (i.e., $\vec{h} + \vec{r}$) should be close to the embedding of the tail entity (\vec{t}) if the triple is positive, as 374 shown in Fig 9. Thus, a Euclidean distance-based score function is utilized to score the 375 positive and negative triples, as defined in Eq. (1), where $\vec{h}, \vec{r}, \vec{t}$ are the embeddings of the 376 head entity, relation, and tail entity, respectively, and f(h,r,t) is the score of the triple 377 378 (h, r, t). The embeddings are then updated to maximize and minimize the scores of positive and negative triples, respectively. After updating in iterations, the learned embeddings 379 make $\vec{h} + \vec{r} \approx \vec{t}$ (i.e., the assumption) hold for every (h, r, t). Details of TransE can be 380 found in [55]. 381

$$f(h, r, t) = -\left\|\vec{h} + \vec{r} - \vec{t}\right\|_{L_1/L_2}$$
(1)



Fig 9. Illustration of the TransE assumption (i.e., the sum of embeddings of the head entity and relation, $\vec{h} + \vec{r}$, should be close to the embedding of the tail entity, \vec{t} , if the triple is positive)

However, TransE suffers from complex relations such as 1-to-N, N-to-1, and N-to-N [53,56]. To address these limitations, TransR [53] is proposed, where the entities are embedded in the same vector space while different relations are represented in different relation spaces, and projection matrixes for different relations are introduced to project the entity embeddings into the relation-specific spaces, as follows:

$$\overrightarrow{h_{\perp}} = M_r \vec{h} \tag{2}$$

$$\vec{t_{\perp}} = M_r \vec{t} \tag{3}$$

$$f(h,r,t) = -\left\|\overrightarrow{h_{\perp}} + \overrightarrow{r} - \overrightarrow{t_{\perp}}\right\|_{L_1/L_2}$$
(4)

in which M_r refers to the projection matrix of relation r, $\vec{h_{\perp}}$ and $\vec{t_{\perp}}$ stand for the head and tail entity embeddings respectively that are projected from the entity space into the space of relation *r*. Consequently, the scoring function is formulated in Eq. (4). Other parts (e.g.,
embedding initialization, negative triple sampling, embedding updating with respect to
triple scores) are similar to TransE (Fig 8, Fig 9). Details of TransR can be found in [53].

399 TransR regards different projection matrixes as dense ones with the same dimension. However, such assumption ignores the imbalance of relations, which means the 400 numbers of triples/entities connected by different relations are different. For example, in 401 the BIM-KG data model for the QTO-oriented BIM model auditing (shown in Fig 6), the 402 403 relation *contact_with* connects at least three times as many triples/entities as *has_type* does. Considering the projection matrixes for different relations in the same way cannot 404 distinguish them. To address this limitation, dynamic sparse matrixes are proposed instead 405 of static dense ones for the projection operation in the original TransR so as to overcome 406 407 the relation imbalance issue, as follows:

$$\delta_r = 1 - n_r / n_{max} \tag{5}$$

$$\overrightarrow{h_{\perp}} = M_{\delta_r} \overrightarrow{h} \tag{6}$$

$$\vec{t_{\perp}} = M_{\delta r} \vec{t} \tag{7}$$

where a sparse factor δ_r is introduced to dynamically adjust the sparsity of the projection matrixes for different relations, n_r is the number of triples connected by relation r and n_{max} is the maximum value, δ_r indicates how many elements in the projection matrix are 0 values. Correspondingly, M_{δ_r} is the dynamic sparse projection matrix of relation r, where a ratio of δ_r elements in the matrix are set to 0 randomly. The scoring function is defined as the same as that in TransR, as shown in Eq. (4).

Through the training of this improved TransR model, embeddings of the entities and relations in the standard BIM-KG from the standard BIM model are obtained. The embeddings are then utilized in subsequent steps to determine mistake elements. The standard BIM model/standard BIM-KG is the single source of truth, based on which wrong patterns in different BIM models are identified using the embeddings. Details are provided in the following sections 3.3.2 and 3.3.3.

420

421 3.3.2. Contextual comparison to obtain embeddings of new BIM-KG entities

Following the transformation mechanism described in Section 3.2, new BIM-KG entities are generated from the new BIM model to be audited. Note that the embeddings

are trained over the standard BIM-KG. In other words, only the entities and relations in the 424 425 standard BIM-KG have corresponding embeddings. For example, an entity *slab_234* in the 426 standard BIM-KG has an embedding of [-0.201,0. 089,...,0.105]. However, the new BIM-427 KG entities may not appear in the standard BIM-KG, which causes problems in the auditing. For instance, a new entity *slab_567* does not exist in the standard BIM-KG and thus has 428 429 no corresponding embedding. Consequently, it cannot be scored (i.e., take the embeddings of entities and relations in a BIM-KG triple into a predefined score function such as Eq. (4) 430 431 to calculate a triple score) and compared with a threshold to decide whether it should be rejected or accepted according to the auditing procedure in Fig 4. To tackle this problem 432 that new unseen entities from new BIM models may not have embeddings, a contextual 433 434 comparison mechanism is developed as follows.

435 Proxy entities are selected for the new unseen entities from the new BIM model to be audited. For a new unseen entity, a proxy entity is an entity with high semantic 436 437 similarities in the standard BIM-KG where each entity has an embedding trained by the improved TransR. The embedding of the proxy entity then serves as the embedding of the 438 439 new unseen one for scoring the new triple in subsequent steps. The semantic similarities 440 between the proxy entity and the new unseen entity are different for different kinds of 441 entities. For new element entities (e.g., slab_567), the proxies should share similar 442 semantic properties and spatial positions. For new attribute entities, the proxies should 443 belong to similar elements. For example, the proxy for the new entity *slope* in a new triple 444 *<beam_123, has_type, slope>* should be one of the beam types such as *horizontal* rather than *vertical* which is a column type. To achieve this, a mechanism based on contextual 445 information comparison is developed to obtain appropriate proxy entities. As shown in Fig 446 447 10, if the unseen new entity is an element entity (e.g., *slab_567*), the entities from the 448 standard BIM-KG that share the same relation, category, and level act as candidate proxy entities. Otherwise, if it is an attribute entity (e.g., *slope*), the candidate proxy entities are 449 450 those with the same relation from the standard BIM-KG. Following this, one-hop neighbors (i.e., the directly connected entities in the KG) of the obtained candidate proxy entities are 451 452 compared with those of the new entity respectively to derive common neighbor information 453 (e.g., category, property) between this new entity and each of its candidate proxies. Based on such neighbor information, the candidate proxy entity with the most similar common 454

- 455 neighbors is selected as the proxy entity. Finally, the embedding of the proxy entity serves
- as that of the new entity for the subsequent scoring process.



Fig 10. Mechanism to obtain embeddings of new BIM-KG entities

459 **3.3.3. Self-evolving mechanism to determine a proper threshold**

Once the embeddings of the unseen entities from the new BIM model to be audited 460 are obtained, the scores of relevant triples can be calculated and compared with the 461 threshold to determine the auditing results (i.e., whether the involved elements in the triples 462 should be accepted or rejected). For example, the score of a new BIM-KG triple 463

 464 obtained embeddings and then compared with a threshold to decide whether slab_234 465 should be rejected or accepted. However, the threshold the scores need to be compared 466 with is unknown. To obtain a proper threshold automatically, a self-evolving mechanism 467 is proposed. It is a process of updating the threshold from a randomly initialized one to a 468 proper one according to the auditing results in iterations over a set of BIM models without 469 human intervention. 470

As shown in Fig 13, a set of new BIM models to be audited with different mistakes 471 472 about semantic information and modeling style is used to develop the threshold iteratively. In each epoch (i.e., a complete pass through the entire set of new BIM models), a set of 473 474 triples from new BIM models are scored using the scoring function shown in Eq. (4). A triple is accepted if its score is greater than the current threshold, meaning that the involving 475 476 elements in this triple are classified as correct (i.e., the element is modeled in accordance 477 with the specification). Otherwise, the elements are deemed as mistakes and rejected for 478 modifications. Based on the classification results, the confusion matrix shown in Fig 11 is derived. 479

		True Class							
		Positive	Negative						
d Class	Positive	True Positive (TP)	False Positive (FP)						
Predicte	Negative	False Negative (FN)	True Negative (TN)						

Fig 11. Confusion matrix

Then, the sensitivity that measures how many truly mistake elements are classified as mistakes and the specificity that measures how many truly correct elements are classified as correct are calculated according to Eqs. (8) - (9). Subsequently, the threshold is iteratively updated with respect to Eq. (10), as follows:

$$Sensitivity = TP/(TP + FN)$$
(8)

$$Specificity = TN/(TN + FP)$$
(9)

$$\theta = \theta_0 + \lambda (f(h, r, t)_{max} - f(h, r, t)_{min}) - \gamma (f(h, r, t)_{max} - f(h, r, t)_{min})$$
(10)

$$\lambda = \lambda + \lambda_0 (1 - sensitivity) \tag{11}$$

$$\gamma = \gamma + \gamma_0 (1 - specificity) \tag{12}$$

where θ is the learned threshold and θ_0 is the initial one, λ is the introduced adjusting factor to increase the threshold to filter mistake elements as much as possible, γ is the introduced penalty factor to decrease the threshold to avoid reporting correct elements as mistake ones, and $f(h, r, t)_{max}$ and $f(h, r, t)_{min}$ are the maximum and minimum scores of the triples from the standard BIM model, respectively. λ and γ are also obtained iteratively and dynamically according to Eqs. (11) – (12), where λ_0 and γ_0 are the initial values, respectively.

Finally, if the average sensitivity and specificity over the BIM models in the development set meet certain criterions, the average threshold is regarded as the final one. Otherwise, another epoch is conducted to further optimize the threshold until the performance criterions (i.e., sensitivity and specificity) are satisfied or the number of epochs reaches the limit. In this mechanism, the criteria for sensitivity (i.e., 0.95) is stricter than that for specificity (i.e., 0.9) because it is more important to find as many mistake elements as possible for model auditing problems.

500 Through this self-evolving mechanism, a threshold to filter out mistake elements is 501 obtained automatically. For the new BIM model to be audited, corresponding new BIM-KG triples are generated according to the transformation mechanism provided in Section 502 503 3.2 and their embeddings are obtained through the contextual comparison described in Section 3.3.2. Then, the Euclidean distance-based score function shown in Eq. (1) takes 504 505 the embeddings of the new BIM-KG triples to calculate their scores. As described in Section 3.3.1, given that the embeddings will favor high scores for positive triples (i.e., 506 BIM-KG triples with correct elements) and low scores for negative triples (i.e., BIM-KG 507

triples with mistake elements), the scores are compared with the obtained threshold to 508 decide the auditing results. More specifically, if the score of a new BIM-KG triple is lower 509 510 than the threshold, the element involved in the triple is deemed as a mistake element and thus is rejected. Otherwise, the element is regarded as a correct one and is accepted. Fig 12 511 shows an example of how the BIM-KG embeddings help to identify mistake elements with 512 the threshold as the criterion. Three embeddings $\overline{slab}_{side}(\vec{h}), \overline{contact}_{with}(\vec{r}),$ and 513 $\overline{beam \ 350477}$ (\vec{t}) are obtained for the triple $\langle slab_side, contact_with, beam_350477 \rangle$. 514 The score function takes the embeddings to calculate a score for the triple. In this example, 515 516 *beam_350477* is a mistake element modeled inappropriately according to the BIM OIR for QTO [31] (i.e., it wrongly takes the precedence over slabs). As shown in Fig 12, the triple 517 score is lower than the threshold. Given that BIM-KG triples with mistake patterns are 518 519 supposed to obtain low scores (i.e., lower than the threshold), the element, beam_350477, 520 in the triple is deemed as a mistake one and is rejected for further modifications.



Fig 12. Examples of scoring BIM-KG triples with the threshold as the criterion to
 identify mistake elements





Fig 13. Mechanism to determine a proper threshold

526 4. ILLUSTRATIVE EXAMPLES

527	The proposed framework has been validated through identifying different kinds of
528	mistake elements about semantic information and modeling style based on real BIM
529	projects. The BIM models presented in this paper were developed based on real-world BIM
530	projects with similar characteristics accordingly, for illustration. The BIM models are
531	created by Autodesk Revit 2021 [57]. Dynamo 2.10 [58] is utilized to develop the prototype
532	program for the mechanism in Section 3.2 in order to perform the transformation from BIM
533	data into BIM-KG triples. The BIM-KG entities and relations are stored in a graph database,
534	namely Neo4j Community Edition 4.3.2 [59]. The improved TransR model in Section 3.3.1
535	is implemented with Python 3.7.10 and PyKEEN 1.5.1.dev0 [60]. Other BIM modeling
536	auditing mechanisms described in Section 3.3.2 and 3.3.3 are also built with Python 3.7.10.
537	Py2neo 2021.1.5 [61] is used to conduct the interaction (e.g., retrieval of one-hop neighbors)
538	between the Neo4j database and the Python scripts for the auditing mechanisms.
539	
540	4.1. Configuration of BIM Models
541	Fig 14 shows 13 BIM models prepared using Autodesk Revit 2021 for illustration
542	purposes. Model A (Fig 14 (a)) is the standard BIM model in accordance with the BIM
543	MIR for QTO [31], meaning that it is created according to the following requirements:
544	(1) Sufficient semantic information
545	• The model contains all the necessary semantic attributes such as type and
546	concrete grade for QTO.
547	(2) Consistent modeling style
548	• Vertical elements (i.e., columns and walls) take precedence over horizontal
549	elements (i.e., slabs and beams).
550	Slabs take precedence over beams.
551	Models $B - M$ are regarded as the new BIM models to be audited. As shown in Fig
552	14 (b) $-$ (m), they cover common types of building structures (i.e., frame structure, shear
553	wall structure, shear wall-frame structure) and different mistakes (i.e., insufficient semantic
554	information, different inconsistent precedencies between elements). Models B – I are used
555	for the development of a proper threshold, while models $\mathbf{J}-\mathbf{M}$ are for the testing purpose.
556	Table 2 shows the quantities that are taken off from the illustrative BIM models with

- 557 different mistakes. They deviate from the baselines (i.e., correct quantities calculated
- according to the measurement rules). Besides, they are inconsistent and thus are difficult
- to apply uniform adjustments to correct them. This indicates that it is significant to audit
- the BIM models to ensure they are prepared consistently according to the requirements so
- that the quantities can be taken off correctly.



(d) Frame structure type – beams and slabs on the second floor have wrong modeling style

information



(g) Shear wall-frame structure type – slabs and columns on the second floor have wrong modeling style



(f) Shear wall-frame structure type – beams and slabs on the second floor have wrong modeling style



(h) Shear wall structure type – walls on the second floor lack concrete grade information



n the first floor lack (1) Frame structure type (for testing) – Beams and slabs on the first floor have wrong modeling style

concrete grade information



(m) Shear wall-frame structure type (for testing) – Slabs and walls on the second floor have wrong modeling style

- Fig 14. Configurations of BIM models for the illustration: (a) Model A; (b) Model B; (c) Model C; (d) Model D; (e) Model E; (f) Model F; (g)
 Model G; (h) Model H; (i) Model I; (j) Model J; (k) Model K; (l) Model L; (m) Model M

			Frame structure					Shear-wall frame structure				Shear wall structure				
		Model B	Model C	Model D	Model J	Model K	Model L	Model E	Model F	Model G	Model M	Model H	Model I			
Clab	Take-off quantities (m ³)	*	70.36	64.55	70.65	*	64.55	_*	65.70	70.58	71.17	_*	71.22			
5140	Baseline quantities (m ³)			70.	.36				70).36		68.74				
Doom	Take-off quantities (m ³)	-*	11.62	17.42	11.62	-*	17.42	9.31	13.97	9.31	9.31					
Dealli	Baseline quantities (m ³)	11.62					9.31			NA						
Column	Take-off quantities (m ³)	8.06	8.06	8.06	7.77	8.06	8.06	-	6.05	5.83	6.05	IN.	A			
Column	Baseline quantities (m ³)	8.06							6	.05						
Wall	Take-off quantities (m ³)			N				23.30	23.30	23.30	22.47	*	66.73			
vv all	Baseline quantities (m ³)	NA						23	3.30		69.	20				

Table 2. Quantities of concrete elements in the illustrative BIM models

 quantities (m³)

 571

 Note: assume all the elements have the same concrete grade when calculating the quantities for the models

572 **: Cannot take off quantities due to the lack of necessary semantic information (e.g., concrete grade)*

573 4.2. Automatic Transformation to KG Representations

A program was developed to examine the BIM-KG transformation mechanism in 574 Section 3.2 in Dynamo [61], which enables customized BIM data extraction and processing. 575 As shown in Fig 15, BIM-KG fact triples in the form of *<head*, *relation*, *tail>* are obtained 576 from the standard BIM model automatically. The entities and relations are then stored in 577 the Neo4j [64] database, which is a native and flexible graph data platform. Through this 578 process, BIM models can be automatically transformed into a set of fact triples whose 579 embeddings are trained for the computation of mistake elements. The stored KG 580 representations can be used for data (e.g., one-hop neighbors) retrieval in subsequent steps. 581

582



585

586 4.3. Automatic BIM Model Auditing Based on the KG Representations

587 4.3.1. Improved TransR model to obtain KG embeddings

- 588 The improved TransR model in Section 3.3.1 is utilized to train the standard BIM-
- 589 KG fact triples to obtain the embeddings of the entities and relations. Fig 16 presents
- 590 examples of the obtained embeddings.

head	relation	tail	head	relation	tail
<column_36803 <column_side, <beam_368103, <slab_368473,< th=""><th> has_concrete_grade, contact_with, has_surface, join_with, </th><th>C30>> slab_363626>> beam_top>> column_368315>></th><th><[0.088,0.098,,-0.037], <[-0.099,-0.020,,-0.075j <[0.219,0.189,,-0.209], <[-0.191,0.136,,0.003],</th><th>[-0.249,0.093,,-0.234], !, [0.160,0.191,,0.164], [-0.146,-0.187,,-0.165] [0.073,-0.010,,0.082],</th><th>[0.107,-0.171,,0.064]> [-0.183,0.157,,-0.045]>], [-0.105,-0.047,,0.251]> [-0.017,-0.358,,0.028]></th></slab_368473,<></beam_368103, </column_side, </column_36803 	 has_concrete_grade, contact_with, has_surface, join_with, 	C30>> slab_363626>> beam_top>> column_368315>>	<[0.088,0.098,,-0.037], <[-0.099,-0.020,,-0.075j <[0.219,0.189,,-0.209], <[-0.191,0.136,,0.003],	[-0.249,0.093,,-0.234], !, [0.160,0.191,,0.164], [-0.146,-0.187,,-0.165] [0.073,-0.010,,0.082],	[0.107,-0.171,,0.064]> [-0.183,0.157,,-0.045]>], [-0.105,-0.047,,0.251]> [-0.017,-0.358,,0.028]>
	 Standard BIM-KG fact	triples		 Trained embeddings	

591 592

Fig 16. Examples of trained embeddings

- 593 For evaluation of knowledge graph embeddings, a common practice is to perform
- the link prediction task and calculate two metrics, namely Mean Rank and Hits@10. For
- each fact triple (h, r, t) existing in the KG, h is replaced by every other entity h' in the

entity set. The scores (i.e., plausibility) of all the corrupted triples (h', r, t) as well as the 596 original correct one (h, r, t) is calculated using the embeddings and scoring function and 597 ranked in descending order. Such a ranking process is also applicable to the situation where 598 599 t is replaced. The average rank of the correct fact triples (h, r, t) is the Mean Rank. The proportion of the correct fact triples ranked in the top 10 over all the correct ones is the 600 Hits@10. Eqs. (13) – (14) show the calculations, where R is the set of ranks of all the 601 correct fact triples, r is a rank in R, |R| means the number of the ranks in R, and $|r \leq 10|$ 602 denotes the Boolean calculation (i.e., $[r \le 10]$ equals 0 if r is greater than 10, otherwise, 603 it is 1). A lower Mean Rank and higher Hits@10 indicate better quality of the obtained 604 605 embeddings.

Table 3 lists the evaluation metrics of the TransR and proposed modified TransR. The results show that the proposed modified TransR outperforms the baseline model, TransR, consistently, clearly indicating that it has better expressivity and can improve the quality of the trained embeddings.

$$Mean Rank = \frac{1}{|R|} \sum_{r \in R} r$$
(13)

$$Hits@10 = \frac{1}{|R|} \sum_{r \in R} [r \le 10]$$
(14)

Table 3. Comparison between the TransR and proposed modified TransR

Model	Mean Rank	Hits@10(%)
TransR	14	68.97
Proposed modified TransR	13	74.37

611

612 **4.3.2.** Contextual comparison to obtain embeddings of new BIM-KG entities

As mentioned in Section 3.3.1, it is necessary to find embeddings for the new entities from BIM models to be audited. In this section, we use Model B shown in Fig 14 (b) to illustrate the process of obtaining proper embeddings for new entities. Similar to Section 4.2, BIM-KG triples, including entities and relations, are obtained from Model B according to the mechanism in Section 3.2. Then, these new entities and relations are also stored in the Neo4j graph database. As described in Section 3.3.2 (Fig 10), candidate proxy entities are obtained first for each new entity. For instance, the new entity *column_350358*

(Fig 17) from the second floor in the triple *<slab side, contact with, column 350358>* 620 621 considers the column entities that are in the same level and in contact with other entities as 622 well (i.e., connected by the *contact_with* relation) as its candidate proxy entities. Fig 18 shows five examples. Following this, one-hop neighbors of these candidate proxy entities 623 and the new entity are retrieved from the BIM-KGs of Model B and the standard BIM 624 model, respectively. Then, they are compared to find the common one-hop neighbor 625 information, as illustrated in Fig 18. The common one-hop neighbor information indicates 626 627 the semantic similarities described in Section 3.3.2 between the candidate proxy entities and the new entity. For example, as shown in Fig 6 and Fig 18, such information on an 628 element entity reveals the common semantic properties (e.g., concrete grade such as C40, 629 type such as *vertical*) and common categories of joining and contacting elements nearby 630 631 that describe the spatial position (e.g., corner, edge, middle). Therefore, in Fig 18, the new entity column_350358 selects column_36065 or column_358067 as its proxy from the 632 candidates since they share the most common semantic properties (i.e., C40, vertical) and 633 spatial positions (i.e., edge) that are derived from the number of common categories of 634 635 joining and contacting elements. Through such a contextual comparison based on one-hop neighbor information between two BIM-KGs, the proxy entity that has the most semantic 636 637 similarity with the new one is derived from the standard BIM model. Its embedding is then used as the embedding of the new entity for calculating the scores of relevant triples. 638 639 Afterwards, the calculated scores are utilized to identify mistake elements in the next step.



Fig 17. A new entity in Model B and its one-hop neighbor information retrieved from the
 BIM-KG of Model B

Candidate proxy entity 1: column 368061

- One-hop neighbor information (common one-hop neighbors with the new entity are highlighted in bold): C30, vertical, slab, slab, beam, beam, wall, wall, column, column_bottom, column_bottom, column_top, column_top, column_side, slab_side, beam_side, wall side
- Number of common one-hop neighbors: 12

Candidate proxy entity 5: column 368069

 One-hop neighbor information (common one-hop neighbors with the new entity are highlighted in bold): C40, vertical, slab, slab, beam, beam, wall, wall, column, column_top, column_top, column_bottom, column_bottom, column_side, slab_side, beam_side, wall_side

Candidate proxy entity 4: column 368067

• Number of common one-hop neighbors: 19

beam side

One-hop neighbor information (common one-hop

neighbors with the new entity are highlighted in bold):

C40, vertical, slab, slab, slab, slab, beam, beam, beam,

beam, beam, beam, column, column top, column top,

column bottom, column bottom, column side, slab side,

Number of common one-hop neighbors: 13

Candidate proxy entity 2: column_368063

- One-hop neighbor information (common one-hop neighbors with the new entity are highlighted in bold): C30, vertical, slab, slab, slab, slab, slab, beam, beam, beam, beam, column, column_top, column_top, column_bottom, column_top, column_side, slab_side, beam_side
- Number of common one-hop neighbors: 18

643

Candidate proxy entity 3: column 368065

- One-hop neighbor information (common one-hop neighbors with the new entity are highlighted in bold): C40, vertical, slab, slab, slab, slab, slab, beam, beam, beam, beam, beam, column_top, column_top, column_bottom, column_top, column_side, slab_side, beam_side
- Number of common one-hop neighbors: 19
- Fig 18. Examples of one-hop neighbor comparison between the new entity in the new BIM model and its candidate proxy entities in the standard
 BIM model

646 **4.3.3. Self-evolving mechanism to determine a proper threshold**

647 Once the embeddings of the entities and relations from the new BIM models to be audited are obtained, the scores of relevant triples are calculated using the scoring function 648 in Eq. (1). They are then compared with a threshold to derive auditing results, as shown in 649 Fig 12. To facilitate such a scoring and comparing process, Models B – I are utilized to 650 learn a proper threshold iteratively according to the mechanism described in Section 3.3.3. 651 Note that the threshold is a constant learned from a set of BIM models (i.e., Models B - I) 652 653 with different mistakes about semantic information (i.e., absent or inappropriate semantic attributes) and modeling style (i.e., inconsistent topological arrangements between 654 elements). New different BIM models with similar mistakes on the two aspects are 655 656 compared with the constant threshold to determine mistake elements. Fig 19 presents the 657 self-evolving processes of the threshold as well as other parameters in Fig 13. Each epoch iterates all the models B – I with a gradually changing threshold to filter mistake elements. 658 659 At the beginning of the first epoch, the low initial threshold results in 0% sensitivity and 100% specificity, meaning that all the elements are classified as correct (i.e., the threshold 660 661 is too low so that no mistake elements are identified). Consequently, the adjusting factor is increased to raise the threshold, which gradually increases the sensitivity. Once the 662 663 threshold is so high that the specificity drops, the penalty factor is raised to lower the threshold so as to avoid the case where the correct elements are misclassified as mistake 664 665 ones. Finally, if the sensitivity and specificity reach the plateau and satisfy the criterions in 666 Fig 13, the adjusting and penalty factors are stabilized, leading to a converged threshold, which is -1.872. Then, the comparison between the triple score and the threshold shown in 667 Fig 12 can be undertaken to identify mistake elements. 668

669 Four unseen models J - M (Fig 14 (j) – (m)) with different kinds of mistake 670 elements are used to for evaluation. Similarly, BIM-KG triples are first obtained from these testing models. The embeddings for the new entities and relations are derived and then 671 672 utilized to compute triple scores, which are compared with the learned threshold (i.e., 1.872) to classify the mistake and correct elements. As shown in Table 4, all the mistake elements 673 in the four testing models are identified successfully with the reasons aligned with the 674 mistakes described in Fig 14 (j) - (m). Table 5 shows the performance metrics of the 675 classifications. 100% sensitivity is achieved in all the testing BIM models, indicating that 676

all the mistake elements are identified successfully. In addition, the proposed method consistently provides high specificities, meaning that only a few correct elements are erroneously recognized as mistake elements. This suggests that BIM modelers can be effectively informed of all the mistake elements that they are most concerned about. The few correct elements that are identified as mistake elements require little additional effort to be excluded during the model modification process.

After the mistake elements are identified with respect to the proper threshold, they are rejected. The BIM model is then sent back to the BIM modeler with the list of reject elements for them to edit until no element is identified as a mistake. As a result, it can be ensured that all the elements are modeled consistently according to the modelling requirements in the specification.









692

Table 4. Overall auditing results of the testing models

	Mistake elements	All are identified successfully?	Reason
Model J	9 slabs; 16 columns	Yes	9 slabs take precedence over 16 columns by mistake
Model K	24 beams	Yes	24 beams lack concrete grade information
Model L	9 slabs; 24 beams	Yes	24 beams take precedence over 9 slabs by mistake
Model M	9 slabs; 4 walls	Yes	9 slabs take precedence over 4 walls by mistake

693

694

Table 5. Performance metrics of the testing models

	Model J	Model K	Model L	Model M	Average
Sensitivity	100%	100%	100%	100%	100%
Specificity	100%	100%	88%	90%	94%

695

696 **5. CONCLUSIONS**

In this paper, the information requirements of BIM model auditing for QTO purposes are identified from QTO-oriented BIM modeling specifications in order to establish a BIM-KG data model to represent unstructured BIM data (including properties and interrelationships) explicitly, based on which BIM-KG triples are transformed from BIM models automatically. An improved knowledge graph embedding model is proposed

to translate the BIM-KG representations into computable embeddings. Then, auditing 702 703 mechanisms, including deriving embeddings for new BIM-KG entities and obtaining an 704 appropriate threshold iteratively, are developed to utilize these embeddings for automatic 705 mapping and inferences of auditing results without human intervention. The framework is applied to 13 BIM models for illustration. The results validate the effectiveness of the 706 707 approaches through automatically and successfully identifying mistake elements in BIM models with different kinds of errors regarding semantic information and modeling style. 708 709 In addition to the presented mistakes, the proposed framework is also applicable to other BIM modeling issues which originate from the absence of semantic information or 710 inappropriate topological arrangements between elements. For example, inconsistent 711 712 installation sequences of interior material elements in BIM models (e.g., a gypsum board 713 may be modeled after the floor heating system or the expanded polystyrene in a BIM model, which causes quantity deviations in the areas of the gypsum board) [14] can also be 714 715 detected since such issues may arise from inconsistent topological arrangements between elements. Overall, this study contributes to the following: 716

The proposed framework utilizes BIM models as training sources to obtain computable embeddings so that the underlying patterns among BIM data can be captured. Such a BIM-based data-driven manner enables automatic and efficient identification of mistake elements without human intervention. To the best knowledge of the authors, this is pioneering research in BIM-based data-driven model auditing for QTO that can greatly reduce the required human efforts on manual inspection or development of rule patterns.

724 This research brings insights on how to improve the efficiency of auditing BIM ٠ 725 models for QTO in a fundamental way, through BIM data representation (i.e., 726 the design of the BIM-KG representation and transformation mechanisms that can preserve both object properties and interrelationships explicitly) and 727 728 manipulation (i.e., the development of the BIM-KG utilization mechanisms 729 that manipulate the transformed BIM data to achieve the QTO-oriented model 730 auditing purposes). The basic principles are generalizable to future studies on 731 this problem and thus this research provides a reliable foundation.

- The modified TransR model provides better expressivity in terms of the
 imbalance of relations in BIM-KG representations, and outperforms the
 baseline model (i.e., TransR). The modified TransR can hence output better
 embeddings to support downstream manipulations such as the BIM-KG triple
 scoring.
- The proposed framework for BIM model auditing is generic and can be applied
 for not only QTO purposes but also other applications or projects where BIM
 models need to satisfy different but consistent requirements on semantic
 information and modeling style, e.g., standard modeling approaches
 incorporating structural design concepts [27].

742 However, there are certain limitations as follows. This study mainly focuses on typical building elements of concrete structures and the mistakes about semantic 743 information (i.e., absent or inappropriate semantic attributes) and modeling style (i.e., 744 745 inconsistent topological arrangements between elements) in BIM models. Besides, the framework is developed across different platforms and scripting languages, which may 746 747 make it difficult for domain engineers to grasp. Therefore, future works include: (1) considering more types of building elements and structures, as well as BIM modeling 748 749 mistakes, to make the framework more comprehensive; (2) developing a more user-750 friendly one-stop interface integrating different components in the framework to facilitate 751 the usage of it in domain engineers.

752

753

754 **REFERENCES**

- [1] Z. Shen, R.R.A. Issa, Quantitative evaluation of the BIM-assisted construction detailed
 cost estimates, Journal of Information Technology in Construction (ITcon). 15 (2010)
 pp. 234–257. https://doi.org/10/18.
- [2] S. Aram, C. Eastman, R. Sacks, A knowledge-based framework for quantity takeoff
 and cost estimation in the AEC industry using BIM, in: The 31st International
 Symposium on Automation and Robotics in Construction and Mining (ISARC),
 Sydney, Australia, 2014: pp. 434–442. https://doi.org/10.22260/ISARC2014/0058.

- [3] C. Khosakitchalert, N. Yabuki, T. Fukuda, Improving the accuracy of BIM-based quantity takeoff for compound elements, Automation in Construction. 106 (2019) pp. 102891. https://doi.org/10.1016/j.autcon.2019.102891.
- [4] L. Holm, J. E. Schaufelberger, D. Griffin, T. Cole, Construction cost estimating:
 process and practices, 1st Edition, Pearson, 978-0130496652, 2004.
- [5] R. Sacks, C. Eastman, G. Lee, P. Teicholz, BIM Handbook: A Guide to Building
 Information Modeling for Owners, Designers, Engineers, Contractors, and Facility
 Managers, John Wiley & Sons, 978-1-119-28753-7, 2018.
- [6] M. Juszczyk, R. Kozik, A. Leśniak, E. Plebankiewicz, K. Zima, Errors in the
 Preparation of Design Documentation in Public Procurement in Poland, Procedia
 Engineering. 85 (2014) pp. 283–292. https://doi.org/10.1016/j.proeng.2014.10.553.
- [7] A. Nadeem, A.K.D. Wong, F.K.W. Wong, Bill of Quantities with 3D Views Using
 Building Information Modeling, Arabian Journal for Science and Engineering. 40
 (2015) pp. 2465–2477. https://doi.org/10.1007/s13369-015-1657-2.
- [8] T. Akanbi, J. Zhang, Y.-C. Lee, Data-Driven Reverse Engineering Algorithm
 Development Method for Developing Interoperable Quantity Takeoff Algorithms
 Using IFC-Based BIM, Journal of Computing in Civil Engineering. 34 (2020) pp.
 04020036. https://doi.org/10.1061/(ASCE)CP.1943-5487.0000909.
- [9] A. Monteiro, J.P. Martins, A survey on modeling guidelines for quantity takeofforiented BIM-based design, Automation in Construction. 35 (2013) pp. 238–253.
 https://doi.org/10.1016/j.autcon.2013.05.005.
- [10] C.E. Firat, D. Arditi, J.-P. Hämäläinen, J. Stenstrand, J. Kiiras, Quantity take-off in
 model-based systems, in: Proceedings of the 27th CIB W78 International Conference,
 Cairo, Egypt, 2010: pp. 16–18. https://itc.scix.net/pdfs/w78-2010-112.pdf (accessed
 April 5, 2021).
- [11] K. Zima, Impact of information included in the BIM on preparation of Bill of
 Quantities, Procedia Engineering. 208 (2017) pp. 203–210.
 https://doi.org/10.1016/j.proeng.2017.11.039.
- [12] Hong Kong Institute of Surveyors, Hong Kong Standard Method of Measurement of
 Building Works, Fourth Edition, Pace Publishing Limited, 988-98402-4-3, 2005.

- [13] H. Liu, J.C.P. Cheng, V.J.L. Gan, S. Zhou, A knowledge model-based BIM framework
 for automatic code-compliant quantity take-off, Automation in Construction. 133
 (2022) pp. 104024. https://doi.org/10.1016/j.autcon.2021.104024.
- [14] S. Kim, S. Chin, S. Kwon, A Discrepancy Analysis of BIM-Based Quantity Take-Off
 for Building Interior Components, Journal of Management in Engineering. 35 (2019)
 pp. 05019001. https://doi.org/10.1061/(ASCE)ME.1943-5479.0000684.
- 798 [15] Construction Industry Council (CIC), CIC BIM Standards General (Version 2.1 -
- 2021), (2021). https://www.bim.cic.hk/zh-hant/resources/publications_detail/100
 (accessed December 30, 2021).
- [16] D. Olsen, J.M. Taylor, Quantity Take-Off Using Building Information Modeling
 (BIM), and Its Limiting Factors, Procedia Engineering. 196 (2017) pp. 1098–1105.
 https://doi.org/10.1016/j.proeng.2017.08.067.
- [17] G. Lee, R. Sacks, C.M. Eastman, Specifying parametric building object behavior
 (BOB) for a building information modeling system, Automation in Construction. 15
 (2006) pp. 758–776. https://doi.org/10.1016/j.autcon.2005.09.009.
- 807 [18] B. Succar, Building information modelling framework: A research and delivery
 808 foundation for industry stakeholders, Automation in Construction. 18 (2009) pp. 357–
 809 375. https://doi.org/10.1016/j.autcon.2008.10.003.
- [19] R. Sacks, M. Girolami, I. Brilakis, Building Information Modelling, Artificial
 Intelligence and Construction Tech, Developments in the Built Environment. (2020)
 pp. 100011. https://doi.org/10.1016/j.dibe.2020.100011..
- [20] A. Sheth, S. Padhee, A. Gyrard, Knowledge Graphs and Knowledge Networks: The
 Story in Brief, IEEE Internet Computing. 23 (2019) pp. 67–75.
 https://doi.org/10.1109/MIC.2019.2928449.
- 816 [21] A. Khalili, D.K.H. Chua, IFC-Based Graph Data Model for Topological Queries on
 817 Building Elements, Journal of Computing in Civil Engineering. 29 (2015) pp.
- 818 04014046. https://doi.org/10.1061/(ASCE)CP.1943-5487.0000331.
- [22] A. Ismail, A. Nahar, R. Scherer, Application of graph databases and graph theory
 concepts for advanced analysing of BIM models based on IFC standard, (2017).
 https://ifcwebserver.org/doc/ifc2gdb_eg-ice2017_ismail.pdf (accessed July 5, 2021).

[23] N. Skandhakumar, F. Salim, J. Reid, R. Drogemuller, E. Dawson, Graph theory based
representation of building information models for access control applications,
Automation in Construction. 68 (2016) pp. 44–51.
https://doi.org/10.1016/j.autcon.2016.04.001.

- [24] Y. Hu, D. Castro-Lacouture, C.M. Eastman, S.B. Navathe, Component Change List
 Prediction for BIM-Based Clash Resolution from a Graph Perspective, Journal of
 Construction Engineering and Management. 147 (2021) pp. 04021085.
 https://doi.org/10.1061/(ASCE)CO.1943-7862.0002092.
- [25] International Organization for Standardizatio (ISO), ISO 19650-1:2018 Organization 830 and digitization of information about buildings and civil engineering works, including 831 building information modelling (BIM) — Information management using building 832 833 information modelling ____ Part 1: Concepts and principles, 2018. https://www.iso.org/standard/68078.html (accessed June 20, 2021). 834
- [26] Ministry of Housing and Urban-Rural Development of the People's Republic of China,
 Standard for Graphic Expression of Building Information Modeling, (2018).
 http://download.mohurd.gov.cn/bzgg/hybz/JGJT%20448-
- 838 2018%20%E5%BB%BA%E7%AD%91%E5%B7%A5%E7%A8%8B%E8%AE%B

839 E%E8%AE%A1%E4%BF%A1%E6%81%AF%E6%A8%A1%E5%9E%8B%E5%8

- 840 8%B6%E5%9B%BE%E6%A0%87%E5%87%86.pdf (accessed July 3, 2021).
- 841 [27] Hong Kong Housing Authority, Standard Approach of Modelling (SAM) For Creating
- 842 Building Information Structural model for Development and Construction Division of
- 843 Hong Kong Housing Authority, (2014).

844 https://www.housingauthority.gov.hk/en/common/pdf/business-

partnerships/resources/building-information-modelling/modelling_guidelines.pdf

846 (accessed June 29, 2021).

[28] A. Kiviniemi, M. Rekola, K. Belloni, J. Kojima, T.K. ja T. Mäkeläinen, H. Kulusjärvi,

- J. Hietanen, Senate Properties: BIM Requirements 2007 Volume 7: Quantity take-off,(2007).
- https://web.archive.org/web/20120519151455/http://www.senaatti.fi/tiedostot/BIM_2
- 851 007_Vol_7_Quantity_take-off_R1_0.pdf (accessed June 30, 2021).

- [29] A. Kiviniemi, M. Rekola, K. Belloni, J. Kojima, T.K. ja T. Mäkeläinen, H. Kulusjärvi,
- 853J. Hietanen, Senate Properties: BIM Requirements 2007 Volume 3: Architectural854Design,(2007).
- https://web.archive.org/web/20120519151206/http://www.senaatti.fi/tiedostot/BIM_2
- 856 007_Vol3_Architectural_Design.pdf (accessed June 30, 2021).
- [30] National Institute of Building Sciences, National BIM Standard United States®
 Version 3, (2015). https://www.nationalbimstandard.org/nbims-us (accessed June 25, 2021).
- [31] The Hong Kong Institute of Surveyors, BIM Model Information Requirements forQuantity Take-off, Pre-publishing, (2021).
- 862 [32] Solibri, Solibri Model Checker, 2021. https://www.solibri.com/ (accessed June 30,
 863 2021).
- [33] Autodesk, Autodesk Model Checker for Revit, 2021.
- https://interoperability.autodesk.com/modelchecker.php (accessed June 29, 2021).
- [34] P.A. Zadeh, G. Wang, H.B. Cavka, S. Staub-French, R. Pottinger, Information Quality
 Assessment for Facility Management, Advanced Engineering Informatics. 33 (2017)
 pp. 181–205. https://doi.org/10.1016/j.aei.2017.06.003.
- [35] H.B. Cavka, S. Staub-French, E.A. Poirier, Levels of BIM compliance for model
 handover, Journal of Information Technology in Construction (ITcon). 23 (2018) pp.
 243–258. http://www.itcon.org/paper/2018/12.
- [36] E. Gholami, A. Kiviniemi, S. Sharples, Implementing Building Information Modelling
- (BIM) in Energy-Efficient Domestic Retrofit: Quality Checking of BIM Model, in:
 Eindhoven, The Netherlands, 2015: pp. 235–244. https://itc.scix.net/pdfs/w78-2015paper-024.pdf (accessed April 28, 2021).
- [37] V. Donato, M.L. Turco, M.M. Bocconcino, BIM-QA/QC in the architectural design
 process, Architectural Engineering and Design Management. 14 (2018) pp. 239–254.
- 878 https://doi.org/10.1080/17452007.2017.1370995.
- 879[38] S. Ji, S. Pan, E. Cambria, P. Marttinen, P.S. Yu, A Survey on Knowledge Graphs:880Representation, Acquisition, and Applications, IEEE Transactions on Neural Networks881andLearningSystems.(2021)pp.1–21.
- 882 https://doi.org/10.1109/TNNLS.2021.3070843.

- [39] F.N. Stokman, P.H. de Vries, Structuring Knowledge in a Graph, in: G.C. van der
 Veer, G. Mulder (Eds.), Human-Computer Interaction, Springer, Berlin, Heidelberg,
 1988: pp. 186–206. https://doi.org/10.1007/978-3-642-73402-1_12.
- [40] A. Bordes, J. Weston, R. Collobert, Y. Bengio, Learning structured embeddings of
 knowledge bases, in: Proceedings of the Twenty-Fifth AAAI Conference on Artificial
 Intelligence, AAAI Press, San Francisco, California, 2011: pp. 301–306.
 https://www.aaai.org/ocs/index.php/AAAI/AAAI11/paper/viewFile/3659/3898
- 890 (accessed July 10, 2021).
- [41] A. Nahar, Applying graph theory concepts for analyzing BIM models based on IFC
 standards, Master Thesis, Technische Universität Dresden, 2017. https://tu dresden.de/bu/bauingenieurwesen/cib/ressourcen/dateien/publikationen/Projekt-
- 2021).
 2021).
- [42] Z. Pan, C. Su, Y. Deng, J. Cheng, Video2Entities: A computer vision-based entity
 extraction framework for updating the architecture, engineering and construction
 industry knowledge graphs, Automation in Construction. 125 (2021) pp. 103617.
 https://doi.org/10.1016/j.autcon.2021.103617.
- [43] C. Wu, P. Wu, J. Wang, R. Jiang, M. Chen, X. Wang, Developing a hybrid approach
 to extract constraints related information for constraint management, Automation in
 Construction. 124 (2021) 103563. https://doi.org/10.1016/j.autcon.2021. pp. 103563.
- 903 [44] Z. Wang, R. Sacks, T. Yeung, Exploring graph neural networks for semantic
 904 enrichment: Room type classification, Automation in Construction. (2021) pp. 104039.
 905 https://doi.org/10.1016/j.autcon.2021.104039.
- [45] X.-Y. Wang, Y. Yang, K. Zhang, Customization and generation of floor plans based
 on graph transformations, Automation in Construction. 94 (2018) pp. 405–416.
 https://doi.org/10.1016/j.autcon.2018.07.017.
- [46] V.J.L. Gan, BIM-based graph data model for automatic generative design of modular
 buildings, Automation in Construction. 134 (2022) pp. 104062.
 https://doi.org/10.1016/j.autcon.2021.104062.

- 912 [47] B. Strug, E. Grabska, G. Ślusarczyk, Supporting the design process with hypergraph
 913 genetic operators, Advanced Engineering Informatics. 28 (2014) pp. 11–27.
 914 https://doi.org/10.1016/j.aei.2013.10.002.
- [48] P. Pauwels, T.M. de Farias, C. Zhang, A. Roxin, J. Beetz, J. De Roo, C. Nicolle, A
 performance benchmark over semantic rule checking approaches in construction
 industry, Advanced Engineering Informatics. 33 (2017) pp. 68–88.
 https://doi.org/10.1016/j.aei.2017.05.001.
- [49] B. Zhong, C. Gan, H. Luo, X. Xing, Ontology-based framework for building
 environmental monitoring and compliance checking under BIM environment, Building
 and Environment. 141 (2018) pp. 127–142.
 https://doi.org/10.1016/j.buildenv.2018.05.046.
- [50] L. Jiang, J. Shi, C. Wang, Multi-ontology fusion and rule development to facilitate
 automated code compliance checking using BIM and rule-based reasoning, Advanced
 Engineering Informatics. 51 (2022) pp. 101449.
 https://doi.org/10.1016/j.aei.2021.101449.
- 927 [51] buildingSMART, IFC4_ADD2_TC1 4.0.2.1 [Official], (2020).
- 928 https://standards.buildingsmart.org/IFC/RELEASE/IFC4/ADD2_TC1/HTML/
- 929 (accessed August 17, 2021).
- [52] Q. Wang, Z. Mao, B. Wang, L. Guo, Knowledge Graph Embedding: A Survey of
 Approaches and Applications, IEEE Transactions on Knowledge and Data Engineering.
 29 (2017) pp. 2724–2743. https://doi.org/10.1109/TKDE.2017.2754499.
- [53] Y. Lin, Z. Liu, M. Sun, Y. Liu, X. Zhu, Learning entity and relation embeddings for
 knowledge graph completion, in: Proceedings of the Twenty-Ninth AAAI Conference
 on Artificial Intelligence, AAAI Press, Austin, Texas, 2015: pp. 2181–2187.
- 936 [54] M. Ali, M. Berrendorf, C.T. Hoyt, L. Vermue, M. Galkin, S. Sharifzadeh, A. Fischer,
- 937 V. Tresp, J. Lehmann, Bringing Light Into the Dark: A Large-scale Evaluation of
- 938 Knowledge Graph Embedding Models Under a Unified Framework, IEEE
- 939 Transactions on Pattern Analysis and Machine Intelligence. PP (Accepted/In press).
- 940 https://doi.org/10.1109/TPAMI.2021.3124805.
- [55] A. Bordes, N. Usunier, A. Garcia-Durán, J. Weston, O. Yakhnenko, Translating
 embeddings for modeling multi-relational data, in: Proceedings of the 26th

- 943 International Conference on Neural Information Processing Systems Volume 2,
 944 Curran Associates Inc., Red Hook, NY, USA, 2013: pp. 2787–2795.
- 945 [56] Z. Wang, J. Zhang, J. Feng, Z. Chen, Knowledge Graph Embedding by Translating
 946 on Hyperplanes, in: Proceedings of the Twenty-Eighth AAAI Conference on Artificial
 947 Intelligence, Québec, Canada, 2014: pp. 1112–1119.
- https://ojs.aaai.org/index.php/AAAI/article/view/8870 (accessed September 25, 2021).
- 949 [57] Autodesk Revit 2021, Multidisciplinary BIM software for higher-quality, coordinated
- designs, 2021. https://www.autodesk.com.hk/products/revit/overview (accessed June
 10, 2021).
- 952 [58] Dynamo, Open source graphical programming for design, 2020.
- https://dynamobim.org/ (accessed January 10, 2021).
- [59] Neo4j, Neo4j: Graph Database Platform, 2021. https://neo4j.com/ (accessed June 29, 2021).
- [60] M. Ali, M. Berrendorf, C.T. Hoyt, L. Vermue, S. Sharifzadeh, V. Tresp, J. Lehmann,
 PyKEEN 1.0: A Python Library for Training and Evaluating Knowledge Graph
 Embeddings, Journal of Machine Learning Research. 22 (2021) pp. 1–6.
 http://jmlr.org/papers/v22/20-825.html.
- [61] Py2neo, The Py2neo Handbook, 2021. https://py2neo.org/2021.1/ (accessed July 16, 2021).