# Feature Reduction for Document Clustering and Classification

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#### Abstract

Often users receive search results which contain a wide range of documents, only some of which are relevant to their information needs. To address this problem, ever more systems not only locate information for users, but also organise that information on their behalf. We look at two main automatic approaches to information organisation: interactive clustering of search results and pre-categorising documents to provide hierarchical browsing structures. To be feasible in real world applications, both of these approaches require accurate yet efficient algorithms. Yet, both suffer from the curse of dimensionality — documents are typically represented by hundreds or thousands of words (features) which must be analysed and processed during clustering or classification. In this paper, we discuss feature reduction techniques and their application to document clustering and classification, showing that feature reduction improves efficiency as well as accuracy. We validate these algorithms using human relevance assignments and categorisation.

## **1** Introduction

Search Engines are a common gateway to huge document collections, be it the World Wide Web (WWW) or a collection of abstracts in an electronic book shop. It has been recognised that one limiting factor of search engine technology is the low precision of the results returned. It is not uncommon to get thousands or even millions of matches for a query such as "computer games". Even sophisticated ranking algorithms cannot know whether the user wants to browse documents on the latest advance in technology in this area or rather on entertaining products.

There are three basic approaches to this problem: 1) interactively clustering documents to allow users to preview a large collection more efficiently; 2) organising document collections into a set of categories to allow users to navigate in a structured way; 3) learning more about the user's interests and/or task to allow the system to better identify the relevant documents for this user and/or task.

For the first approach, we believe that cluster analysis of the documents returned by a query system provides a way to confront a user with different clusters/types of documents. Each cluster would either contain a high or a very low concentration of documents relevant to the user. This would allow users to quickly weed out whole clusters of irrelevant documents in accordance with the *cluster hypothesis* (van Rijsbergen 1979), which is commonly accepted for query results. For example (Hearst and Pedersen 1996) show that the cluster hypothesis holds for retrieval results using their efficient scatter/gather clustering. Complementary to this work, we formalise the clustering assessment procedure and argue that low-dimensional documents representations can avoid the curse of dimensionality (Section 3). This is done using a similarly efficient algorithm that clusters 1000s of documents within a second CPU time. A visual-navigation search engine based on this work and related visualisation techniques have been successfully implemented and are described elsewhere (Sewraz and Rüger 2000; Au, Carey, Sewraz, Guo and Rüger 2000).

As evidenced by the success of Yahoo and many other Internet index sites, browsing hierarchies (the second approach) are extremely popular methods to navigate the WWW. However, many of these indices are created manually, a time-consuming and expensive procedure. In Section 4 we will discuss the effectiveness of an automatic text categorisation algorithm and the effects of dimensionality reduction on its accuracy.

Finally, the system could learn about the user's interests and attempt to use this information to expand the query and/or post-process the search results. In addition to technical barriers, this approach requires users to allow their Web surfing behaviour to be monitored and that information to be shared with a search engine, which will be a social barrier for many users. As it is not directly related to dimensionality reduction, this approach will not be further discussed in this paper, but a discussion can be found in (Pretschner and Gauch 1999).

## 2 The Curse of Dimensionality and Feature Reduction

The natural features of text documents are words or phrases, and a document collection can contain millions of different features. Even after applying standard feature reduction techniques, the number of features remains large: in our clustering experiments with 528,155 US-American newspaper articles, we only kept nouns based on Brill's tagger (Brill 1994) with a medium document frequency: the noun had to appear in least three documents and in no more that 33% of all documents. Additionally, a list of stop-words was used to eliminate obvious function words of the language. This resulted in a vocabulary of around 280,000 so-called *potentially interesting words*. In our system we store a set of around 100 potentially interesting words are used by a query may still have a potentially-interesting-words vocabulary of 10,000s of different words. Consequently, the often-used word histogram representation of documents leads to high-dimensional vectors.

The problem with this kind of representations is that any two randomly picked vectors in a highdimensional hypercube tend to have a constant distance from each other, no matter what the measure is! As an example, let  $x, y \in [0, 1]^n$  be drawn independently from a uniform distribution. The expectation value of their sum-norm distance is n/3 with a standard deviation (ie, the square root of the variance) of  $\sqrt{n/18}$ :

$$\begin{split} \mathbf{E}(|x-y|_{1}) &= \mathbf{E}\left(\sum_{i=1}^{n}|x_{i}-y_{i}|\right) \\ &= n \, \mathbf{E}(|x_{1}-y_{1}|) & \text{linearity of } \mathbf{E} \\ &= n \int \int |x_{1}-y_{1}| \, \mathrm{d} \, x_{1} \, \mathrm{d} \, y_{1} \\ &= n/3 \end{split}$$
  
$$\begin{aligned} \mathrm{Var}(|x-y|_{1}) &= \mathrm{Var}\left(\sum_{i=1}^{n}|x_{i}-y_{i}|\right) \\ &= n \, \mathrm{Var}(|x_{1}-y_{1}|) \\ &= n(\mathbf{E}(|x_{1}-y_{1}|^{2}) - \mathbf{E}^{2}(|x_{1}-y_{1}|)) \\ &= n/18. \end{split}$$

For n = 1,800 (corresponding to a joint vocabulary of just 1,800 words for a word histogram representation) this means a typical distance of  $|x - y|_1 = 600 \pm 10$ . With increasing *n* the ratio between standard deviation and vector size gets ever smaller, as it scales with  $1/\sqrt{n}$ . This is a generic statistical property of high-dimensional spaces with any standard distance measure, provided the components of *x* are independent random variables, and can be traced down to the law of large numbers.

In post-retrieval document sets this phenomenon is somewhat alleviated through three properties: firstly, the restriction to a post-retrieval document set limits the vocabulary in a natural way; secondly, the dimensions carry different weights of relevance, usually tf-idf (where tf is the term frequency of a term within one document and idf is the inverse document frequency); thirdly, not all terms of the vocabulary are uncorrelated (the set of documents containing "Hewlett" is probably not much different from the set of documents containing "Packard"). The second property means that we have to consider only those dimensions with a high weight — these are predominantly given by terms with a low document frequency; according to Zipf's law (Narana and Balasubrahmanyan 1998) this is a constant (and with English documents more than 50%) proportion of the number of different words. The third property reduces the number of effective, independent dimensions through inherent co-occurrences in the documents.

Although real document collections have a lower number of effective dimensions than the size of the vocabulary might indicate and despite the fact that word histogram document representations are by no

means random vectors, each additional dimension tends to not only spread the size of a cluster but also dilute the distance of two previously well-separated clusters. Hence, it seems prohibitive involving all semantic features (e.g., the words) of a document collection for document clustering and classification.

## 3 Clustering

Document clustering has attracted much interest in the recent decades, eg (Salton 1968; Croft 1978; Voorhees 1985; Rasmussen 1992), and much is known about the importance of feature reduction in general, eg (Krishnaiah and Kanal 1982) and, in particular, clustering (van Rijsbergen 1979), but little has been done so far to facilitate feature reduction for document clustering of query results.

#### 3.1 Feature Reduction for Query Result Clustering

Let D be a set of documents and H the subset that is matched by a particular query. We suggest ranking the importance of each such word j with a weight

$$w_j = \frac{h_j}{d_j} \cdot h_j \log(|H|/h_j),$$

where  $h_j$  is the number of documents in H containing the word j, and  $d_j$  is the number of documents in the whole document collection D containing j. The second factor prefers medium matched-document frequency  $h_j$ , while the first factor prefers words that specifically occur in the matched documents. The highest-ranked words are meant to be related to the query. Indeed, we have "hardware", "software", "IBM" etc as the top-ranked words when querying for "computer". This seems to be a powerful approach to restrict the features of the matched documents to the top k ranked words, which we will call the *related words*. One important aspect is that the features are computed at query time. Hence, when the query "computer" is refined to "computer hardware", a completely new set of features would emerge automatically.

We represent each matched document i as a k-dimensional vector  $v_i$ , where the j-th component  $v_{ij}$  is a function of the number of occurrences  $t_{ij}$  of the j-th ranked related word in the document i:

$$v_{ij} = \log(1 + t_{ij}) \cdot \log(|D|/d_j)$$

This is a variation of the tf-idf weight that stresses the term frequency less. We project the vector  $v_i$  onto the k-dimensional unit sphere obtaining a normalised vector  $u_i$  that represents the document *i*. We deem the Euclidean distance between  $u_a$  and  $u_b$  a sensible *semantic distance* between two documents *a* and *b* in the document subset *H* returned by a query with respect to the complete document collection *D*. Note that the Euclidean distance is related to the cosine similarity measure owing to the process of normalisation.

#### 3.2 Clustering Algorithm

Post-retrieval document clustering has been well studied in the recent years, eg (Cutting, Karger, Pedersen and Tukey 1992; Allen, Obry and Littman 1993; Leouski and Croft 1996; Zamir and Etzioni 1998).

We deploy a variant of the Buckshot algorithm (Cutting, Karger, Pedersen and Tukey 1992), a two-phase process to cluster the document representations  $u_i$  in an Euclidean k-dim space. Each cluster contains a certain number of document vectors and is represented by their normalised arithmetic mean, the so-called centroid vector. In the first phase, hierarchical clustering with complete, single or average linkage operates on the best-ranked 150 documents (in contrast to the original Buckshot method, which would use a random document sample). This can be done in a fraction of one second CPU time. Hierarchical clustering has the advantage that one can either prescribe the number N of clusters or let the number of clusters determine by demanding a certain minimum similarity within a cluster. Either way, once clusters within the top-ranked documents are identified, their N centroids can be computed and used as a seed for standard iterative clustering of the remaining documents. This algorithm consumes an amount of time linear in the number |D| of documents and in the number N of clusters. In our experience, one cycle of iterative clustering is not only adequate but also preserves the cluster structure given by the top-ranked documents, which are thought to be the most important ones. 1,000s of documents can thus be clustered in less than a second on a standard 500 MHz PC.

#### 3.3 Validation

Any clustering method — even random assignment — leads to a partition of the documents. We propose a method to assess the quality of the clustering process based on human-expert data. We have used the 1997-1998 collection of the TREC data (Voorhees and Harman 1999) with 528,155 documents, mainly newspaper articles, 100 queries and corresponding relevance assessments. We ignored queries that contained fewer than 40 relevant documents and divided the remaining 61 queries randomly into test data (15) and training data (46). For each of the training queries we would run the query in a standard search engine and partition the set H of 1000 best-ranked documents into six clusters  $H_1, \ldots, H_6$  according to above scheme. A certain proportion  $p_*$  of the documents in H would be relevant documents in each cluster, respectively, were either 0 or 1 would be ideal. Contrary, a clustering where  $p_1 = \ldots = p_6 = p_*$ , could not assist a human user at all to quickly weed out big sets of irrelevant documents (see Figure 1).



Figure 1: The document collection after searching and clustering

We introduce a quality measure  $q_i \in [0, 1]$  for each cluster *i* such that  $q_i$  interpolates linearly between the cases  $q_i = 1$  for  $p_i = 0$ ,  $q_i = 0$  for  $p_i = p_*$  and  $q_i = 1$  for  $p_i = 1$  (see Figure 2). The weighted sum of these individual cluster qualities, weighted by the relative cluster size, gives rise to an overall quality measure

$$q = \sum_{i} q_i |H_i| / |H| \text{ with } q \in [0, 1].$$

Averaging over all available training queries gives insight into the typical behaviour of a clustering routine in the context of a particular search engine.

### 3.4 Experimental Results and Discussion

The experimental procedure was applied to queries with different dimensions for the document representation and three linkage methods each (single, average and complete) for the seeding of the iterative-clustering centres. For each of the combinations, we computed a cluster quality as described above and calculated the average  $\pm$  standard deviation and the 10% and 90% quantile of these qualities over the 46 training queries, see Table 1.

Our preliminary results indicate that complete linkage seems to outperform the other two linkage methods, especially in high dimensions. This table also indicates that low-dimensional representations outperform



Figure 2: The quality  $q_i$  of an individual cluster *i* 

the much more computationally intensive high-dimensional representations. Especially between 9 to 11 dimensions did we find a significant ( $\alpha = 0.05$ ) better clustering quality (using complete linkage) over a wide range of queries in contrast to high-dimensional representations which cost up to a factor of 25 more computing time. These findings have been confirmed on the test queries. As a byproduct, our studies confirmed that the average cluster quality is significantly higher than random cluster assignments, which supports the cluster hypothesis for retrieval results.

The big variation of the cluster qualities given by the large standard deviations indicate that for each query another number of features might be optimal given a particular document representation.

Similar studies have been carried out by (Schütze and Silverstein 1997); they found (to their surprise) that no loss of cluster quality is observed by latent semantic indexing (Dumais, Furnas, Landauer, Deerwester and Harshman 1988) or by using the maximum term frequency weights for dimensionality reduction. However, they did not observe a significant improvement at low-dimensional representations, either. One possible explanation, in our opinion, is that these representations aim to preserve the distances of the corresponding full document representations. Although latent semantic indexing has found many applications in information retrieval through implicit concept building based on co-occurrence statistics, it might be through the explicit effort to preserve document distances that prevents improved clustering performance in lower dimensions.

## 4 Classification

Browsing is another method to find information. Several search engines provide subject hierarchies that can be browsed, but the associated Web pages are manually placed in the categories, e.g., Infoseek's Ultraseek (Infoseek 1998) which limits the amount of information available. In contrast, we build a browsing structure automatically by categorising documents into concepts in a pre-defined ontology, or subject hierarchy. In one application, all the pages for a given Web site are categorised into concepts in a standard ontology to produce a site map for that site (Zhu, Gauch, Gerhard, Kral and Pretschner 1999). A site map represents the information space of a site by either relating a group of Web pages to a particular subject or depicting the links specified in the Web pages. To generate a subject-based site map, one must describe a subject space, which typically has a hierarchical structure, and then associate documents with the appropriate subjects. Other automatic approaches may employ neural networks (Lin 1995) document clustering (Cartia 1998) or the links among the Web pages (Maarek, Ben-Shaul, Jacovi, Shtalhaim, Ur and Zernik 1997)

Our classification approach uses a pre-existing ontology (in our case, a browsing hierarchy used by a prominent Web site) as a reference ontology. Each Web page from the local site to be characterised is automatically classified into the best matching concept in the reference ontology. The documents that have been manually attached to each concept in the reference ontology are used as training data for categorising the new documents. We use a vector space approach, calculating the cosine similarity measure to identify the closest match between a vector representing the Web page and the vectors representing the concepts in the reference ontology. All the training documents associated with a given concept are concatenated to form a superdocument. These superdocuments are then indexed using a vector space retrieval engine. Each

dim	complete linkage	average linkage single linkage	
2	$0.147 \pm 0.17 \; [0.01,  0.33]$	$0.147 \pm 0.17 \; [0.01,  0.33]$	$0.148 \pm 0.17 \ [0.01, \ 0.33]$
4	$0.235 \pm 0.20 \ [0.03, \ 0.51]$	$0.236 \pm 0.20 \ [0.03, \ 0.51]$	$0.236 \pm 0.20 \ [0.03, \ 0.51]$
6	$0.287 \pm 0.21 \ [0.06, \ 0.63]$	$0.278 \pm 0.21$ [0.06, 0.54]	$0.269 \pm 0.20 \ [0.05, \ 0.52]$
7	$0.317 \pm 0.22 \ [0.07, \ 0.66]$	$0.313 \pm 0.23 \ [0.06, \ 0.68]$	$0.287 \pm 0.21$ [0.06, 0.62]
8	$0.315 \pm 0.20 \ [0.06, \ 0.62]$	$0.320 \pm 0.22 \ [0.06, \ 0.66]$	$0.280 \pm 0.21$ [0.05, 0.61]
9	$0.354 \pm 0.21 \ [0.08, \ 0.67]$	$0.330 \pm 0.22 \ [0.03, \ 0.66]$	$0.290 \pm 0.22$ [0.04, 0.62]
10	$0.354 \pm 0.20 \ [0.15, \ 0.66]$	$0.320 \pm 0.21 \ [0.05, \ 0.65]$	$0.318 \pm 0.20 \ [0.08, \ 0.63]$
11	$0.352 \pm 0.19 \ [0.11, \ 0.66]$	$0.336 \pm 0.19 \ [0.10, \ 0.65]$	$0.311 \pm 0.20 \ [0.06, \ 0.63]$
12	$0.307 \pm 0.20 \ [0.06, \ 0.61]$	$0.298 \pm 0.21 \ [0.03, \ 0.64]$	$0.286 \pm 0.21 \ [0.05, \ 0.63]$
13	$0.336 \pm 0.20 \ [0.06, \ 0.60]$	$0.325 \pm 0.20 \ [0.07, \ 0.64]$	$0.306 \pm 0.20 \ [0.07, \ 0.57]$
14	$0.293 \pm 0.18 \ [0.06, \ 0.57]$	$0.310 \pm 0.20 \ [0.08, \ 0.66]$	$0.276 \pm 0.20 \ [0.05, \ 0.55]$
15	$0.290 \pm 0.17 \; [0.06,  0.57]$	$0.291 \pm 0.21 \ [0.05, \ 0.65]$	$0.301 \pm 0.19 \ [0.08, \ 0.56]$
16	$0.286 \pm 0.18 \ [0.07, \ 0.55]$	$0.311 \pm 0.20 \ [0.08, \ 0.60]$	$0.300 \pm 0.19 [0.07, 0.55]$
20	$0.270 \pm 0.20 \ [0.01, \ 0.56]$	$0.249 \pm 0.20 \ [0.01, \ 0.55]$	$0.267 \pm 0.20 \ [0.01, \ 0.54]$
24	$0.296 \pm 0.20 \ [0.03, \ 0.58]$	$0.299 \pm 0.22 \ [0.04, \ 0.58]$	$0.296 \pm 0.21 \ [0.04, \ 0.58]$
28	$0.266 \pm 0.19 \ [0.03, \ 0.57]$	$0.223 \pm 0.19 \ [0.02, \ 0.53]$	$0.277 \pm 0.21 \ [0.02, \ 0.58]$
32	$0.258 \pm 0.17 \; [0.04,  0.54]$	$0.217 \pm 0.19 \; [0.01,  0.49]$	$0.232 \pm 0.17 \ [0.01, \ 0.44]$
36	$0.279 \pm 0.18 \ [0.04, \ 0.55]$	$0.239 \pm 0.18 \ [0.01, \ 0.47]$	$0.243 \pm 0.19 \ [0.02, \ 0.53]$
64	$0.276 \pm 0.17 \ [0.05, \ 0.47]$	$0.202 \pm 0.17 \; [0.01,  0.42]$	$0.209 \pm 0.18 \ [0.02, \ 0.48]$
96	$0.239 \pm 0.16 \ [0.03, \ 0.48]$	$0.219 \pm 0.18 \ [0.02, \ 0.50]$	$0.131 \pm 0.14 \ [0.01, \ 0.32]$
128	$0.264 \pm 0.18 \ [0.02, \ 0.50]$	$0.182 \pm 0.16 \ [0.02, \ 0.38]$	$0.115 \pm 0.14 \ [0.01, \ 0.33]$
256	$0.276 \pm 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.06, \ 0.49 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \ 0.17 \$	$0.172 \pm 0.15 \ [0.02, \ 0.39]$	$0.090 \pm 0.11 \ [0.02, \ 0.27]$

Table 1: Clustering quality statistics for 46 queries each (avg  $\pm$  stddev [10%, 90%] quantile)

Web page to be categorised is then treated as a query and the retrieval engine returns the top matching superdocuments for that "query" (i.e., the top matching categories for that Web page). Each document is attached to only the top matching concept in the ontology. The weights of all the document matches to a particular concept are then accumulated to determine the weight of that concept in the site being studied.

To validate the quality of our categorisation, the next section discusses series of experiments that compare the performance of the vector space categorisation approach with one of the top classifiers, Naïve-Bayes (Friedman, Geiger and Goldszmidt 1997).

#### 4.1 Validation

We compared the performance of our approach with a Naïve-Bayes implementation from Carnegie-Mellon University (McCallum 1998), which has been found to be among the most effective classifiers (Friedman and Goldszmidt 1996). In the Naïve-Bayes approach (Langley, Iba and Thompson 1992), the conditional probability of each attribute value given a particular category is determined as well as the probability of the category appearing. This probabilistic information is typically established through a learning procedure, which takes in a new training instance each time and adjusts the probabilistic information of the corresponding category.

For the experiments, we selected an ontology containing 1,274 concepts and spidered 10 associated Web pages for each concept. We evaluated the accuracy of classifiers with a variable numbers of Web pages (one through eight per concept) in the training set, using the remaining two Web pages per concept as the test set.

#### 4.2 Experimental Results and Discussion

Table 2 shows the mean distance between the concept chosen by the classifiers and the concept with which the test document was originally associated. We defined the distance between two concepts as the length of the path between them. For example, the distance between a parent and its child in the ontology would be one and the distance between siblings would be two. Since the ontology had a maximum depth of 11, the maximum possible distance between the assigned and target concepts would be 22. Table 2 also shows

	Vector Space		Naïve Bayes	
training pages	mean dist	# of matches	mean dist	# of matches
1	6.07	127.0	7.07	32.0
2	5.69	202.5	6.87	61.0
3	5.11	289.0	6.61	95.5
4	4.69	355.0	6.43	127.0
5	4.42	407.5	6.29	149.0
6	4.27	434.5	6.11	184.0
7	4.32	423.5	6.09	188.0
8	4.39	415.0	5.96	184.0
Average	4.87	331.75	6.43	127.56

Table 2: Mean distance and number of matches per test page for the vector space and Naïve-Bayes approaches

the number of exact matches, where the classifier chose the same category with which the Web page was originally associated. The results in Table 2 are based on classifying two test documents per concept (ie, 2,548 test documents) when variable numbers of pages per concept were used for training. The statistical t-test analysis shows that the mean distance produced by the vector space approach is significantly smaller than that for the Naïve-Bayes approach (t-statistics = 5.56 > t(14) for p = 0.001). The number of matches for the vector space is also significantly larger than that for the Naïve-Bayes approach (t-statistics = 4.45 > t(14) for p = 0.001).

Examining Table 2 in more detail, we can see the effect of the amount of training data on the classification accuracy, which shows that, for the Vector Space method, the highest accuracy occurs with six training pages per concept. Adding more pages per concept degrades it slightly. Figure 3 illustrates the classifiers' performance in more detail, showing the histogram of distances when the number of training documents was six.



Figure 3: The histogram of distances between assigned concept and the correct concept (number of training pages - 6) for the vector space approach and the naïve-Bayes approach

In addition to varying the number of training pages, we also investigated the effect of using only a subset of words rather than the complete test documents as the input to the vector space classifier. The words were weighted using  $tf \cdot idf$  (where tf was the frequency of the term in the test document and idf was the inverse document frequency calculated over all available training documents) and we selected the top-weighted words. Figure 4 shows the results when we varied the number of words selected. The data show that the mean distance decreased as the number of selected words increased, but little improvement is seen

beyond 40 words selected. These results confirm the power of dimensionality reduction in two ways. First, our best result was found with only six training pages, adding more pages (and more words per concept) did not improve the classification. Similarly, representing pages to be classified by more than the 40 most important words (features) did not appreciably improve the classification.



Figure 4: Mean distance as a function of the number of top words in test documents

In summary, the data from the experiments show that the vector space approach was more accurate than the Naïve-Bayes approach, and that a modest number of training documents (approximately six per concept) are sufficient for good performance. The results also show that a small number of the most important words for a document convey enough information for classification. Overall, the site map generated by the our Local Classification Agent seems to be quite accurate for an entirely automatic approach.

## 5 Conclusions and Further Work

We have presented a method of assessing the quality of a document clustering procedure using human relevance assessments. We have demonstrated that this measure and the respective measure for the quality of a document classification procedure show the effects of the curse of dimensionality in accordance to a wellknown statistical effect. We used these data to reduce the number of features used to represent concepts (for classification) or documents in a collection subset (for clustering), respectively. Not only do the reduced feature representations reduce computing time but they also show a better discriminatory behaviour. Owing to the generic nature of the curse of dimensionality it has to be assumed that our feature reduction techniques are likely to improve the relevance and speed of any document clustering or classification algorithm which is based on feature vector representations.

Our work focused on finding a typical optimal number of features for clustering and classification purposes, yet it can be expected that individual document subsets or concepts each require a different number of features. It is left for further studies to fine-tune the average number of features (generated with the above methods) using properties of the particular concept or document set without reference to training data or human assessments.

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