It’s a gas: Oxidative dehydrogenation of propane over boron nitride catalysts

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\section*{Abstract}

Boron nitride and related boron-containing materials have recently been suggested as very promising catalysts in the oxidative dehydrogenation of propane. The high selectivity towards propylene at comparably high conversion significantly exceeds the performance of established vanadium-based catalysts. In the current work we show that the high selectivity towards propylene and ethylene is fully consistent with a gas-phase conversion mechanism and that it can be modelled reasonably well by the recent detailed microkinetic reaction mechanism of Hashemi and coworkers. Our analysis, using six heterogeneous catalytic reaction pathways, each representing a hypothetical limit case, shows that the boron nitride catalyst is responsible for initiating the gas-phase chemistry. The increased conversion of propane in cases with water co-feed, as well as the trends in the selectivities of minor species upon dilution of the catalytic bed and upon varying the $\text{C}_3\text{H}_8/\text{O}_2$ inlet ratio, as observed by Venegas and Hermans, are here explained as gas-phase phenomena. Hence, the oxidative dehydrogenation of propane over boron nitride catalysts is an example of a coupled gas- and catalytic-chemistry system. The current work also highlights the importance of modelling of the complete heated zone, including the rear heat shields and reactor padding if present.

\section{Introduction}

“It is surprising that boron nitride (BN), a material known for its high stability under oxidative conditions, is catalytically active at all.”\footnote{Since this landmark 2016 publication by Grant et al. in Science, boron-containing materials have become a hot topic in oxidative dehydrogenation (ODH), and with\* E-mail: peter.kraus@curtin.edu.au}
good reason. The claimed selectivity to propylene ($S(C_3H_6)$) is 80% at propane conversion ($X(C_3H_8)$) of 21%,\cite{2} while established vanadium-based catalysts offer only 60% selectivity at half the conversion.\cite{13} The performance of some BN materials remains stable up to 300 hours on stream\cite{2} and catalysts can be regenerated by co-feeding NH$_3$.\cite{2} In fact, it seems good ODH performance can be obtained with any material provided it contains boron.\cite{6,9}

Most studies of ODH of alkanes over BN focus on the catalytic surface chemistry, and despite the high temperatures required, usually in excess of 500°C, the potential contribution of gas-phase chemistry remains comparably unassessed. This is understandable as blank experiments with SiO$_2$ instead of BN in the reactor show almost no conversion.\cite{4,7} However, the operating conditions across the various catalytic tests have not been standardised,\cite{8} making comparisons between datasets difficult. Pretreatment, heat transport, diluent and dilution, reactor dimensions, and feed composition all play a significant role in the activity of hexagonal boron nitride (hBN).\cite{6,9} Venegas et al. proposed that the observed catalytic activity of diluted hBN for ODH of propane may be rooted in gas-phase oxidation chemistry, initiated by catalytic surface reactions, and that hBN may even act as a radical quenching agent.\cite{8} This was later reinforced by the suggestion that the role of the gas-phase must be established and incorporated in future model development.\cite{6} Such mechanisms have been proposed for ODH of butane\cite{10} and more recently propane.\cite{9}

It is a fortunate coincidence that a “low-temperature” (from a combustion point of view) gas phase mechanism for propane oxidation has been recently published.\cite{11} This allows us to investigate the relative gas-phase and catalytic contributions to the observed ODH of propane. We accordingly explore the differences between the predicted gas-phase behaviour and observed catalytic performance under dry conditions\cite{8} by coupling six catalytic “limit” mechanisms, derived from literature, to the gas-phase chemistry of Hashemi et al.\cite{11} We emphasise the heterogeneous mechanisms used in this work are not designed to represent the true surface chemistry of hBN. Rather, they are used as a probe to investigate the limits of the impacts of the heterogeneous chemistry on the overall ODH process. These mechanisms include direct dissociative adsorption as well as oxygen-mediated Eley-Rideal adsorption pathways, and investigate the potential impact of catalytically-generated propylene, propoxy radicals, propyl radicals, or C–C scission products on the gas-phase chemistry. The mechanisms are evaluated against the reference experimental conditions that span a range of residence times and consider the impact of dilution of the
catalyst in dry feed with the impact of steam and O₂ concentration in the feed thoroughly evaluated by Venegas et al.

2 Computational methods

The gas-phase and heterogeneous modelling in this work was performed using Cantera version 2.4. All fitting is performed with the nonlinear least squares routine curve_fit from the scipy.optimize Python library. The inputs used in the modelling, the resulting data, and the post-processing routines are all included in the Binder-compatible Supporting Information archive.

2.1 Gas-phase chemistry

The following gas-phase models are used in this work: i) the “DTU” model developed for high-pressure oxidation of propane, ii) the mechanism of Burluka et al. developed to model laminar burning velocities of C₃ oxygenated species, and iii) the “JetSurF” mechanism developed for high-temperature combustion of jet fuel surrogate mixtures. The DTU model includes low-temperature chemistry of the hydroperoxyalkyl (QOOH) radicals, as well as revised C₃H₈ thermal activation and radical abstraction rates. The Burluka model predates this low-temperature QOOH chemistry, but it includes more complete decomposition pathways of propylene oxide (c-C₃H₆O) which we show to be a potentially significant minor product. Finally, JetSurF is based on a C₁−C₄ submechanism that was extensively validated for higher temperatures and is mainly included for comparison purposes.

The ignition delay and selectivity-vs-conversion plots shown in Section 3 are modelled using an adiabatic constant pressure reactor, with the size of the time step adjusted dynamically by the solver. The ignition point τ is determined as the time corresponding to the maximum in the time derivative of the OH concentration (τ = arg max f(t) := d[OH]/dt). At the current temperatures, propane autoignition proceeds in two stages, with the first stage due to a combination of HO₂ and OH radical chemistry, and the second, high-temperature ignition stage characterised by OH chemistry. The τ determined using the above method corresponds to the latter, high-temperature ignition delay, and therefore corresponds to an upper boundary.
2.2 Catalytic surface chemistry

Table 1: The catalytic H/O sub-mechanism\[20\] in the form $AT^\beta e^{-E_A/RT}$, where $\theta(X)$ is surface fraction of species $X$, $s_0$ is the sticking coefficient, $s$ indicates a surface bond and $\dagger$ a first order rate law.

<table>
<thead>
<tr>
<th>#</th>
<th>Reaction</th>
<th>$A$ (m, mol, s)</th>
<th>$\beta$ (–)</th>
<th>$E_A$ (kJ/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>R1</td>
<td>$H_2 + 2^{\dagger}Bs \rightarrow 2 Hs$</td>
<td>$4.46 \times 10^4$</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>R2</td>
<td>$2 Hs \rightarrow H_2 + 2 Bs$</td>
<td>$3.7 \times 10^{15}$</td>
<td>0</td>
<td>67.4 - 6$\times$$\theta(Hs)$</td>
</tr>
<tr>
<td>R3</td>
<td>$H + Bs \rightarrow Hs$</td>
<td>$s_0 = 1$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R4</td>
<td>$O_2 + 2 Bs \rightarrow 2 Os$</td>
<td>$1.8 \times 10^9$</td>
<td>-0.5</td>
<td>0</td>
</tr>
<tr>
<td>R5</td>
<td>$O_2 + 2 Bs \rightarrow 2 Os$</td>
<td>$s_0 = 0.023$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R6</td>
<td>$2 Os \rightarrow O_2 + 2 Bs$</td>
<td>$3.7 \times 10^{15}$</td>
<td>0</td>
<td>213.2 - 60$\times$$\theta(Os)$</td>
</tr>
<tr>
<td>R7</td>
<td>$O + Bs \rightarrow Os$</td>
<td>$s_0 = 1$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R8</td>
<td>$H_2O + Bs \rightarrow H_2Os$</td>
<td>$s_0 = 0.75$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R9</td>
<td>$H_2Os \rightarrow H_2O + Bs$</td>
<td>$1 \times 10^{13}$</td>
<td>0</td>
<td>40.3</td>
</tr>
<tr>
<td>R10</td>
<td>$OH + Bs \rightarrow OHs$</td>
<td>$s_0 = 1$</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>R11</td>
<td>$OHs \rightarrow OH + Bs$</td>
<td>$1 \times 10^{13}$</td>
<td>0</td>
<td>192.8</td>
</tr>
<tr>
<td>R12</td>
<td>$Hs + Os \leftrightarrow OHs + Bs$</td>
<td>$3.7 \times 10^{15}$</td>
<td>0</td>
<td>11.5</td>
</tr>
<tr>
<td>R13</td>
<td>$Hs + OHs \leftrightarrow H_2Os + Bs$</td>
<td>$3.7 \times 10^{15}$</td>
<td>0</td>
<td>17.4</td>
</tr>
<tr>
<td>R14</td>
<td>$OHs + OHs \leftrightarrow H_2Os + Os$</td>
<td>$3.7 \times 10^{15}$</td>
<td>0</td>
<td>48.2</td>
</tr>
</tbody>
</table>

The heterogeneous models used in this work are based on the H/O sub-mechanism developed for CH$_4$ oxidation over platinum.\[20\] The model comprises 14 reactions and thermochemistry, shown in Table 1. We do not suggest that this H/O sub-mechanism developed for Pt is directly transferrable to hBN. For instance, there are large differences in the dominant mode of O$_2$ adsorption, as on transition metals the adsorption is dissociative,\[20\] while on boron-containing materials the associative adsorption plays an important role.\[7,21\] The contribution of the hBN surface and the nature of the active site remains a subject of intense study, with recent spectroscopic evidence of a significantly higher degree of surface oxidation\[22,23\] than previously thought. It has been proposed that the exceptional properties of boron-containing materials are due to this dynamic layer, formed in situ under ODH conditions, as it features active configurations that are not present in stable isomers.\[23\] However, in the absence of an existing validated H/O mechanism for hBN, our choice is one of convenience as the selected mechanism is distributed with Cantera, and it is computationally efficient due to its small size. The impact of the H/O sub-mechanism in the current work is also limited by ensuring the adsorption of propane is the rate limiting step, as discussed below. Most pre-exponential factors in the H/O model are order-of-magnitude estimates ($10^{13}$ s$^{-1}$ for desorptions and $3.7 \times 10^{15}$ m$^3$mol$^{-1}$s$^{-1}$ for bimolecular surface reactions). All original parameters are retained with the site density adjusted to reproduce the conversion.
observed with the current hBN based catalyst. The sensitivities to the site density (Γ) and oxygen adsorption parameters are accordingly assessed below. The thermochemistry of additional surface species is estimated from the corresponding gas-phase species in the DTU mechanism without further correction. In our previous work on Pt and Rh, the thermochemistry of the surface species was corrected by the heat of adsorption of the gas-phase species, obtained from systematic semi-empirical estimates. \[25\] Similar corrections for hBN would require values for the atomic heats of adsorption, which are currently unavailable and would have to be estimated. As a result, we introduced irreversible catalytic reaction steps (i.e. separate forward and reverse reactions) for the C₃/C₂/C₁ surface chemistry.

Table 2: Properties of materials used in the heterogeneous model, where κ is the thermal conductivity, \(\rho\) the density and \(S_A\) the surface area.

<table>
<thead>
<tr>
<th>Material</th>
<th>(\kappa) (W m(^{-1})K(^{-1}))</th>
<th>(\rho) (kg m(^{-3}))</th>
<th>(S_A) (m(^2)kg(^{-1}))</th>
</tr>
</thead>
<tbody>
<tr>
<td>SiO(_2)</td>
<td>3 [26]</td>
<td>100</td>
<td>1000</td>
</tr>
<tr>
<td>hBN</td>
<td>33 [8]</td>
<td>410 [8]</td>
<td>7000 [8]</td>
</tr>
<tr>
<td>SiC</td>
<td>300 [27]</td>
<td>860 [28]</td>
<td>13000 [28]</td>
</tr>
</tbody>
</table>

Figure 1: Schematic of the modelled reactor (not to scale). The catalytic section shown in red, front and rear heat shield sections filled with SiO\(_2\)-wool in white, and reactor padding SiO\(_2\) chips in gray.

The catalytic reactor is modelled using a plug flow approximation, with the modelled domain comprising four sections shown in Fig. 1: a SiO\(_2\)-wool heat shield, a catalytic section filled with hBN or optionally diluted with SiC, another SiO\(_2\)-wool heat shield, and the remainder of the reactor filled with SiO\(_2\) chips. The applied boundary conditions are taken from Venegas and Hermans where available: \[8\] an inlet temperature of 298 K; bath temperature of 773 K; reactor radius \(r\) of 4 mm; the tortuosity of the catalytic and SiO\(_2\)-wool sections set to 4; a porosity of the catalytic and SiO\(_2\)-wool sections of...
0.4; inlet flow rates between 40 and 160 ml min\(^{-1}\); length of the front and rear SiO\(_2\)-wool sections of 15 and 10 mm, respectively; length of the catalytic section between 3 and 25.5 mm depending on dilution of hBN with SiC; an overall reactor length of 200 mm. The inlet composition is 30% C\(_3\)H\(_8\), 15% O\(_2\), and 55% N\(_2\) by volume in all cases. The porosity and tortuosity of the section containing SiO\(_2\) chips is not provided; for simplicity we assume a tortuosity of 1 with the impact of porosity on conversion assessed below. The temperature of the modelled reactor is regulated by an isothermal bath coupled to the domain using a \(d = 4\) mm thick wall with material dependent properties listed in Table 2. The thermal conductances \(U_i\) for each reactor section \(i\) filled with material X are calculated according to Eq. (1), where \(V_i\) is the volume of the \(i\)th section.

\[
U_i = \kappa_i(X) \times d/(V_i S_{A_i}(X) \rho_i(X)) \quad (1)
\]

\[
A_{c_i} = V_i S_{A_i}(\text{hBN}) \rho_i(\text{hBN})/f_{\text{dil}} \quad (2)
\]

The gas-phase chemistry is evaluated in all parts of the reactor with the heterogeneous mechanism enabled only in the catalytic section. In cases where hBN is diluted by SiC, the catalytic area of each cell \(A_{c_i}\) is scaled by the dilution factor \(f_{\text{dil}} = V_{\text{bed}}/V_{\text{cat}} \in \{1.0, 1.5, 2.0, 3.5, 6.0, 8.5\}\) (see Eq. (2)), and the thermal conductance is approximated as the weighted sum of the conductivities of hBN and SiC. The density of grid points \(i\) in the four sections of the modelled reactor is 10/mm for the front and rear SiO\(_2\)-wool sections, 50/mm for the hBN-containing section, and 1/mm for the section filled with SiO\(_2\) chips. Grid resolution independence was confirmed using a 10× finer grid with the conversion converged to within 6% and selectivities to within 1% for the two grids. The carbon-based selectivities \(S\) and propane conversions \(X\) reported in this work are product based, using Eqs. (3) and (4), respectively.

\[
S(\text{prod}) = \frac{n_C(\text{prod}) x(i, \text{prod}) f_e(i)}{\sum_{p \neq \text{C}_3\text{H}_8} n_C(p) x(i, p) f_e(i)} \quad (3)
\]

\[
X(\text{C}_3\text{H}_8) = \frac{\sum_{p \neq \text{C}_3\text{H}_8} n_C(p) x(i, p) f_e(i)}{\sum_r n_C(r) x(i, r) f_e(i)} \quad (4)
\]

Here, \(n_C(p)\) is number of carbon atoms in species \(p\), \(x(i, p)\) is the mole fraction of \(p\) in cell \(i\), and \(f_e(i)\) is
the expansion factor defined as $f_e(i) = x(i, N_2)/x(0, N_2)$. Note that the index $p$ runs over the products only, while the index $r$ runs over all species.

3 Results and discussion

To provide background for the aspects of the catalytic chemistry in the studied system, we first investigate the behaviour of the gas-phase chemistry as predicted by the DTU,\textsuperscript{[11]} Burluka,\textsuperscript{[13]} and JetSurF\textsuperscript{[14]} reaction mechanisms under the experimental conditions. Then, we assess the impact of the surface chemistry of hBN on the selectivity of the overall system by using six hypothetical limiting heterogeneous reaction mechanisms. These limit mechanisms are used to probe the extremes of catalytic behaviour in the context of the gas-phase chemistry, by imposing 100% catalytic selectivity towards either propylene, propoxy radicals, propyl radicals, or C–C scission products. We then explore the contribution of the gas-phase chemistry within these limits of possible catalytic behaviours and the experimentally observed conversion and selectivities. Finally, we briefly discuss more recent experiments where the inlet composition was varied.

3.1 Gas-phase selectivities to major products

The temperatures used in most investigations of propane ODH over hBN are usually in excess of 500°C, which is higher than the usual conditions applied with vanadium-based catalysts.\textsuperscript{[3]} Such temperatures are potentially compatible with gas-phase ignition. Despite this, the contribution of gas-phase chemistry to the performance of hBN has not been quantified. Control experiments performed using a reactor filled only with quartz chips have been reported and show “negligible” conversion at well below 1%.\textsuperscript{[8]} While conceptual catalytic and combined homo- and heterogeneous mechanisms have been proposed,\textsuperscript{[1,7–10]} only two studies have assessed the gas-phase behaviour: i) Loiland et al. applied a gas-phase microkinetic model (AramcoMech2.0) to study gas-phase effects, however, the imposed boundary conditions (a 100 mm long modelled section) appear incongruous with the geometry of the experimental reactor (38 mm long diluted catalytic bed in a 610 mm long heated quartz reactor).\textsuperscript{[29]} ii) Venegas et al. performed a chemical kinetic analysis using a combined gas-phase and heterogeneous reaction mechanism, however, only selected gas-phase pathways were coupled to the surface chemistry instead of a comprehensive
The high temperature ignition delays shown in Fig. 2 present an indication that gas-phase phenomena may play a non-negligible role under the studied conditions. At 500°C, the DTU mechanism (---) shows an ignition delay just outside the residence time domain in the experiments of Venegas and Hermans (red zone); the other two mechanisms (Burluka (-----) and JetSurF (----)) predict ignition well within the experimental time domain. It should further be noted that the HO₂ radical chemistry will be active in the gas phase at lower temperatures. The experimental temperature of 500°C is determined from a single thermocouple embedded in the catalytic bed, and despite best practices ensuring the bed is as isothermal as practicable, small inhomogeneities from the reaction temperature would have an exponential effect on the kinetics this close to self-ignition. We note that the ignition delay times shown in Fig. 2 are obtained from adiabatic calculations, while the catalytic reactor is likely close to the isothermal limit. The temperature rise for the adiabatic computations is 3 K at 1% conversion and reaches an upper limit of 103 K at 20% conversion. The gas phase contribution is expected to be correspondingly higher than observed experimentally. Therefore, further results from gas-phase calculations are presented as a function of conversion. For combined heterogeneous and gas-phase calculations, we model the reactor using a plug-flow approximation coupled to a heat bath, validated in Section 3.3 below.

The performance of hBN (and other B-containing materials) for ODH of propane is remarkable mainly due to the high selectivity to propylene and ethylene. However, as shown in Figure 3, the high combustion mechanism.
selectivity to both propylene (C₃H₆, —) and ethylene (C₂H₄, —) is consistent with the kinetics of the DTU gas-phase mechanism. The experimental $S$(C₃H₆) at $X$(C₃H₈) ≤ 20% is matched almost exactly, while the trend in $S$(C₂H₄) is predicted qualitatively with a constant underprediction of ≈ 5% in the same conversion range. The other two mechanisms significantly underpredict the observed $S$(C₃H₆). For minor products, methane (CH₄, •) is well predicted by the DTU (—) and Burluka (⋯⋯) mechanisms, but the main combustion product CO (---) is much better captured by JetSurF. The results indicate strongly that the pyrolysis part of the DTU mechanism is accurate while experimental selectivity to CO indicates that further low temperature oxidation pathways may be required.

3.2 Gas-phase selectivities to minor products

All three mechanisms underpredict the experimental $S$(CO₂) by ≈ 1%. The best agreement is obtained by JetSurF (--- in Fig. 3), which predicts roughly half this value. The DTU mechanism also predicts propylene oxide (c–C₃H₆O) to be a significant minor product with $S$(c–C₃H₆O) around 8%. However, propylene oxide was neither observed experimentally [8], nor predicted by Burluka and JetSurf mechanisms. The DTU mechanism contains revised propylene oxide formation pathways passing via the QOOH route that are of particular relevance to the current temperature window [15]. However, the associated destruction pathways have to date not been formulated. The Burluka and JetSurF mechanisms rely upon a simpler formation step via C₃H₆ + HO₂ ↔ c–C₃H₆O + OH, but include c–C₃H₆O destruction pathways via ring opening towards acetone (CH₃C(O)CH₃) and propionaldehyde (CH₃CH₂CHO).
Propylene oxide is a liquid at room temperature and pressure, and the reactor effluent is cooled to -5°C to remove water prior to the chromatographic analysis. Hence, propylene oxide may be inadvertently removed from the effluent stream. However, the reported error in the experimental carbon mass balance is 3%, significantly less than the amount of propylene oxide predicted by the DTU mechanism. Inclusion of decomposition pathways of propylene oxide should ultimately lead to increased CO₂ and CO production, and improved agreement with experimental data as discussed below. It may further be noted that the catalyst may be active to propylene oxide as noted for copper-based catalysts by Xiao and Wang.

Table 3: The six heterogeneous “limit” submechanisms in the form \( A T^\beta e^{-E_A/RT} \). † indicates rate fitted to obtain \( X(C_3H_8) = 3.65\% \) with \( \Gamma = 1.6 \times 10^{-7} \text{ mol m}^{-2} \) and 20% porosity with undiluted catalyst at 40 ml min⁻¹ flow.

<table>
<thead>
<tr>
<th>#</th>
<th>Reaction</th>
<th>( A ) (m, mol, s)</th>
<th>( \beta ) (–)</th>
<th>( E_A ) (kJ/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>M1-R15</td>
<td>( C_3H_8 + 2 Bs \rightarrow C_3H_7s + Hs )</td>
<td>† 5.64 \times 10^{-4}</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>M1-R16</td>
<td>( C_3H_7s \rightarrow C_3H_6 + Hs )</td>
<td>1 \times 10^{13}</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>M2-R15</td>
<td>( C_3H_8 + 2 Os \rightarrow C_3H_7Os + OHs )</td>
<td>† 4.61 \times 10^{-7}</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>M2-R16</td>
<td>( C_3H_7Os \rightarrow C_3H_6 + OHs )</td>
<td>1 \times 10^{13}</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>M3-R15</td>
<td>( C_3H_8 + 2 Os \rightarrow C_3H_7Os + OHs )</td>
<td>† 2.79 \times 10^{-7}</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>M3-R16i</td>
<td>( C_3H_7Os \rightarrow i-C_3H_7O + Bs )</td>
<td>2 \times 10^{13}</td>
<td>0</td>
<td>20.9</td>
</tr>
<tr>
<td>M3-R16n</td>
<td>( C_3H_7Os \rightarrow n-C_3H_7O + Bs )</td>
<td>6 \times 10^{13}</td>
<td>0</td>
<td>3.4</td>
</tr>
<tr>
<td>M4-R15</td>
<td>( C_3H_8 + 2 Bs \rightarrow C_3H_7s + Hs )</td>
<td>† 3.81 \times 10^{-4}</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>M4-R16i</td>
<td>( C_3H_7s \rightarrow i-C_3H_7 + Bs )</td>
<td>2 \times 10^{13}</td>
<td>0</td>
<td>31.4</td>
</tr>
<tr>
<td>M4-R16n</td>
<td>( C_3H_7s \rightarrow n-C_3H_7 + Bs )</td>
<td>6 \times 10^{13}</td>
<td>0</td>
<td>20.9</td>
</tr>
<tr>
<td>M5-R15</td>
<td>( C_3H_8 + 2 Os \rightarrow C_3H_7Os + OHs )</td>
<td>† 2.65 \times 10^{-7}</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>M5-R16</td>
<td>( C_3H_7Os \rightarrow C_2H_4 + CH_3 + Os )</td>
<td>1 \times 10^{13}</td>
<td>0</td>
<td>0</td>
</tr>
<tr>
<td>M6-R15</td>
<td>( C_3H_8 + 2 Os \rightarrow C_3H_7Os + OHs )</td>
<td>† 4.74 \times 10^{-7}</td>
<td>0.5</td>
<td>0</td>
</tr>
<tr>
<td>M6-R16</td>
<td>( C_3H_7Os \rightarrow C_2H_4 + CO + Bs )</td>
<td>1 \times 10^{13}</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

### 3.3 Catalysis in the propylene forming limit (M1)

The six heterogeneous “limit” submechanisms are shown in Table 3. The first of these sequences (M1) is used to evaluate the impact of catalytic formation of propylene on the selectivities, as well as validate configuration related parameters such as the reactor porosity and the catalytic site density. The morphology of the catalyst may impose transport limitations and therefore impact the observed outcomes. The global impact of different morphologies will be reflected in the residence time, as the tortuosity and porosity of the bed will differ. In previous work, we imposed mass transport limitations via efficiency factors and the same approach could be applied here (e.g. based on Knudsen diffusion). However, this
would further emphasise the effects of the gas phase chemistry. We instead choose to use the plug-flow model and apply the literature values of porosity and tortuosity in the first three reactor sections (see Fig. 1). To validate our plug-flow reactor model, we determine the impact of porosity of the last section on the overall conversion due to residence time effects in the heated section. For this purpose, the DTU gas-phase mechanism is coupled to the catalytic chemistry shown in Table I and extended by sequence M1 as shown below.

\[
\begin{align*}
M1 - R15: & \quad C_3H_8 + 2 Bs \rightarrow C_3H_7s + Hs, \quad A = 5.64 \times 10^{-4} \text{ m}^3\text{mol}^{-1}\text{s}^{-1}, \quad \beta = 0.5, \quad E_A = 0 \\
M1 - R16: & \quad C_3H_7s \rightarrow C_3H_6 + Hs, \quad A = 1.0 \times 10^{13} \text{ s}^{-1}, \quad \beta = 0, \quad E_A = 0
\end{align*}
\]

The desorption in M1-R16 is unlikely to be barrierless. However, setting a barrier height has no effect if M1-R16 is not rate limiting as there is no alternative outlet for \( C_3H_7s \). Under such circumstances, the pre-exponential of M1-R15 can be fitted to match the observed conversion. The conversion reported in the control experiments without hBN is \( X(C_3H_8) = 1\% \) at 550°C and 0.3% at 500°C with the latter value indicated in Fig. 4 by the open circle (○). We note again that in the experiments, the temperature of the furnace is controlled by a single thermocouple embedded in the catalytic bed. This low level of conversion is only matched when the porosity of the rear section is around 1%, an unusually low value given that the porosity of the SiO\(_2\) wool is 40% and the porosity of SiO\(_2\) chips has been reported as high as 50%. In the following, we tentatively apply an intermediate value of porosity of 20%, corresponding to a conversion of 0.9% in the control experiment.

In addition to the porosity of the last section of the reactor and the adsorption rate constant M1-R15, \( X(C_3H_8) \) is also a function of the site density \( \Gamma \). The physical constraint on the site density of hBN is \( \Gamma \leq 3.04 \times 10^{-5} \text{ mol m}^{-2} \), derived from a theoretical unit cell area of 5.462 Å\(^2\) per boron site. The \( \Gamma \) used throughout the current work is fitted together with the pre-exponential of M1-R15 to ensure \( X(C_3H_8) = 3.65\% \) for the undiluted case, and 18.60% for \( V_{\text{bed}}/V_{\text{cat}} = 8.5 \), given a porosity of 20% in the last section of the reactor, shown in Fig. 4. The resulting values are \( A_{M1-R15} = 5.64 \times 10^{-4} \text{ m}^3\text{mol}^{-1}\text{s}^{-1} \) and \( \Gamma = 1.6 \times 10^{-7} \text{ mol m}^{-2} \) corresponding to 0.5% availability of boron sites with respect to the theoretical maximum.
Figure 4: Effect of porosity on the propane conversion and propylene selectivity, with the pre-exponential of R15-1 fitted to match conversion for undiluted case. Shading implies porosity in the range of 1–50%. Γ set to 1.6 × 10^{-7} mol m^{-2} for all dilutions and porosities. Flow rate \sim 40 ml min^{-1}.

The above two-step process is a limiting case. It is much more likely the actual propane activation process involves reversible C\textsubscript{3}H\textsubscript{8} adsorption followed by a C–H bond activation on the surface with an appreciable barrier. The dissociative adsorption described by M1-R15 can accordingly be thought of as a global reaction step with an exceptionally low sticking coefficient (s\textsubscript{0} ~ 10^{-12}) when compared to s\textsubscript{0} = 5.8 \times 10^{-3} for C\textsubscript{3}H\textsubscript{8} on rhodium.\cite{34} To obtain the same rate constant at 500°C, assuming the same propane sticking coefficient as on rhodium, the dissociative adsorption would have to proceed with a barrier of 117 kJ/mol. The barrier appears high, but is well below the reported experimental apparent activation energies for ODH of propane (184–233 kJ/mol\cite{2,29}). For comparison, on vanadium oxides, dissociative adsorption of propane was calculated to proceed with a barrier of 144–151 kJ/mol.\cite{35}

### 3.4 Catalysis in the Eley-Rideal mediated propylene forming limit (M2)

The second (M2) limiting mechanism features an Os–mediated Eley-Rideal type C\textsubscript{3}H\textsubscript{6} forming mechanism as proposed by Shi et al.\cite{7}. The mechanism is consistent with the presence of surface oxygen in X–ray photoelectron spectra (XPS)\cite{1,5} as well as B–OH vibrations in infrared spectra.\cite{7,36} The applied rate constants are listed in Table 3. The adsorption rate (M2-R15) has again been fitted to match the conversion in the undiluted case, which allowed us to apply a barrierless desorption step, as the adsorption is rate limiting.

The direct C\textsubscript{3}H\textsubscript{6} mechanism (M1, --- in Fig. 5) and the Os-mediated C\textsubscript{3}H\textsubscript{6} mechanism (M2, not shown) show nearly identical selectivity and conversion profiles, despite the different nature of C\textsubscript{3}H\textsubscript{8} activation on the catalytic surface. The pre-exponentials of the adsorption steps in the two mechanisms...
Figure 5: Selectivities ($S$) and conversion ($X$) of selected species as a function of downstream distance with four of the six limit mechanisms: M1: direct C$_3$H$_6$ (---), M3: Os-mediated C$_3$H$_7$O (-----), M4: direct C$_3$H$_7$ (-----), and M5: Os-mediated C–C scission (-----). Case with an undiluted catalyst (left) and with the highest dilution ($V_{\text{bed}}/V_{\text{cat}} = 8.5$, right), both at $\sim 40$ ml min$^{-1}$. Lines are calculated data, circles are experimental results, shaded areas correspond to the front and rear heat shield (white), the catalytic zone (red), and SiO$_2$ chips (gray).

differ by around a factor of $10^3$ with the Os-mediated M2 mechanism being the more active (i.e. a reduction in the pre-exponential factor is required to meet the target conversion). The predicted surface coverages of Bs and Os are 1.8% and 98.2% after the first mm and 2.8% and 97.1% after the last mm of the undiluted catalyst, respectively. When the effect of surface coverages on the rate laws is taken into account, the Eley-Rideal pathway leads to a $5/2$ faster propane adsorption rate at the beginning of the catalytic section. However, both mechanisms quickly converge to the same adsorption rate in the last mm of the catalyst, yielding indistinguishable conversion profiles. The availability of free (Bs) and Os sites is therefore not limiting in the current model. A small proportion of sites (0.06% in undiluted, 0.1% in diluted cases) is covered by OHs, regardless of the adsorption pathway. The presence
of OHs is consistent with analysis of the spent catalysts, but it is not conclusive proof of an Eley-Rideal mechanism, as the adsorption of propane may equally plausibly proceed on exposed Bs or Os sites, and the B–OH species can be explained by either abstraction of the second H by Os leading to C₃H₆ formation, or by a surface reaction between Hs and Os. The predicted surface coverages may change once multiple branching pathways are introduced, and once the H/O submechanism is validated for hBN.

Figure 6: Normalised sensitivity coefficients \( c(i) \) of parameters \( i \) with respect to the O₂ adsorption rate for reaction (R4) in the H/O submechanism from Deutschmann et al. [20]

The H/O submechanism, developed for platinum, is taken verbatim from Deutschmann et al. [20].

As we have adjusted \( \Gamma \), a sensitivity analysis on the rate of O₂ dissociative adsorption (R4) was performed by varying the pre-exponential factor \( (A_{R4}) \) by an order of magnitude between \( 1.8 \times 10^8 - 1.8 \times 10^{10} \text{ m}^6\text{mol}^{-2}\text{s}^{-1} \). The largest absolute sensitivity coefficient is \( c(S(C₃H₆)) = \partial S(C₃H₆)/\partial A_{R4} \) with a value on the order of \( 10^{-2} \), which indicates the H/O chemistry is significantly contributing to the surface chemistry. The normalised coefficients of the 10 most sensitive parameters are shown in Figure [6].

\( X(C₃H₈) \) and selectivities to minor species correlate positively with \( A_{R4} \), while \( S(C₃H₆) \) correlates negatively. In a rigorous approach to mechanism development, the H/O submechanism would have to be tailored to account for the differences between Pt and hBN, including pathways such as the associative adsorption of O₂, [7] or the role H₂O may play in active site regeneration. [9] Figure [6] shows that a further increase in the ratio of the effective sticking probabilities of O₂ and C₃H₆ would lead to a higher activity of the catalyst and lower selectivity to propylene.

As shown in Fig. [5] the M1 and M2 mechanisms are unsurprisingly the most selective towards C₃H₆ (——). The downstream profiles show only a small amount of post-catalytic combustion of the main product (gray shading). However, similarly to the gas-phase results, the selectivities towards
C\textsubscript{2}H\textsubscript{4} (- - ) and CO (--- ) are underpredicted, especially in diluted catalytic beds ($\Delta \sim 8\%$). This may be a consequence of the high selectivity towards propylene oxide (c-C\textsubscript{3}H\textsubscript{6}O, --- , 9.0%), acrolein (C\textsubscript{2}H\textsubscript{3}CHO, 3.3%) and formaldehyde (CH\textsubscript{2}O, 1.9%), neither of which has been recorded experimentally.

When compared to the gas-phase $S$ vs $X$ results (Fig. 3), the addition of the surface pathways decreases the agreement with experiment. Therefore, while C\textsubscript{3}H\textsubscript{6} may be produced on the surface, it is unlikely to be the only catalytic product as proposed by Shi et al.

### 3.5 Catalysis in the radical forming limit (M3 and M4)

The initially proposed mechanism for the activity of hBN (M3) involves adsorption on oxygen-covered boron sites and leading to the formation of propoxy radicals (C\textsubscript{3}H\textsubscript{7}O).\[1\] We also include the direct, propyl radical (C\textsubscript{3}H\textsubscript{7}) forming analogue (M4), considered by Venegas and Hermans.\[8\] A catalytic process where propyl radicals desorb rather than undergo further H–abstraction to propylene on the surface seems unlikely. Venegas et al.\[9\] recently proposed a mechanism where surface-bound oxygen (Os) abstracts hydrogen from propane leading to C\textsubscript{3}H\textsubscript{7} isomers via a barrierless process. Here, we include the propyl forming mechanism to probe the potential impact that additional propyl radicals would have on the gas-phase behaviour. The rate constants are listed in Table 3. Rather than overfitting the models by using six parameters in each of the two mechanisms, we have opted to fit only the adsorption pre-exponential terms (M3-R15 and M4-R15) to match the observed conversion. The adsorption steps are therefore rate limiting. The pre-exponential factors for the desorption step are branched to iso- and n-propano (or propyl) radicals, and the order of magnitude estimates are scaled 2:6 to account for the number of equivalent hydrogens in propane. The barrier heights for product desorption are taken from similar gas-phase reactions in the DTU mechanism. As the reference experiments have been carried out at a single temperature, and the adsorption step is enforced to be rate limiting, the choice of the desorption barrier heights is arbitrary.

The two mechanisms show a very different behaviour when considered in isolation as well as when compared to the propylene forming limit cases (M1 and M2). In the undiluted case, the propoxy mechanism (--- ) results in a significantly higher amount of C–C scission than the propyl mechanism (----- ). The selectivity to the main product, propylene, is significantly underpredicted by both of these
mechanisms, and it is dropping in the catalytic zone (red area) of the reactor. The mechanism based on C$_3$H$_7$O isomers underpredicts S(C$_3$H$_6$) by over 20% (---), while overpredicting S(C$_2$H$_4$) by 6% (---), and CO (---) by 0.6%. By contrast, in the undiluted case the mechanism featuring C$_3$H$_7$ isomers underpredicts S(C$_3$H$_6$) to a smaller degree (-----), and it predicts the correct amount of C$_2$H$_4$ (-----).

However, the selectivity to propylene oxide (-----) is nearly double that of the other mechanisms studied, as the propyl radicals are clearly forming propylene oxide in the gas-phase upon (the unlikely) desorption from the catalyst. Finally, upon dilution of the catalytic bed, both mechanisms converge towards the values predicted for the M1 and M2 mechanisms as the gas-phase chemistry pushes the selectivities towards equilibrium. Both mechanisms also predict c$^\text{−}$C$_3$H$_6$O and C$_2$H$_3$CHO selectivities similar to the M1 and M2 mechanisms, with the C$_3$H$_7$O pathways yielding the highest amount of CH$_2$O (2.8%).

### 3.6 Catalysis in the C–C scission limit (M5 and M6)

The final two limit mechanisms studied here are two-step models leading to either C$_2$H$_4$ and CH$_3$ formation (M5), or C$_2$H$_6$ and CO formation (M6), both proceeding via O$s$–mediated adsorption, see Table 3. From the multitude of possible saturated, unsaturated, or oxygenated C–C scission products, we chose the above two combinations to directly stimulate C$_2$H$_4$ and CH$_4$ (M5) or CO (M6) production. We note that detailed heterogeneous microkinetic mechanisms for C$_3$ species that also include C$_2$ products are rather rare: the above mentioned mechanism for propane partial oxidation over rhodium [34] only contains desorption pathways for C$_3$H$_8$, CO, CO$_2$, and CH$_4$; the mechanism for propane ODH over vanadium oxide catalysts is more complete [35] but has, to our knowledge, not been evaluated together with gas-phase chemistry. As in previous cases, the rate constants of the adsorption processes (M5-R15, M6-R16) are fitted to match the experimental conversion and therefore are rate limiting.

When the surface chemistry is fully shifted towards C$_2$H$_4$ and CH$_3$ (M5, ---), the selectivities to S(C$_2$H$_4$) (---) and S(CH$_4$) (-----) exceed the experimental values for the undiluted case. Tian et al. [37] suggested a catalytic C–C scission would lead to a 1:1 C$_2$:C$_1$ distribution in products while a higher ratio of 2:1 is observed experimentally in the undiluted case. [8] The authors proposed a catalytic CH$_3$-coupling process as a way of accounting for this discrepancy. [37] Here, we obtain an overall C$_2$:C$_1$ ratio of 1.67 with the oxygen mediated C$_3$H$_6$ forming mechanism (M2) and ratios above 1.90 with both C–C scission
mechanisms. For the undiluted cases, catalytic C–C scission unsurprisingly leads to higher C$_2$:C$_1$ ratios than mechanisms without surface C–C bond scission. Contrary to previous reports\cite{21,37}, we show that the experimental C$_2$:C$_1$ ratios can be matched without CH$_3$-coupling surface reactions. In all other aspects, the C$_2$H$_4$ and CH$_3$ mechanism (M5) is very similar to the M3 mechanism corresponding to the i–C$_3$H$_7$O and n–C$_3$H$_7$O forming limit (----). On the other hand, the C$_2$H$_6$ and CO forming limit (M6, not shown) performs rather poorly, as S(C$_3$H$_6$) is underpredicted by over 30%, S(CO) is overpredicted by 10%, and most of the 22% of C$_2$H$_6$ produced on the surface does not dehydrogenate towards C$_2$H$_4$ in the gas phase. It is therefore unlikely that CO is formed via direct oxidation of C$_3$H$_8$ on the surface, or that C$_2$H$_6$ is formed by the catalyst.

Upon dilution of the catalytic bed, convergence of both C–C scission pathways with the other four mechanisms (M1-M4) can be observed, leading to a significant underprediction of selectivities to S(C$_2$H$_4$) (----, $\Delta = 5\%$) and S(CO) (----, $\Delta = 8\%$) even with C$_2$H$_4$ or CO formed catalytically on the surface. This behaviour is accompanied by a high selectivity to experimentally undetected products c–C$_3$H$_6$O, C$_2$H$_3$CHO and CH$_2$O.

### 3.7 Impact of propylene oxide chemistry on selectivities

As discussed above, the selectivity towards propylene oxide calculated with the DTU mechanism appears at variance with experimental data. The low temperature chemistry of propylene oxide is hence likely to require further work. By contrast, the propylene oxide chemistry in the JetSurF mechanism is based on the high temperature shock temperature work by Lifshitz and Tamburu\cite{35}. This mechanism was later expanded by Burluka et al.\cite{13} and the resulting c–C$_3$H$_6$O submechanism is listed in Table 4. We note that the c–C$_3$H$_6$O and C$_2$H$_3$CHO pathways are not directly coupled and inclusion of the high-temperature decomposition pathways into the DTU mechanism does not impact the selectivities at high bed dilutions. However, the conversion of propane goes down appreciably from 18.5% to 16.7%.

In view of the incomplete low temperature propylene oxide chemistry, a different approach is to replace the c–C$_3$H$_6$O pathways in the DTU mechanism with that shown in Table 4. This modified mechanism is denoted DTU/B. As shown in Fig. 7, the gas-phase selectivity to propylene oxide drops (----), and is compensated mainly by an increase in S(C$_3$H$_6$) (----) and a small increase in S(CO)
Table 4: Propylene oxide formation and decomposition pathways from Burluka et al.\textsuperscript{13} with rate parameters in the form $A T^\beta e^{-E_A/RT}$.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>$A$ (m, mol, s)</th>
<th>$\beta$ (–)</th>
<th>$E_A$ (kJ/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\text{C}_3\text{H}_6 + \text{HO}_2 \leftrightarrow \text{c-C}_3\text{H}_6\text{O} + \text{OH}$</td>
<td>$1.05 \times 10^6$</td>
<td>0.0</td>
<td>59.46</td>
</tr>
<tr>
<td>$\text{C}_3\text{H}_6 + \text{CH}_3\text{OO} \leftrightarrow \text{c-C}_3\text{H}_6\text{O} + \text{CH}_3\text{O}$</td>
<td>$4.00 \times 10^5$</td>
<td>0.0</td>
<td>49.04</td>
</tr>
<tr>
<td>$\text{CH}_3\text{CH}_2\text{OO} + \text{C}_3\text{H}_6 \leftrightarrow \text{cC}_3\text{H}_6\text{O} + \text{CH}_3\text{CH}_2\text{O}$</td>
<td>$8.05 \times 10^5$</td>
<td>0.0</td>
<td>67.78</td>
</tr>
<tr>
<td>$\text{C}_3\text{H}_6 + \text{CH}_2\text{CHCH}_2\text{OO} \leftrightarrow \text{c-C}_3\text{H}_6\text{O} + \text{c-C}_3\text{H}_5\text{O}$</td>
<td>$1.05 \times 10^5$</td>
<td>0.0</td>
<td>59.41</td>
</tr>
<tr>
<td>$\text{C}_3\text{H}_6 + \text{n-C}_3\text{H}_2\text{OO} \leftrightarrow \text{c-C}_3\text{H}_6\text{O} + \text{n-C}_3\text{H}_7\text{O}$</td>
<td>$1.05 \times 10^1$</td>
<td>0.0</td>
<td>0.0</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} \leftrightarrow \text{C}_2\text{H}_5 + \text{HCO}$</td>
<td>$2.45 \times 10^{13}$</td>
<td>0.0</td>
<td>244.80</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} \leftrightarrow \text{CH}_3\text{CH}_2\text{CHO}$</td>
<td>$1.82 \times 10^{14}$</td>
<td>0.0</td>
<td>244.80</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} \leftrightarrow \text{CH}_3 + \text{CH}_3\text{CO}$</td>
<td>$4.54 \times 10^{13}$</td>
<td>0.0</td>
<td>250.60</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} \leftrightarrow \text{CH}_3 + \text{CH}_2\text{CHO}$</td>
<td>$2.45 \times 10^{13}$</td>
<td>0.0</td>
<td>246.10</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} \leftrightarrow \text{CH}_3 + \text{c-C}_3\text{H}_3\text{O}$</td>
<td>$8.00 \times 10^{15}$</td>
<td>0.0</td>
<td>384.97</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{H} \leftrightarrow \text{H}_2 + \text{CH}_2\text{CO} + \text{CH}_3$</td>
<td>$2.70 \times 10^1$</td>
<td>2.0</td>
<td>20.92</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{O} \leftrightarrow \text{OH} + \text{HCO} + \text{C}_3\text{H}_4$</td>
<td>$7.80 \times 10^7$</td>
<td>0.0</td>
<td>21.80</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{OH} \leftrightarrow \text{H}_2\text{O} + \text{CH}_2\text{CO} + \text{CH}_3$</td>
<td>$7.80 \times 10^9$</td>
<td>2.0</td>
<td>-3.20</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{HO}_2 \leftrightarrow \text{CH}_2\text{CO} + \text{CH}_3 + \text{H}_2\text{O}_2$</td>
<td>$1.20 \times 10^6$</td>
<td>0.0</td>
<td>64.85</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{CH}_3 \leftrightarrow \text{CH}_2\text{CO} + \text{CH}_3 + \text{CH}_4$</td>
<td>$6.00 \times 10^5$</td>
<td>0.0</td>
<td>40.20</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{CH}_3\text{OO} \leftrightarrow \text{CH}_3\text{OOH} + \text{CH}_2\text{CO} + \text{CH}_3$</td>
<td>$6.00 \times 10^5$</td>
<td>0.0</td>
<td>40.20</td>
</tr>
<tr>
<td>$\text{c-C}_3\text{H}_6\text{O} + \text{C}_2\text{H}_5 \leftrightarrow \text{C}_2\text{H}_5 + \text{CH}_2\text{CO} + \text{CH}_3$</td>
<td>$6.00 \times 10^5$</td>
<td>0.0</td>
<td>46.02</td>
</tr>
</tbody>
</table>

(- - -) at higher conversions. When the two mechanisms are coupled with the Eley-Rideal propylene limit mechanism (M2), the amount of c–C$_3$H$_6$O formed is appreciably reduced ($\Delta = -5.42\%$), with the selectivities to C$_2$H$_4$ ($\Delta = +0.22\%$), CO ($\Delta = +0.34\%$), and especially C$_3$H$_6$ ($\Delta = +3.95\%$) increasing accordingly as shown in Fig 8. The modification of the DTU mechanism therefore improves the agreement with experiment significantly. However, the discrepancies in $S$(C$_2$H$_4$) and especially $S$(CO) remain.

Figure 7: Effect of c–C$_3$H$_6$O chemistry on the gas-phase selectivity vs conversion behaviour. The unmodified DTU mechanism (——) is compared to the DTU/B mechanism (-----) containing c–C$_3$H$_6$O formation and destruction pathways from Burluka et al.\textsuperscript{13} listed in Table 4. Same conditions as in Fig. 3.

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Figure 8: The effect of propylene oxide decomposition pathways on the selectivities. Shown for $V_{\text{bed}}/V_{\text{cat}} = 8.5$ at $\sim 40$ ml/min flow rate, with gas-phase and heterogeneous mechanisms as indicated.

A further possible explanation for the lack of experimentally observed $c-$C$_3$H$_6$O may be due to its catalytic decomposition towards C–C scission products. Xiao and Wang investigated $c-$C$_3$H$_6$O formation pathways from propylene on Cu surfaces using density functional theory, proposing an oxygenated metallacyclic intermediate as the key intermediate.\cite{31} We note one of these intermediates could plausibly decompose towards CH$_2$O and C$_2$H$_4$ following a single H-shift and explore this possibility by augmenting the M2 mechanism by two speculative pathways denoted as M7.

$$M7 - \text{R17}: c-$C_3$H_6O + 2 Bs \rightarrow OCH_2CHCH_3s_2, \quad s_0 = 0.75, \quad E_A = 95 \text{ kJ/mol}$$

$$M7 - \text{R18}: OCH_2CHCH_3s_2 \rightarrow C_2H_4 + CH_2O + 2 Bs, \quad A = 1.0 \times 10^{13} \text{ s}^{-1}, \quad \beta = 0, \quad E_A = 60 \text{ kJ/mol}$$

The ring-opening adsorption of $c-$C$_3$H$_6$O (M7-R17) is modelled as an associative process, requiring two sites, with a near-unity $s_0$ of 0.75 and a barrier height estimated from the energetics calculated for the Cu$^0$/Cu$^+$ couple (95 kJ/mol).\cite{31} The C–C bond scission and desorption are lumped into a single step (M7-R18), with an order-of-magnitude estimate of the pre-exponential, and the barrier height estimated from gas-phase endothermicity of the overall reaction ($\sim 60$ kJ/mol). The results obtained when this mechanism is coupled to the original DTU gas phase chemistry (DTU + M7) are shown in Fig. 8. Sequence M7 significantly reduces the selectivity to $c-$C$_3$H$_6$O ($\Delta = -4.27\%$) even at the highest bed dilution studied. This is compensated by an increase in $S(C_2H_4)$ ($\Delta = +2.75\%$), $S(CO)$ ($\Delta = +0.83\%$), and $S(CH_2O)$ ($\Delta = +0.69\%$) and suggests that discrepancies in selectivities between the gas-phase model and observed catalytic data may also arise from surface decomposition pathways.
3.8 Effect of higher flow rates

With increased inlet flow rates, the experimentally observed conversion drops and the selectivity shifts towards C$_3$H$_6$. This blow-off effect is more pronounced under higher dilutions of the catalytic bed, as with $V_{\text{bed}}/V_{\text{cat}} = 8.5$ the selectivities to CO and CH$_4$ obtained at $\sim$ 40 ml min$^{-1}$ are almost double of the selectivities at $\sim$ 160 ml min$^{-1}$. When the DTU/B mechanism is coupled with the Os-mediated C$_3$H$_6$ mechanism (M2, in Fig. 9), the experimental $X(C_3H_8)$ (●) are well predicted at all studied inlet flow rates and catalyst dilution ratios. Most qualitative trends with increasing flow rates are well captured, including the shape of the blow-off in $S(C_2H_4)$, $S(CH_4)$, and $S(CO)$ at $V_{\text{bed}}/V_{\text{cat}} \geq 2.0$. A notable exception is the slightly increasing $S(CH_4)$ (●) with increased flow rate in the undiluted case. Quantitatively, the agreement of the DTU/B + M2 mechanism with experimental selectivities is poor, as experimental $S(C_3H_6)$ (●) are overpredicted by the model (— ) in all cases, with a maximum absolute deviation ($\Delta_{\text{max}} = \max(S_{\text{calc}}(\text{prod}) - S_{\text{exp}}(\text{prod}))$) in $S(C_3H_6)$ of +9.6% (at $V_{\text{bed}}/V_{\text{cat}} = 3.5$, 120 ml min$^{-1}$). This leads to a significant underprediction in the C–C scission products even with an undiluted catalyst. In section 3.5 we have coupled the DTU/B to the propyl-forming limit pathway (M4) and we have obtained an excellent agreement in the undiluted case at 40 ml min$^{-1}$ (see —— in Fig. 5).

However, as shown in Fig. 9 at higher inlet flow rates, the $S(C_2H_4)$ is overpredicted (——+, $\Delta = +2.2\%$) at the expense of $S(C_3H_6)$ (—— , $\Delta = -6.3\%$). By contrast, in diluted cases with $V_{\text{bed}}/V_{\text{cat}} \geq 2.0$ this combined mechanism struggles to predict the correct $S(CH_4)$ (—— ) and $S(C_2H_4)$ at low inlet velocities, with $\Delta_{\text{max}}$ in $S(C_2H_4) = -7.0\%$. Furthermore, $S(CO)$ (—— ) remains significantly underpredicted. In summary, the propylene forming limit mechanism (M2) captures the qualitative trends in selectivities with bed dilution and flow rate, and is likely to be a key catalytic pathway. On the other hand, the propyl limit mechanism (M4) produces results that are in better agreement with experiments in undiluted beds, however upon dilution and at higher flow rates it is qualitatively inconsistent with the experimental data. Hence we do not propose it as a credible catalytic pathway.

3.9 Effect of inlet O$_2$ and H$_2$O concentration

Venegas and coworkers have recently discussed the effects of varying inlet C$_3$H$_8$/O$_2$ ratio as well as the impact H$_2$O co-feed has on the activity of the catalyst. Variation in the inlet C$_3$H$_8$/O$_2$ ratio has an
Catalyst dilution: \( V_{\text{bed}} / V_{\text{cat}} \)

Inlet flow rate (ml/min)

Selectivity or Conversion (%)

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**Figure 9:** Selectivity and conversion of selected species as a function of inlet flow rate for all studied catalyst dilution ratios. Symbols are experimental data, solid lines are results calculated with the DTU/B gas-phase mechanism coupled either to the propane limit M2 (---) or the propyl limit M4 (-----) surface chemistries. Colour coding as per Fig. 5.

The effect on selectivity, with higher amount of \( C_2 \) products observed at lower \( O_2 \) concentrations. On the other hand, co-feeding \( H_2O \) has almost no effect on selectivity, however the activity of the catalyst is increased significantly. The results are supported by density functional theory calculations, identifying a metastable active site that is formed dynamically under operating conditions. The authors propose the catalyst is responsible for activating oxygen, which then readily abstracts hydrogen from propane, yielding \( C_3H_7 \) radicals. This is at odds with our results above. Venegas and co-workers propose that active sites can be regenerated in three ways: i) by recombination of surface hydroxyls followed by desorption of water yielding an empty site, ii) by reaction of surface hydroxyls with gas-phase water yielding an activated oxygen site, and iii) by reaction of surface hydrogens with gas-phase \( O_2 \) yielding peroxy radicals.

In the absence of a validated heterogeneous mechanism, we choose to investigate trends in selectivities caused by the changes in the inlet composition as predicted purely by gas-phase chemistry. To investigate the impact of the \( C_3H_8/O_2 \) ratio, we model the system as an adiabatic constant pressure reactor, allowing the inlet mixture to react from a starting temperature of 525°C, with a pressure of 1 atm, and a final \( X(C_3H_8) \) set to 5% to allow a close comparison with the experimental data. The results are shown in Fig. 10. The agreement in \( S(C_3H_6) \) and \( S(CH_4) \) is excellent, the most significant discrepancy is the
Figure 10: Selectivity to selected species as a function of inlet O\textsubscript{2} fraction. Symbols are experimental data, lines are results of calculations with the DTU/B mechanism. Showing cases with inlet C\textsubscript{3}H\textsubscript{8} fraction of 15% (— , ●) and 25% (— — — , ○), inlet O\textsubscript{2} fraction on the abscissa, and N\textsubscript{2} as balance.

Figure 11: Effect of co-fed H\textsubscript{2}O on gas-phase chemistry. Left: Gas-phase selectivity as a function of conversion, from adiabatic calculations, with dry feed (30% C\textsubscript{3}H\textsubscript{8}, 15% O\textsubscript{2}, balance N\textsubscript{2}, — ) and a feed containing 10% H\textsubscript{2}O (———). Right: Calculated gas-phase conversion of propane (lines) and experimental propane destruction rates (symbols)\footnote{Our calculations result in a 20% faster ignition for a mixture containing water (30% C\textsubscript{3}H\textsubscript{8}, 15% O\textsubscript{2}, 10% H\textsubscript{2}O, balance N\textsubscript{2}) compared to the dry inlet composition at 500°C. As shown in Fig. 11(left), the calculated selectivity profiles as a function of conversion are unchanged. The relationship between ignition delay time and conversion is not straightforward. If we assume the residence time is dictated by the inlet flow rate and underprediction in \(S(C_2H_4)\) (— , \(\Delta_{\text{max}} = -6.4\%\)). The underprediction remains roughly constant at all inlet O\textsubscript{2} and is comparable to the results shown in Fig. 3. Therefore, the changes in selectivities upon variation in the C\textsubscript{3}H\textsubscript{8}/O\textsubscript{2} ratio can be attributed to the gas-phase chemistry.}

The changes in the activity of the system with inlet mixtures that include water are two-fold: there is an immediate spike in the activity upon addition of water, accompanied by a smaller and gradual increase in activity while water is co-fed. Addition of water does not impact selectivity.\footnote{Our calculations result in a 20% faster ignition for a mixture containing water (30% C\textsubscript{3}H\textsubscript{8}, 15% O\textsubscript{2}, 10% H\textsubscript{2}O, balance N\textsubscript{2}) compared to the dry inlet composition at 500°C. As shown in Fig. 11(left), the calculated selectivity profiles as a function of conversion are unchanged. The relationship between ignition delay time and conversion is not straightforward. If we assume the residence time is dictated by the inlet flow rate and underprediction in \(S(C_2H_4)\) (— , \(\Delta_{\text{max}} = -6.4\%\)). The underprediction remains roughly constant at all inlet O\textsubscript{2} and is comparable to the results shown in Fig. 3. Therefore, the changes in selectivities upon variation in the C\textsubscript{3}H\textsubscript{8}/O\textsubscript{2} ratio can be attributed to the gas-phase chemistry.}
oven temperature, and therefore constant with respect to the inlet composition, we can calculate the residence time required to obtain a nominal conversion for a dry case, and use this value to compare the relative increase in gas-phase activity due to water addition. Experimental activity data from inlet mixtures of 25% or 15% C\(\text{\textsubscript{3}}\)H\(\text{\textsubscript{8}}\), 15% O\(\text{\textsubscript{2}}\), and 1–20% H\(\text{\textsubscript{2}}\)O (balance is N\(\text{\textsubscript{2}}\)) is available for a constant inlet flow rate with a nominal conversion of 3%.\(\text{[9]}\) The results of adiabatic (……) and isothermal (—) gas-phase calculations, starting at the experimental temperature of 525°C, are shown in Fig. [11] (right). The experimental results are in excellent agreement with the isothermal calculations at inlet fractions of H\(\text{\textsubscript{2}}\)O below 10%. Above this value the experiments begin to approach the adiabatic limit, likely as a consequence of the heat release caused by ODH. We may therefore conclude that the experimentally observed immediate increase in the activity in cases with co-fed water can be adequately explained by gas-phase phenomena. The smaller, gradual effect may also be caused by an additional release of water. However, such transient effects can not be account for using steady-state modelling, especially without an experimental determination of the amount of water in the product stream.

4 Summary and outlook

The current work corroborates the hypothesis\(\text{[6,8,10]}\) that gas-phase chemistry is the main driver of the catalytic performance of hBN as a selective catalyst for ODH of propane. The hBN surface acts as a driver of conversion, however the influence of the surface chemistry on the resulting product distribution decreases significantly with dilution of the catalytic bed, as gas-phase effects begin to dominate. The work highlights the necessity of modelling of the whole heated section of the reactor: even if little to no conversion is observed in blank experiments, and best practices to limit post-catalytic combustion are followed, we show the post-catalytic zone can be responsible for up to 50% of the total observed conversion.

The propylene limit heterogeneous mechanism featuring the Eley-Rideal mediated propylene forming limit (M2) coupled with the DTU mechanism\(\text{[11]}\) augmented by propylene oxide pathways from Burluka et al.\(\text{[13]}\) (DTU/B) is able to qualitatively predict the experimentally observed propane conversion as well as most trends in selectivities as a function of catalyst dilution and inlet flow rate. A contribution of secondary catalytic pathways is likely necessary to quantitatively reproduce the experimentally ob-
served C₂:C₁ product ratio in undiluted beds. However, upon dilution of the catalytic bed all six limit mechanisms converge towards the gas-phase limit, which leads to an underprediction in both $S(C₂H₄)$ and $S(CO)$ even if those products are formed on the catalyst. The DTU mechanism[11] predicts the formation of a significant amount of propylene oxide, and to a lesser extent acrolein and formaldehyde. The overprediction of propylene oxide is most likely a mechanistic artefact due to missing decomposition pathways or catalytic activity of hBN towards C₃H₆O. The modified DTU/B mechanism is able to predict the observed effects of inlet C₃H₈/O₂ ratio on selectivities, and can account for the immediate increase in activity upon H₂O co-feed. The C₃:C₂:C₁ product distribution predicted using the modified DTU/B mechanism matches the experimentally observed distribution, however, the detailed speciation, particularly of C₁ oxygenated species, is at odds with the modelled experiments. Further study of the low-temperature oxidation chemistry of the above species is necessary.

Finally, we would like to emphasise the importance of a comprehensive approach to the evaluation of gas-phase kinetics in any mechanistic study involving heterogeneous phenomena at elevated temperatures. One of the key advantages of microkinetics over the Langmuir-Hinshelwood-Hougen-Watson model is the ease with which gas-phase and heterogeneous models of various complexities can be coupled. With open-source solvers, such as Cantera,[12] the tools are available to everyone; we hope that the executable code archive attached in the Supporting information may encourage wider adoption of such approaches in the catalytic community.

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**Supporting information**

## References


