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Interfacial Bonding Controls Friction in Diamond–Rock Contacts

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Abstract

Understanding friction at diamond–rock interfaces is crucial to increase the energy efficiency of drilling operations. Harder rocks usually are usually more difficult to drill; however, poor performance is often observed for polycrystalline diamond compact (PDC) bits on soft calcite-containing rocks, such as limestone. Using macroscale tribometer experiments with a diamond tip, we show that soft limestone rock (mostly calcite) gives much higher friction coefficients compared to hard granite (mostly quartz) in both humid air and aqueous environments. To uncover the physicochemical mechanisms that lead to higher kinetic friction at the diamond–calcite interface, we employ nonequilibrium molecular dynamics simulations (NEMD) with newly developed Reactive Force Field (ReaxFF) parameters. In the NEMD simulations, higher friction coefficients are observed for calcite than quartz when water molecules are included at the diamond–rock interface. We show that the higher friction in water-lubricated diamond–calcite than diamond–quartz interfaces is due to increased interfacial bonding in the former. For diamond–calcite, the interfacial bonds mostly form through chemisorbed water molecules trapped between the tip and the substrate, while mainly direct tip–surface bonds form inside diamond–quartz contacts. For both rock types, the rate of interfacial bond formation increases exponentially with pressure, which is indicative of a stress-augmented thermally activated process. The mean friction force is shown to be linearly dependant on the mean number of interfacial bonds during steady-state sliding. The agreement between the friction behaviour observed in the NEMD simulations and tribometer experiments suggests that interfacial bonding also controls diamond–rock friction at the macroscale. We anticipate that the improved fundamental understanding provided by this study will assist in the development of bit materials and coatings to minimise friction by reducing diamond–rock interfacial bonding.

Introduction

The underlying physicochemical mechanisms that control friction between sliding surfaces remain poorly understood. In some systems, friction can be described through the dynamical formation and rupture of interfacial bonds.¹ Filippov et al.² developed a model that directly relates macroscopic friction to the formation and rupture dynamics of interfacial molecular bonds. Using nonequilibrium molecular dynamics (NEMD) simulations of hydrogen-terminated amorphous carbon atomic force microscopy (AFM) tips and diamond substrates, Mo et al.³ showed that the kinetic friction force depended linearly on the number of atoms that chemically interact across the sliding contact. Subsequent AFM experiments by Li et al.⁴ revealed that interfacial bonds also control static friction in silica–silica contacts. They suggested that the large amount of interfacial bonding at the nanoscale is quantitatively consistent with that

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3 required to explain the frictional aging phenomena,⁴ which is commonly observed in
4 macroscale rock friction experiments.⁵ Interfacial bonding could also be an important factor in
5 controlling the friction of rocks with other materials, such as diamond drill bits.
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9 Rock drilling is a crucial process for many areas of the energy industry, from the extraction of
10 oil and gas⁶ to the utilisation of geothermal energy.⁷ Over the next decade, drilling could also
11 play a central role to facilitate carbon capture and storage⁸ and the safe disposal of radioactive
12 waste.⁹ Recent estimates have suggested that, in the energy industry, friction and wear
13 account for around 40 % of total energy losses.¹⁰ A significant proportion of these losses
14 originate from the drilling of rocks, which is a rather inefficient process. Drilling efficiency is
15 usually defined as the ratio of the rock compressive strength to the mechanical specific
16 energy.¹¹ At high cutting depths, the drilling efficiency is between 30–50 %, although this can
17 be as low as 10 % at low cutting depths, where most of the energy dissipation occurs through
18 frictional contact.¹² Drilling efficiency could be improved through the development of improved
19 bit materials and coatings.¹³ This could also improve the economic feasibility of deep-well
20 drilling (below 1.5 km), which would be beneficial for oil, gas, and particularly geothermal
21 applications.¹⁴ The cost of wells increases almost exponentially with increasing depth¹⁴ and
22 drilling costs average 50 % of the \$3–8M total cost of deep wells.¹⁵
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33 The introduction of polycrystalline diamond compact (PDC) bits during the 1970s¹⁶ was a
34 significant advancement in drilling technology.¹⁷ PDC bits proved to be extremely effective in
35 drilling soft to medium rock formations (e.g. clay, sand, shale, limestone, sandstone, and
36 siltstone), where they achieved high rates of penetration (ROP) while also maintaining long bit
37 life.¹⁷ However, in harder formations (e.g. mudstone, chert, pyrite, granite, and quartzite), both
38 ROP and bit life were substantially reduced.¹⁷ The ROP is reduced by high friction coefficients
39 at the bit–rock interface, which are 3–5 times higher for PDCs compared to other (roller cone,
40 tungsten carbide insert) drill bits.¹⁸ High friction coefficients, coupled with high sliding velocities
41 (> 1 m s⁻¹),¹⁹ result in large temperature rises (hundreds of degrees) at the bit–rock interface,¹⁹
42 which can promote deleterious structural transformations (graphitisation) within the surfaces
43 of PDC bits.^{20,21} These transformations, coupled with increased abrasive wear due to the
44 higher hardness of the counter surface,²² are the principal causes of reduced bit life in hard
45 rock formations.
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55 Ersoy and Waller suggested that the majority of damage to PDC bits was due to abrasive
56 wear.²³ In fact, abrasive wear is the major wear mechanism in most tribological systems.²² The
57 Archard equation²⁴ is the most popular empirical model to predict abrasive wear inside
58 macroscale contacts:²⁵
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$$V = (K_b F_n d)/H \quad (1)$$

where V is the wear volume, K_b is the wear coefficient, F_n is the load, d is the sliding distance, and H is hardness. The Archard equation²⁴ has frequently been used to model the abrasive wear of PDC bits.^{26–28} The hardness of the polycrystalline diamond (PCD) used in PDC bits is at least 55 GPa.¹⁹ During the drilling process, the bits can often pass through greatly varying geologies. Even within a single rock type, the properties can vary markedly and can be heterogeneous and scale-dependant. Mean hardness values have been measured for several rock types, for example, calcite-rich rocks (e.g. limestone) have mean hardness of ~2 GPa, while quartz-rich rocks (e.g. granite) have a mean hardness of 9–15 GPa.^{19,29} Since these are both much softer than PCD under ambient or typical wellbore temperatures (< 300 °C), low abrasive wear rates are expected from the Archard model²⁴ for PDCs when drilling both granite and particularly limestone rocks. However, the effective hardness of PCD can be reduced below that of quartz (but not calcite) when local cutting temperatures exceed ~750 °C.³⁰ Under these accommodating conditions, PDCs are susceptible to abrasive wear.³¹ This is consistent with experimental observations of higher PDC wear when drilling granite compared to limestone.²³

As in many tribological systems involving direct solid-solid contact,³² stick-slip can occur during PDC drilling.^{33–35} During drilling operations, PDCs can periodically stop and then rapidly accelerate to velocities that are 2–3 times the applied velocity.³⁴ This is highly undesirable since it leads to vibrations that can reduce both ROP and bit life.³⁵ Stick-slip behaviour is particularly prevalent at low rotation speed (sliding velocity) and high weight-on-bit (pressure) conditions.³⁴ It is now widely accepted that bit–rock interactions are critical to the oscillatory friction and stick-slip behaviour observed when using PDCs.^{33–35} Stick-slip is a particular problem in calcite-containing rocks (e.g. limestone) formations,³⁶ where rock powder has been observed to strongly adhere to the PDC surface following tribometer experiments.³⁷ These observations suggest that stick-slip could be caused by the cooperative rupture of chemical bonds at the sliding bit–rock interface.² Such behaviour has previously been confirmed in atomic force microscopy (AFM) experiments of sliding silica-silica interfaces.^{4,38} Conversely, for quartz-containing rocks (e.g. granite), adhesion between the tip and rock are negligible, meaning that stick-slip is less problematic. The chemistry of the diamond–quartz interface is similar to that studied in previous experiments of silica AFM tips sliding on hydrogenated diamond substrates, on which stick-slip was found to be much less pronounced than for silica-silica interfaces.⁴

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3 In addition to the development of new bit materials, drilling fluids can also be used to increase
4 performance. Rehbinder showed that the addition of surfactants to circulating fluids could
5 markedly influence the ROP in hard rocks.³⁹ The original mechanism offered by Rehbinder
6 was that changes in drilling performance in different environments could be a consequence of
7 adsorption-induced reduction in surface energy of the solid being penetrated.⁴⁰ Subsequently,
8 Mills and Westwood,⁴¹ suggested that surfactant solutions that increased the hardness of the
9 rock surface could reduce the ploughing contribution to diamond–rock friction and thus also
10 decrease frictional heating. Since higher temperatures result in increased wear, they
11 suggested that solutions that increase rock surface hardness could reduce tip wear.⁴¹ This is
12 the opposite trend than would be predicted using the Archard abrasive wear model.²⁴ In more
13 recent work by the same authors, the influence of several other factors, such as adsorption
14 kinetics, polarity, and surfactant concentration, on bit wear were also considered.⁴²
15 Controversy still remains in this area due to the complex interacting processes involved in
16 controlling drilling performance.⁴³ The physicochemical nature of these interactions and their
17 effects on friction for different rock types remain unclear. One likely mechanism is that the
18 surfactants reduce friction by passivating the sliding bit and rock surfaces and minimise
19 interfacial bonding.
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32 Macroscale numerical⁴⁴ and analytical⁴⁵ modelling techniques are commonly used to
33 investigate friction at PDC bit–rock interfaces. However, these techniques are not capable of
34 describing the physiochemical transformations that appear to control the tribological response
35 of the system. NEMD simulations are becoming an increasingly useful tool to study
36 physiochemical transformations inside tribological systems.⁴⁶ Following the seminal work of
37 Mo et al.³, NEMD simulations have been used to study the effect of interfacial bonding on
38 friction in other systems. For example, NEMD simulations of the silica-silica interface using
39 ReaxFF showed that friction increased due to the formation of interfacial siloxane (Si–O–Si)
40 bridges between the sliding surfaces.⁴⁷ Similarly, NEMD simulations using density-functional-
41 based tight binding (DFTB) indicated that interfacial C–C bonds increased the friction between
42 sliding diamond-like carbon (DLC) surfaces.⁴⁸ However, NEMD simulations have not yet been
43 used to study the diamond–rock interfaces relevant to PDC friction.
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52 In this study, we use macroscale tribometer experiments and NEMD simulations to compare
53 the kinetic friction of PDC bits on granite and limestone surfaces. In order to incorporate the
54 effects of interfacial bonding, we employ the reactive force field (ReaxFF) method.⁴⁹ The
55 computational cost of ReaxFF simulations are several orders of magnitude lower than first
56 principles techniques, allowing much larger time and length scales to be accessed.⁵⁰ Unlike
57 first-principles methods, careful parameterisation is required in order to obtain reliable results.
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3 Over the last two decades, ReaxFF parameters have been developed to study a very wide
4 range of systems and processes.⁵¹ Of particular interest to this study, ReaxFF has been widely
5 applied to study tribochemical processes occurring between sliding surfaces.⁵² We employ
6 published ReaxFF parameters for quartz⁵³ and develop new parameters for calcite. The
7 tribometer experiments show that friction is much higher for diamond–limestone than
8 diamond–granite interfaces under air and aqueous environments. The NEMD simulations
9 show that this is due to increased interfacial bonding in diamond–calcite contacts during
10 sliding, mostly through chemisorbed water molecules.

17 Methodology

19 Experimental Procedure

20 We used a pin-on-disk rotary tribometer for the friction measurements. Previous studies⁵⁴ have
21 shown that the friction obtained in these experiments can be directly related to ROP in
22 industry-standard tests such as the vertical turret lathe¹⁷ and the ultra-deep single-cutter
23 drilling simulator.¹⁵ Sliding contact, as studied in these experiments, is experienced by worn
24 and shaped cutting elements that are used in some rock drilling designs. In those elements,
25 wherein the cutting action (indentation depth) is low, interfacial friction dominates the overall
26 energy losses.

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28 Carthage Limestone and Sierra White Granite cores were respectively chosen as
29 representative limestone and granite rock types. The rock samples were all ground to the
30 same smooth surface finish prior to the tribometer experiments ($R_q \approx 12 \mu\text{m}$).⁵⁵ Hemispherical
31 PDC pins with a radius of 4.765 mm were employed, providing idealized point contacts. The
32 root-mean-square surface roughness of the pins was measured using white light
33 interferometry ($R_a = 2.86 \mu\text{m}$, $R_q = 3.65 \mu\text{m}$).^{27,37} The tests were conducted in both aqueous
34 and air environments (average relative humidity = 70 %). The experimental sliding velocity
35 was 0.1 m s^{-1} , which is somewhat lower than that used in operational PDC drills ($2\text{--}4 \text{ m s}^{-1}$).¹⁹
36 The load was progressively increased (1–200 N) and held for 5 minutes at the same sliding
37 velocity while friction data was measured. The maximum Hertz pressure, P_{max} , is
38 approximately 2.5 GPa for limestone ($F_n = 100 \text{ N}$) and 3.3 GPa for granite ($F_n = 200 \text{ N}$). Due
39 to the presence of roughness on the rock and diamond surfaces, the peak asperity pressures
40 will be somewhat higher than predicted by the Hertz equation. However, the non-dimensional
41 α parameters calculated for these systems (0.01–0.03) suggest that Hertz theory provides a
42 reasonable estimate of the contact pressure (within 5 %).⁵⁶

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44 The velocities and loads were selected to characterize the friction response at sliding-
45 dominated regimes, where the cutting action is relatively low. This ensured that the friction
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3 forces measured were due mainly to interfacial interactions, rather than ploughing. In addition
4 to the friction measurements, both rock and diamond surfaces were examined using optical
5 microscopy following the tests. No wear of the tips was measurable following the tribometer
6 experiments.
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10 11 **Simulation Setup**

12 In the experiments, the mineral distribution within the granite and limestone rock substrates
13 display spatial heterogeneity, resulting in location-dependant surface chemistry.⁵⁷ Due to their
14 large computational expense,⁵⁰ NEMD simulations with ReaxFF are limited to the study of
15 nanoscale systems.⁴⁶ Therefore, the major constituents of granite (quartz)⁵⁸ and limestone⁵⁹
16 (calcite) were used as representative models of the rock substrates. The suitability of this
17 comparison was confirmed by energy-dispersive x-ray spectroscopy analysis of the transfer
18 film on the diamond pin after the tribometer experiments (Figure S1). The atomically-smooth
19 α -quartz{0001}⁶⁰ and calcite{10.4}⁶¹ surfaces were selected, which have shown to be the most
20 thermodynamically stable in previous density functional theory (DFT) studies.
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28 Experimental evidence suggests that both quartz⁶² and calcite⁶³ surfaces are hygroscopic and
29 are likely to be covered by a water monolayer in both air and aqueous environments.
30 Therefore, as well as the dry surfaces, we performed NEMD simulations using different
31 numbers of water molecules to simulate humid air and aqueous environments. The NEMD
32 simulations of the water-containing systems are expected to be more representative of the
33 conditions in our tribology experiments and for operational PDCs. For the smaller number of
34 water molecules (50), representing the air environment, the surfaces are covered by a water
35 monolayer and most of the molecules remained chemisorbed to the surface during the
36 equilibration phase. For the larger number of water molecules (150), representing the aqueous
37 environment, there were additional water molecules on top of the complete water monolayer,
38 which submerged the tip during sliding. As expected from previous DFT calculations, adsorbed
39 water molecules spontaneously dissociate on both α -quartz{0001}⁶⁴ and calcite{10.4}⁶¹ to form
40 surface hydroxyl groups (Figure S2).
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50 The tip was modelled by a single-crystal diamond hemisphere with a radius of 2.0 nm.⁶⁵ A
51 representative system for the NEMD simulations (calcite surface with 150 water molecules) is
52 shown in Figure 1. The tip radius is more than two orders of magnitude smaller than the
53 experimental tip radius (4.765 mm), resulting in a much lower contact area, A_c . This is not
54 expected to significantly affect the friction coefficient, however, since the load is reduced
55 accordingly to approximately match the mean Hertz pressure for point contacts. Previous
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studies have shown that the shear stress ($\tau = F_f / A_c$) at diamond–quartz interfaces is independent of both tip radius and tip geometry.⁶⁶

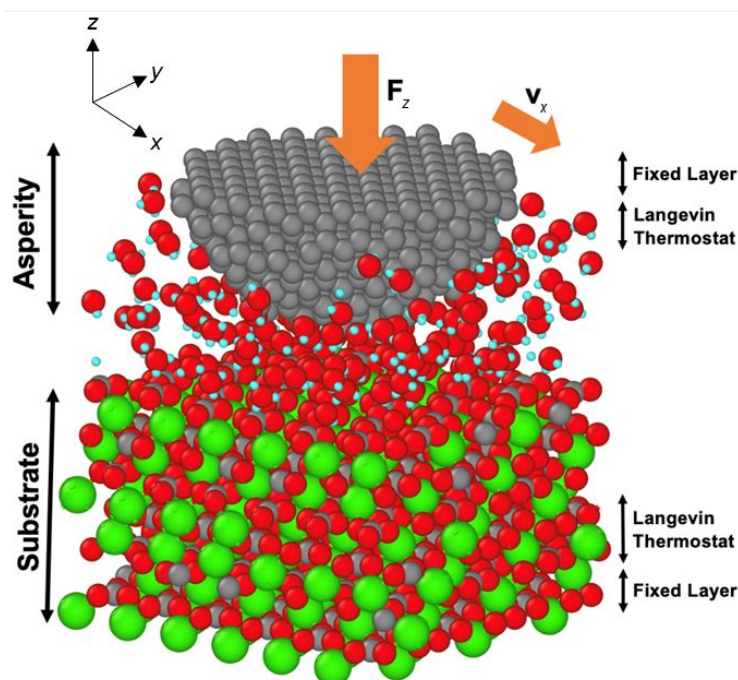


Figure 1. Representative system (calcite surface with 150 water molecules) for the NEMD simulations shown before equilibration. Calcium atoms are shown in green, carbon in grey, oxygen in red, and hydrogen in light blue. Rendered using OVITO.⁶⁷

ReaxFF parameters

ReaxFF is a bond order-based force field that was originally developed by van Duin et al.⁴⁹ to study the reactivity of hydrocarbons. The version of ReaxFF implemented in LAMMPS uses the functional form that was originally outlined by Chenoweth et al.⁶⁸ and was described in more detail by Aktulga et al.⁶⁹ The general functional form of ReaxFF is given by:⁵¹

$$E_{\text{system}} = E_{\text{bond}} + E_{\text{over}} + E_{\text{angle}} + E_{\text{tors}} + E_{\text{vdW}} + E_{\text{Coulomb}} + E_{\text{specific}} \quad (2)$$

where E_{bond} is a continuous function of interatomic distance, describing the energy associated with bond formation (including σ , π , and π - π contributions). E_{angle} and E_{tors} are the energies associated with three-body angle and four-body torsional angle strain respectively. E_{over} is an energy penalty to prevent over-coordination of atoms and is based on atomic valence rules. E_{Coulomb} and E_{vdW} represent the electrostatic and dispersive interactions between all atoms in the system, irrespective of their connectivity and bond order. E_{specific} represents system-specific terms required to capture properties particular to the system of interest, such as lone-

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3 pairs, conjugation, and hydrogen bonding.⁵¹ The point charges on the atoms vary dynamically
4 during the NEMD simulations and are calculated using the charge equilibration (Qeq)
5 method.^{69–71}
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9 For the α -quartz{0001} surfaces, we use the Si/O/H/C ReaxFF parameters developed by
10 Newsome et al.⁵³ to study the oxidation of silicon carbide by oxygen and water. This used a
11 training set including previous first-principles data for silicon,⁷² silicon oxides,^{73,74} and
12 polydimethylsiloxane.⁷⁵ The parameterisation accurately reproduces the experimental density
13 and bulk moduli of α -quartz.⁷³ The relevant parameters have also been validated against first-
14 principles methods for the interactions between silica surfaces and water molecules.⁷⁴ The
15 parameters⁵³ have recently been successfully applied to study the adhesion between
16 graphene sheets and amorphous silica substrates.⁷⁶
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23 A ReaxFF parameterisation is available that includes parameters for all of the elements of
24 interest in this study.⁷⁷ Although this includes parameters developed for CaO,⁷⁸ CaCO₃ was
25 not included in the training set and it performs poorly for this purpose.⁷⁹ A previous version
26 included parameters for CaCO₃, but this required Ca atoms to be fixed as di-cations.⁸⁰
27 Therefore, in this study we developed new ReaxFF parameters for Ca/O/H/C using DFT that
28 do not require fixed charges.
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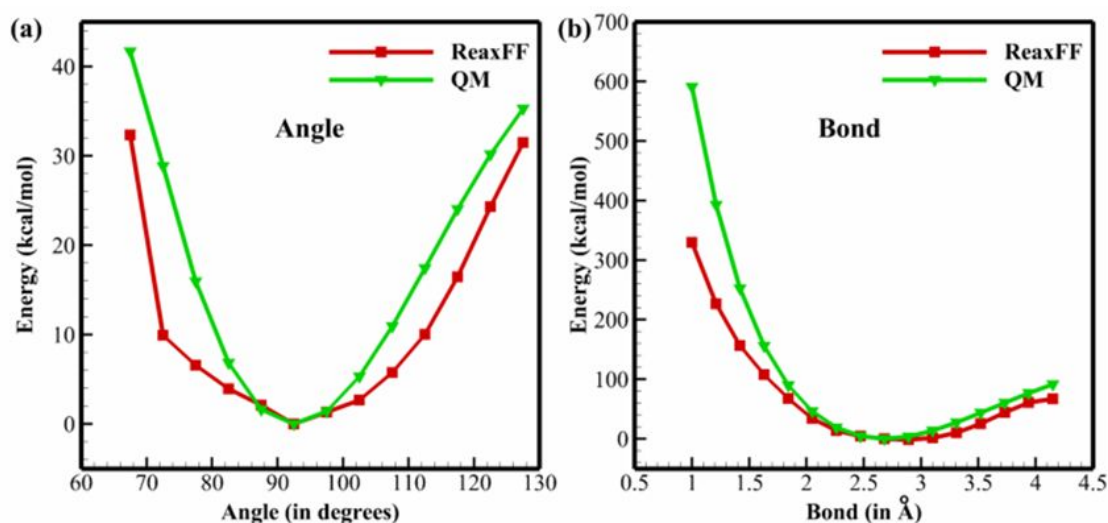
34 The DFT calculations of CaCO₃ were performed with the Jaguar software⁸¹ using the M06-2x
35 functional⁸² with the LACV3P++** basis set. Full geometry optimizations were performed on
36 these clusters without using any symmetry or structural constraints. To obtain potential energy
37 profiles, constrained geometry optimization was applied for the Ca–O–C angle (65–130°) and
38 the Ca–C off-diagonal (1.0–4.2 Å). The vibrational frequency of CaCO₃ was also calculated
39 using the same functional and basis set.
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45 Periodic DFT calculations for CaCO₃ and Ca condensed phases were then performed using
46 the Vienna ab initio simulation package (VASP).^{83–85} The DFT calculations use projector
47 augmented wave (PAW) pseudopotentials⁸⁶ and Perdew-Burke-Ernzerhof (PBE) exchange-
48 correlation functional⁸⁷ with an energy cutoff of 520 eV. All calculations were performed using
49 spin polarization. For CaCO₃, the Brillouin zone is sampled with an (4 × 4 × 4) Monkhorst-
50 Pack k-point mesh.⁸⁸ The equilibrium lattice constant was calculated and the equation of state
51 was determined by deforming the lattice by ±10 %.
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58 In this study, we have optimized the ReaxFF parameters for the Ca–O–C angle and the Ca–
59 C off-diagonal to develop a transferable ReaxFF potential for Ca/C/O interactions, without
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3 requiring local charge constraints.⁸⁰ The Ca–O parameters were obtained from Pitman and
4 van Duin.⁷⁷ The interaction between calcite surfaces and water molecules has previously been
5 validated against first-principles calculations⁸⁰ and the relevant parameters remain unchanged
6 here. The new parameters were developed by training against new and existing DFT data.
7 We used the standard ReaxFF parameter optimization strategy, which involves a weighted
8 single-parameter search method.⁵¹ Parameter correlations, which are quite extensive in
9 ReaxFF, are captured by performing multiple loops over the optimizable force field parameters
10 until the force field error converges. The weights depend on the relevance of a particular
11 training set data point; in general, data points closer to the equilibrium were given higher
12 weights.

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21 Figure 2 shows the comparison between ReaxFF and the DFT energies for the Ca–O–C angle
22 (a) the Ca–C off-diagonal (b) scanning. The agreement between ReaxFF and DFT is relatively
23 good; most of the energy differences are comparable to the typical error of DFT calculations.
24 The mean energy deviation of ReaxFF is 5.2 kcal mol⁻¹ for the Ca–O–C angle and 7.5 kcal
25 mol⁻¹ for the Ca–C off-diagonal. The vibrational frequencies of CaCO₃ obtained with DFT and
26 ReaxFF are also in good agreement (Figure S3 and Figure S4).



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Figure 2. Comparisons of energy from ReaxFF (red) and DFT (green) for constraining of (a) Ca–O–C angle and (b) Ca–C off-diagonal.

The training set also included condensed phase data for the equation of state for the condensed calcite phase of CaCO₃. ReaxFF was trained against the difference in energy when the volume was varied from $\pm 10\%$ of the equilibrium value, as shown in Figure 3. The ReaxFF parameterisation reproduced the equilibrium density of calcite from DFT within the uncertainty of the measurements, but it slightly underestimates the volume-energy curvature

close to the equilibrium density. The heat of formation and heat of reaction of calcite were also included within the training set. The ReaxFF parameters provides similar energy values for these reactions as the DFT calculations (Table S1).

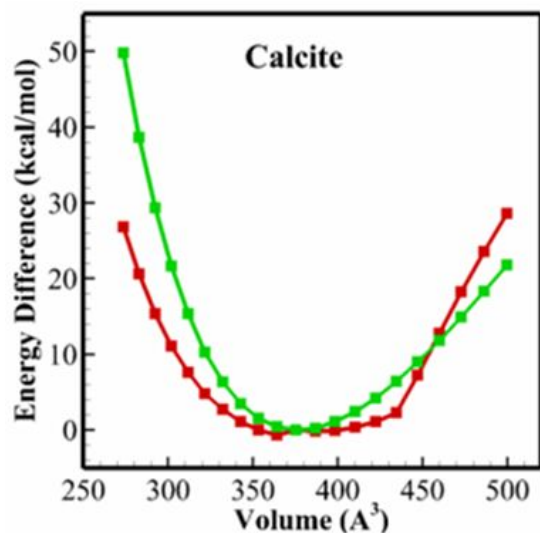


Figure 3. Equations of state of calcite from ReaxFF (red) and DFT (green).

Simulation Details

We performed NEMD simulations using the large atomic/molecular massively parallel simulator (LAMMPS) software package.⁸⁹ We used the velocity-Verlet integration algorithm⁹⁰ with a time step of 0.25 fs. The bottom atomic layer of the substrate was frozen, and periodic boundary conditions were applied in the *x*- and *y*-directions. The temperature was maintained at 300 K using a Langevin thermostat with a coupling time of 25 fs. The thermostat was only applied to the central layers (in the *z*-direction) of the tip and substrate, as shown in Figure 1. A reflective boundary was added in the *xy*-plane at the top of the simulation cell to prevent desorbed species from escaping.

The systems were energy minimised, before being equilibrated at 300 K for 0.1 ns. During the equilibration, a constant normal force ($F_n = 0.1$ nN) was added to the outer layer of atoms in the tip to bring it in contact with the substrate. The normal force was then increased to the target value ($F_n = 2.5$ – 40 nN) and the tip was given a sliding velocity in the *x*-direction ($v_x = 10$ m s⁻¹). This resulted in maximum Hertz pressures in the range $P_{\max} = 1.9$ – 3.9 GPa for diamond–calcite and $P_{\max} = 2.0$ – 4.1 GPa for diamond–quartz. We found that there was negligible difference in the change in friction force with sliding distance for sliding velocities between 1 m s⁻¹ and 10 m s⁻¹ (Figure S5). Therefore, to reduce the computational expense, all results discussed from this point onwards refer to a tip sliding velocity of 10 m s⁻¹. The sliding

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3 simulations were performed for 0.75 ns, which was sufficient for the friction force and number
4 of interfacial bonds to reach a steady state. Chemical bonding information was output every
5 1.0 ps, using a bond order cutoff of 0.3 to identify covalent bonds.⁶⁸ The choice of bond order
6 cutoff only affects the post-processing analysis and does not influence the ReaxFF energy or
7 force calculations.^{77,91}
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11 Results and Discussion

12 Tribometer Experiments

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14 First, we studied the variation in the friction force, F_f , with normal force, F_n , using macroscale
15 tribometer experiments (Figure 4) with diamond–granite (black) and diamond–limestone (red)
16 point contacts in a humid air environment. For both rock types, the friction force increases
17 roughly linearly with normal force with a near-zero intercept. This is consistent with Amontons'
18 friction equation, which states that the coefficient of friction (COF), $\mu = F_f/F_n$. Such a
19 relationship is expected in macroscale contacts and is usually attributed to a linear increase
20 in real contact area between randomly rough surfaces.³ The linear fits in Figure 4 yield $\mu =$
21 0.38 for diamond–limestone and $\mu = 0.18$ for diamond–granite in an air environment. For the
22 diamond–granite contact, the intercept of the linear fit had an intercept of 4 N, suggesting
23 some adhesion at the interface.³
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33 We obtained similar results in an aqueous environment, but with a slightly higher (~10 %)
34 friction coefficient for both rock types. Previous studies have shown that humidity can
35 significantly affect rock friction.⁹² In the current experiments, the air relative humidity (70 %) is
36 already sufficiently high such that there was only a slight increase in friction when changing to
37 an aqueous environment. After the friction experiments, we observed that limestone powder
38 strongly adhered to the diamond tip (Figure S1), which has previously been noted for PDCs
39 that have been used to drill calcite-containing rocks.³⁷
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46 The friction–load curves in Figure 4 are slightly sigmoidal, particularly for the diamond–
47 limestone contact. At low load ($F_n < 80$ N), F_f increases sublinearly with F_n , which is consistent
48 with Hertz theory ($F_f \propto F_n^{2/3}$),³ as shown by the dotted lines in Figure 4. At higher loads ($F_n <$
49 80 N), F_f increases superlinearly with F_n , which implies that the interfacial shear strength
50 increases markedly above a critical load, corresponding to a maximum Hertz pressure of
51 around 2 GPa. While many multi-asperity theories of rough contact predict a linear increase
52 in F_f with F_n ,³ they cannot explain the superlinear increase seen in Figure 4. We attribute the
53 superlinear increase of F_f with F_n at high load to interfacial bond formation, as predicted by the
54 interfacial bonding friction model developed by Filippov et al.² The larger stresses
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encountered at higher load increase the probability for interfacial bond formation by decreasing the activation energy.⁹³ The formation of a greater number of interfacial bonds at high load, which must be ruptured for sliding to proceed, leads to higher friction than is predicted by contact mechanics theories.⁹³ Superlinear friction–load behaviour has recently been observed in AFM experiments of silica–silica contacts,⁹⁴ which are known to form interfacial bonds.⁴ In summary, diamond–rock friction can be adequately described by contact mechanics theories up to a critical load (or pressure) above which interfacial bonding occurs, leading to much higher friction than would otherwise be expected. The friction–load behaviour is more sigmoidal for diamond–calcite than diamond–quartz contacts, suggesting stronger interfacial bonding for the former. The relationship between interfacial bonding and friction was quantified and analysed using NEMD simulations.

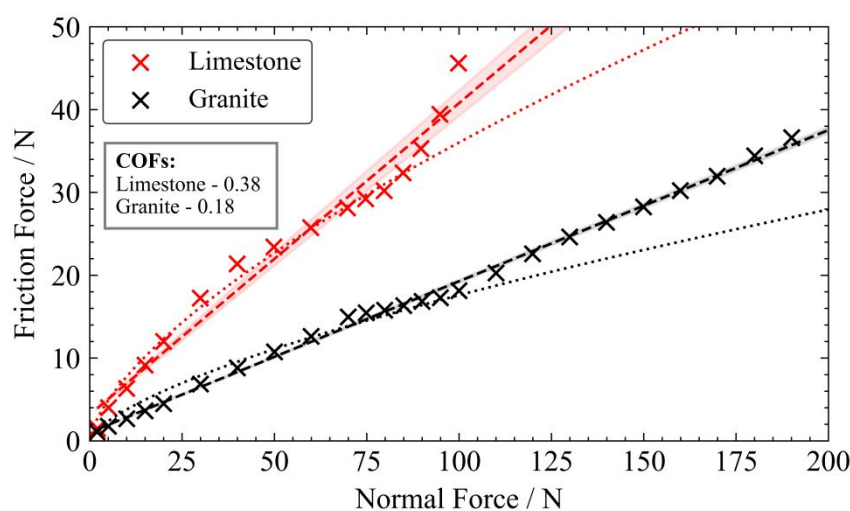
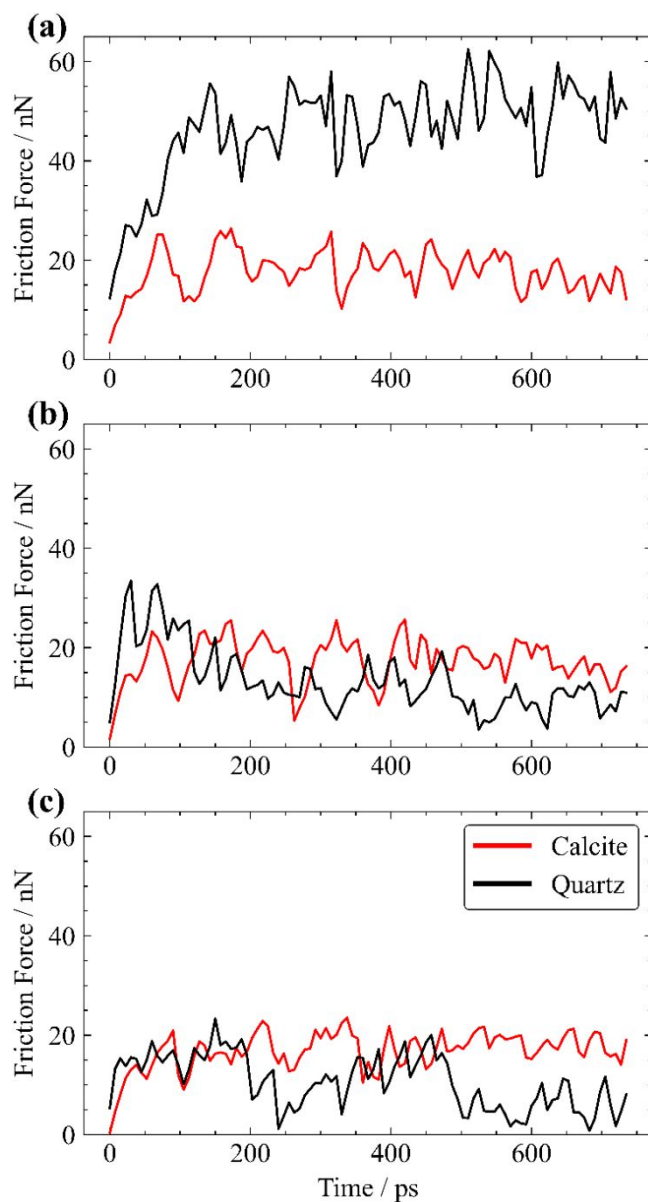


Figure 4. Variation in the friction force, F_f , with normal force, F_n , from the macroscale tribometer experiments with diamond–granite (black) and diamond–limestone (red) point contacts in an air environment. Dashed lines are linear fits to Amontons' friction equation. Shaded regions represent 95 % confidence intervals. Dotted lines are estimates for the low-load region (< 80 N) based on Hertz theory ($F_f \propto F_n^{2/3}$).³

NEMD Simulations

Figure 5 shows how the friction force, F_f , changes with sliding time in the NEMD simulations. The friction force generally increases at short sliding times (< 200 ps) before reaching a steady state. For the water-containing diamond–quartz systems (Figures 5b and 5c), the friction force reaches a maximum before reducing to the steady-state value. Friction curves with similar shapes has been observed previously in NEMD simulations of silica–silica interfaces⁴⁷ and tribometer experiments of quartz-containing sandstone rocks.⁹⁵ For a subset of systems, longer simulations were performed in which there was no further change to the mean friction

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3 force. The steady-state friction force values shown from this point onwards are averaged over
4 the final 200 ps of sliding. Stick-slip friction is observed for all of the studied systems. The
5 degree of stick-slip is more severe in the absence of water (Figure 5a) than when it is present
6 (Figures 5b and 5c), but is quite similar for the quartz and calcite substrates.
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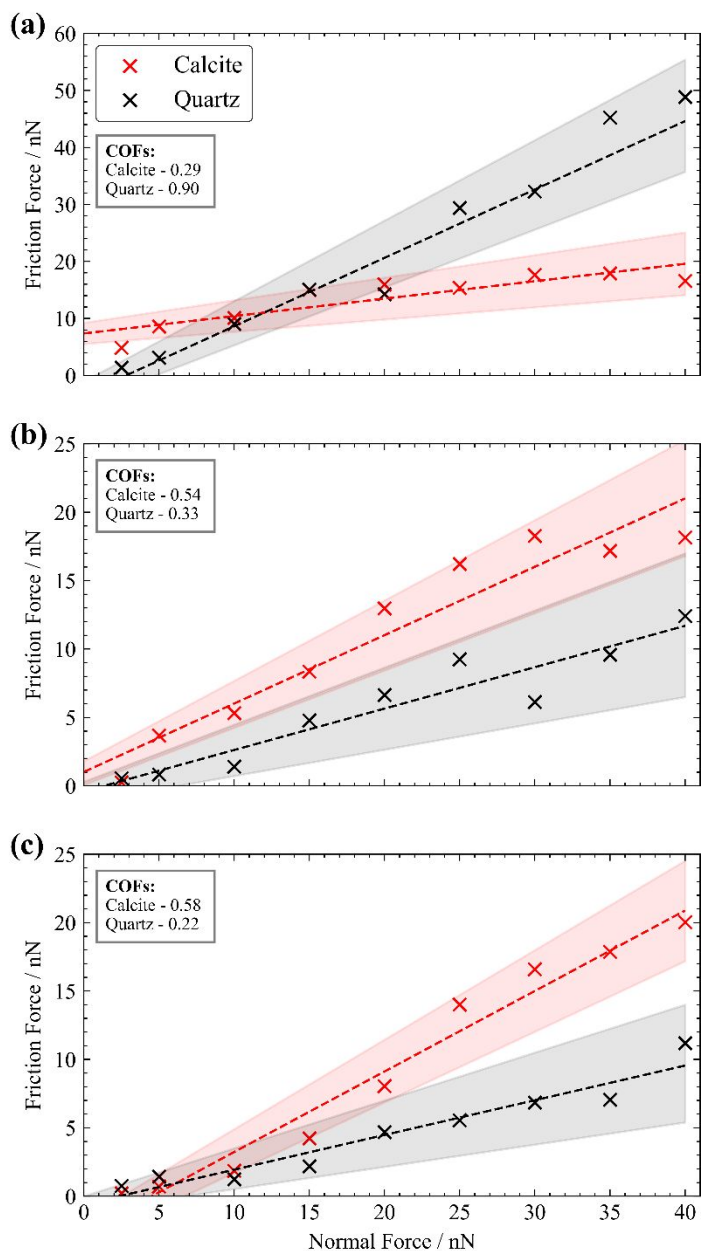
Figure 5. Variation in friction force, F_f , with sliding time from the NEMD simulations for diamond–quartz (black) and diamond–calcite (red) interfaces with 0 (a), 50 (b), and 150 (c) water molecules. Normal force, $F_n = 35$ nN, sliding velocity, $v_x = 10$ m s⁻¹.

Figure 6 shows that F_f increases approximately linearly with F_n in all of the NEMD simulations. This is in agreement with the experimental friction results (Figure 4) and is consistent with Amontons' equation.³ Given that a point contact geometry was used in the simulations, one

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3 might expect that $F_f \propto F_n^{2/3}$, which is consistent with Hertz theory.³ The linear increase in F_f
4 with F_n observed in Figure 6 indicates that the interfacial shear strength increases with
5 pressure,³ which we attribute to interfacial bond formation. The water-lubricated diamond–
6 calcite contacts (Figure 6b and Figure 6c) show a superlinear increase of F_f with F_n at low
7 loads, which can be explained by stress-assisted interfacial bonding.⁹³ It is noteworthy that
8 this behaviour occurs at a similar pressure (2 GPa) as in the experiments (Figure 4). The
9 water-lubricated diamond–granite contacts show a more linear increase in F_f with F_n , which
10 suggests that interfacial bond formation is less prolific compared to diamond–calcite
11 interfaces. Previous single-asperity AFM friction measurements of silica–silica contacts (in
12 which interfacial bonds are known to form⁴) have shown both linear⁹⁶ and superlinear⁹⁴
13 increases in F_f with F_n , depending on the lubricating fluid.
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22 In the absence of water (Figure 6a), the friction coefficient calculated using the Amontons'
23 equation is higher for diamond–quartz ($\mu = 0.90$) than diamond–calcite ($\mu = 0.29$). This is the
24 opposite trend observed experimentally using humid air and aqueous environments (Figure
25 4). For the dry diamond–quartz contact, the linear fit through the data has an intercept close
26 to zero. For the dry diamond–calcite contact, the linear fit to the data has a positive intercept,
27 which suggests that there is some adhesion between the tip and the substrate.³ This could
28 explain why in both the current (Figure S1) and previous³⁷ tribometer experiments using
29 calcite-containing rocks, carbonate material strongly adhered to the diamond surfaces. When
30 a water monolayer is added between the tip and the substrate (Figure 6b), the friction
31 coefficient of the diamond–quartz contact decreases significantly ($\mu = 0.33$), while that for
32 diamond–calcite increases ($\mu = 0.54$). When excess water molecules are added such that the
33 tip is submerged during sliding (Figure 6c), the friction coefficient of the diamond–quartz
34 system decreases further ($\mu = 0.22$), while that for diamond–calcite increases slightly ($\mu =$
35 0.58). It should be noted that the increase in friction coefficient for diamond–calcite from 50 to
36 150 molecules is mostly due to a decrease in friction force at low load ($F_n < 25$ nN), since the
37 friction forces at higher load remain identical within statistical uncertainty. The intercept of the
38 linear fits to the diamond–calcite data decreases from 9 nN for the dry case (Figure 6a) to 2
39 nN when 50 water molecules are present and is negligible when 150 water molecules are
40 added. Additional simulations suggest that there is no measurable change to the friction
41 coefficient when further water molecules (250) are added to either system. Previous
42 experiments have shown that the friction of granite,⁹² quartzite,⁹² silicon⁹⁷ and nanocrystalline
43 diamond⁹⁸ surfaces all decrease with increased relative humidity. First-principles NEMD
44 simulations have also shown that the presence of water molecules at the silica–silica interface
45 significantly reduces friction by suppressing interfacial bond formation.⁹⁹ An increase in friction
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3 in the presence of water, as observed for the diamond–calcite contact, has also been observed
4 for some other materials, such as silicon carbide.¹⁰⁰ The friction coefficients from the water-
5 containing NEMD simulations (Figure 6b and Figure 6c) are in qualitative agreement with
6 those obtained experimentally in an air environment (Figure 4). Most importantly, the friction
7 coefficient is much higher for the diamond–calcite than the diamond–quartz contacts.
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51 **Figure 6.** Variation in the friction force, F_f , with normal force, F_n , from the NEMD simulations
52 with diamond–quartz (black) and diamond–calcite (red) point contacts with 0 (a), 50 (b), and
53 150 (c) water molecules. Mean forces calculated during the final 200 ps of sliding. Dashed
54 lines are fits to Amontons' friction equation. Shaded areas represent 95 % confidence
55 intervals.
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3 The indentation depths in both the tribometer experiments and NEMD simulations were
4 minimised to ensure that friction was dominated by interfacial interactions rather than
5 ploughing. To verify that this was the case, the change in indentation depth with sliding time
6 (Figure S6) was monitored during the NEMD simulations.¹⁰¹ The indentation depth is always
7 deeper for calcite than quartz (Figure S7), as expected due to the lower average hardness of
8 the former (~2 GPa) compared to the latter (~15 GPa).¹⁰² Through the purely geometrical
9 arguments proposed by Bowden and Tabor,¹⁰³ higher friction coefficients are expected at
10 deeper indentation depths because of a larger ploughing contribution. By comparing the how
11 the load-dependant friction coefficient changes with indentation depth compared to the
12 Bowden-Tabor prediction (Figure S8),¹⁰³ it is clear that the ploughing contribution is relatively
13 small for both diamond–quartz and diamond–calcite contacts. Moreover, the large differences
14 in the friction coefficients for diamond–quartz and diamond–calcite interfaces (Figure 6)
15 cannot be explained through ploughing.

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18 To understand the higher friction at the diamond–calcite interface than the diamond–quartz
19 interface observed experimentally and in the water-containing NEMD simulations, the
20 interfacial bond formation during sliding was quantified. The time evolutions of the interfacial
21 bonding for the different systems and conditions are shown in Figure 7. Interfacial bonds are
22 continuously formed and broken during sliding. As interfacial bonds break, the force on the
23 remaining ones increases and the bond rupture becomes synchronised.² This cooperative
24 rupture causes the stick-slip behaviour in the friction force observed in Figure 5. The
25 oscillations in the friction force (Figure 5) are more pronounced than for the interfacial bonds
26 (Figure 7). This suggests that the cooperative formation and rupture of the interfacial bonds
27 are spatially localised at the leading and trailing edge of the tips respectively.¹⁰¹ Since the
28 formation and breaking are not temporally synchronised, there are only small fluctuations in
29 the average number of interfacial bonds during sliding.

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32 In the absence of water molecules, more interfacial bonds form for diamond–quartz (Figure
33 7b) than for diamond–calcite (Figure 7a), leading to higher friction forces and more
34 pronounced stick-slip for the former (Figure 6). When water molecules are added at the
35 interface, far fewer bonds form for diamond–quartz contacts (Figures 7d and 7f), while the
36 number of bonds for diamond–calcite (Figures 7c and 7e) remains similar to the dry case. In
37 fact, at high load (≥ 25 nN), more diamond–quartz interfacial bonds are formed when water
38 molecules are present (Figure 7c) than when they are absent (Figure 7a). This observation
39 could explain why the friction coefficient decreases significantly moving from 0 (Figure 6a) to
40 50 (Figure 6b) and 150 (Figure 6c) water molecules for diamond–quartz contacts, but
41 increases for diamond–calcite. The larger number of interfacial bonds formed for diamond–
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3 calcite contacts than for diamond–quartz when water is present could also explain the higher
4 friction coefficient observed for the former in the NEMD simulations (Figure 6c) and tribometer
5 experiments (Figure 4). Previous NEMD simulations using ReaxFF have shown that, at the
6 interface between hydroxylated amorphous silica and oxidized silicon, the degree of atom
7 transfer was substantially reduced when there were sufficient water molecules present to form
8 a complete monolayer.¹⁰⁴ This was because the silicon atoms at the sliding interface became
9 terminated with hydroxyl groups rather than forming interfacial bonds.¹⁰⁴ NEMD simulations
10 with ReaxFF have also shown that the friction of silica surfaces reduces with increasing
11 hydroxyl group density.¹⁰⁵ Similarly, experiments and first-principles calculations diamond
12 indicated that friction generally decreases with increased relative humidity due to
13 hydrogenation and hydroxylation that passivate the surface.⁹⁸

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22 Figure 7 shows that interfacial bonding increases with sliding time, reaching a steady state
23 after around 500 ps. More interfacial bonds form and the rate of interfacial bond formation
24 increases when the load is increased. This implies that interfacial bond formation at diamond–
25 rock interfaces is a stress-assisted, thermally activated (SATA) process.¹⁰⁶ To confirm this,
26 the temperature-dependence of the interfacial bond formation rate will be investigated in a
27 separate study. In SATA processes, the activation energy (E_0) barrier, which determines the
28 rates and reaction pathways, is reduced by the application of stress, such that:

$$k = Ae^{-(E_0 - N\sigma\Delta v)/(RT)} \quad (3)$$

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34 where A is a prefactor, E_0 is the activation energy, N is Avogadro's number, σ is the applied
35 stress, Δv the activation volume, R the universal gas constant, and T is the absolute
36 temperature.¹⁰⁶ This equation predicts exponential growth in the rate with both temperature
37 and applied stress.¹⁰⁶ The most appropriate stress component in Equation 3 has been debated
38 for different systems. For the mechanochemical decomposition of lubricant additives, it has
39 been proven that, at the macroscale, the shear stress, rather than the normal stress, is the
40 most important parameter.¹⁰⁷ The shear stress has also been selected in nanoscale wear
41 studies.¹⁰⁸ In most previous studies, however, the normal stress is used since this is much
42 easier to measure and control.¹⁰⁶ The stress dependence of the rate of interfacial bond
43 formation can be used to determine the activation volume, Δv .¹⁰⁹ The wear of silicon AFM tips
44 on diamond surfaces¹¹⁰ and the nano-manufacturing of silicon surfaces with a silica tip¹¹¹ have
45 been shown to be SATA processes.¹⁰⁶ Interfacial bonding is also commonly treated as a SATA
46 process.^{93,94}

For single-asperity Hertz contacts, the contact area, A_c , is expected to increase with load as $A_c \propto F_N^{2/3}$, although previous NEMD simulations have suggested that the real contact area, $A_{real} \propto F_N$.³ A higher contact area means that more atoms are close enough to participate in interfacial bonding. Some previous single-asperity studies of SATA processes have normalized the reaction rates by the number of atoms in contact,¹¹⁰ while others have not.¹¹¹ The rates of interfacial bond formation are calculated over the first 200 ps of sliding (dotted lines in Figure 7), where the indentation depth (and thus contact area) is very similar for all of the systems and conditions studied (Figure S6). Moreover, during steady-state, the variation in contact area with load sliding is much smaller than that predicted using the Hertz equation for both diamond–quartz and diamond–calcite contacts (Figure S9). This is because microhardness values used in the Hertz calculations,¹⁰² whereas the indentation depths in the NEMD simulations are always less than 0.5 nm (Figure S7). It is known for many materials that hardness decreases markedly with increasing indentation depth over the first few nanometres.¹¹² For these reasons, we do not normalise the rates shown in Figure 8 by the contact area.

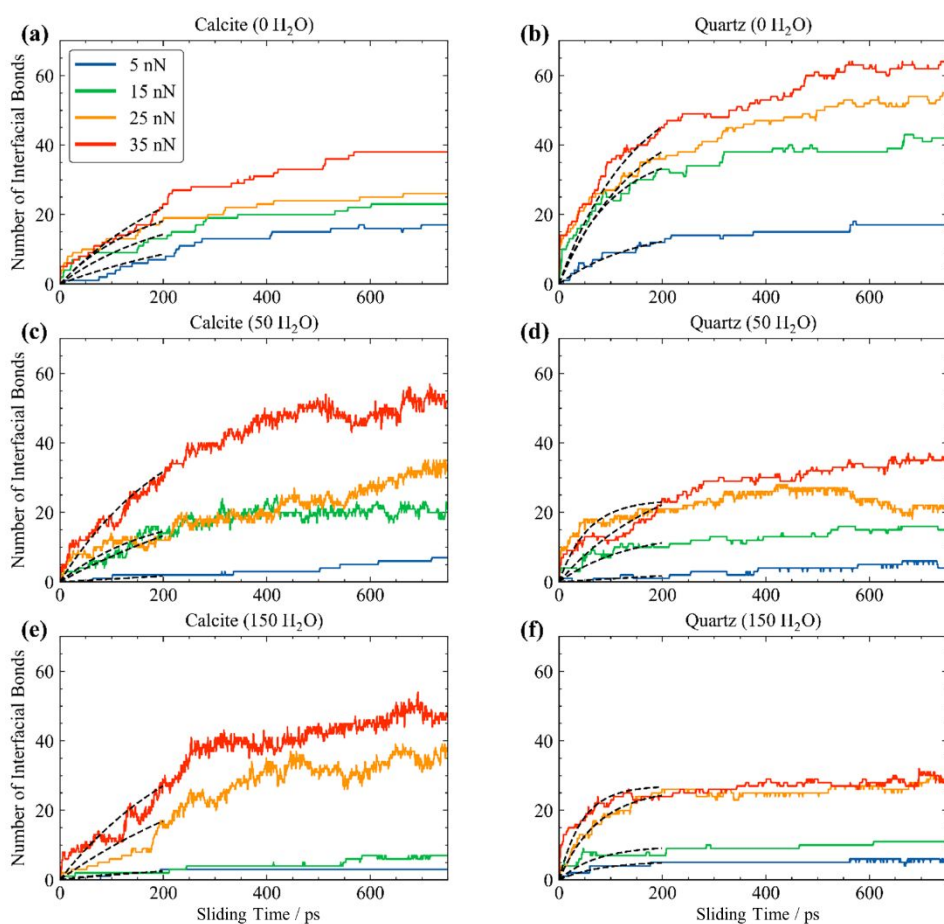


Figure 7. Variation in the total number of interfacial bonds between the tip and the surface during sliding for: (a) diamond–calcite with 0 water molecules, (b) diamond–quartz with 0 water

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3 molecules, (c) diamond–calcite with 50 water molecules, (d) diamond–quartz with 50 water
4 molecules, (e) diamond–calcite with 150 water molecules, and (f) diamond–quartz with 150
5 water molecules. Dashed lines are fits to the function $(1 - e^{-r t})$ over the first 200 ps, where
6 r is the rate of interfacial bond formation and t is sliding time.¹⁰⁹
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12 Figure 8 shows how the rate of interfacial bond formation varies with applied pressure. The
13 rates are calculated using the fits shown in Figure 7. In all cases, the rate of interfacial bond
14 formation increases exponentially with pressure, as predicted using SATA models.¹⁰⁶ This
15 observation is consistent with previous experiments and NEMD simulations of dry silica–silica
16 contacts.¹¹³ When no water molecules are present (Figure 8a), the rate is higher for diamond–
17 quartz than for diamond–calcite. The slope of the linear increase in $\ln(\text{rate})$ with pressure,
18 which is steeper for diamond–quartz than for diamond–calcite, yields an activation volume of
19 $1.17 \pm 0.09 \text{ \AA}^3$ for the former and $0.59 \pm 0.11 \text{ \AA}^3$ for the latter. These values are consistent
20 with single-atom dimensions.¹¹⁰ When 50 water molecules are present (Figure 8b), the rates
21 and activation volumes are similar for both diamond–quartz and diamond–calcite, 1.33 ± 0.09
22 \AA^3 and $1.42 \pm 0.07 \text{ \AA}^3$, respectively. This corresponds to the number of water molecules where
23 the friction coefficients are most similar for the two substrates in Figure 4. When 150 water
24 molecules are present at the interface (Figure 8c), the activation volume is somewhat higher
25 for diamond–calcite ($1.84 \pm 0.02 \text{ \AA}^3$) than diamond–quartz ($1.26 \pm 0.07 \text{ \AA}^3$). This implies a
26 greater stress-dependence of the rate of interfacial bond formation for wet diamond–calcite
27 contacts than for diamond–quartz. The maximum Hertz pressure above which the rate of
28 interfacial bonding accelerates exponentially in the NEMD simulations (2 GPa), corresponds
29 to the pressure at F_f begins to increase superlinearly in with F_n in the macroscale experiments
30 (Figure 4), which supports the proposed link between the two phenomena.⁹³
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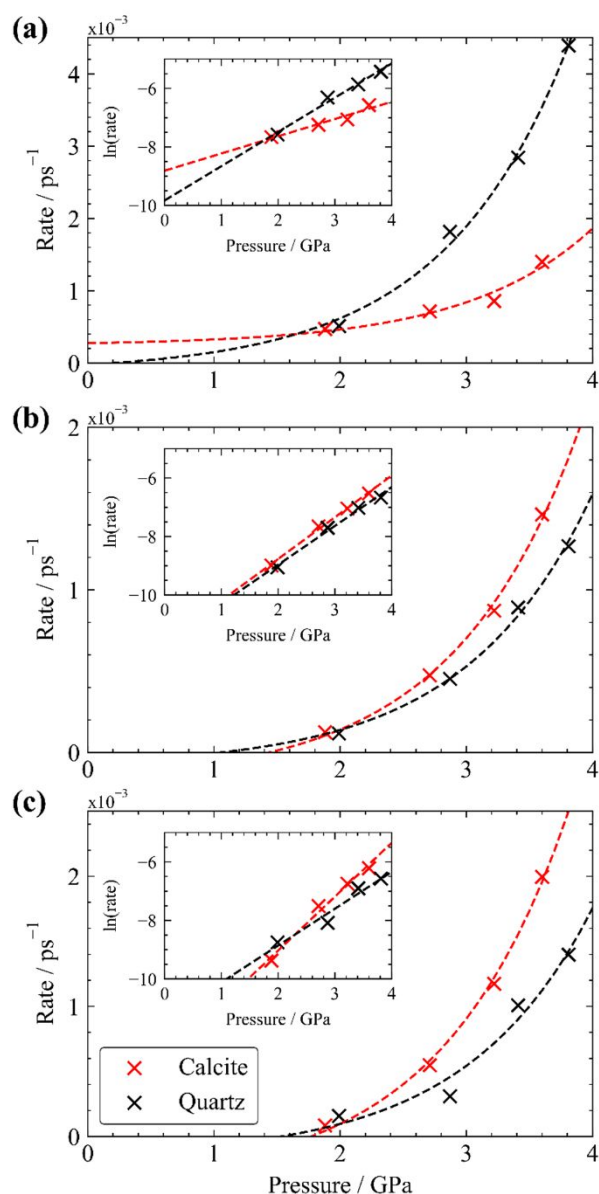


Figure 8. Variation in rate of interfacial bond formation as sliding commences with maximum Hertz pressure for: (a) 0 water molecules, 50 water molecules, 150 water molecules. Insets show linear increase in $\ln(\text{rate})$ with pressure. Dashed lines are fits to Equation 3 used for the calculation of the activation volume.

Figure 9 shows the variation in the steady state number of interfacial bonds with load for the different systems studied. At a nanoscale, friction is proportional to the number of the interatomic interactions between the two sliding surfaces.³ Negligible covalent bonding occurs between C atoms in the tip and Ca, C, (calcite) or Si (quartz) atoms in the substrates; however several C–O interfacial bonds are formed. In the absence of water molecules, only C–O bonds form across the interface for both diamond–calcite (Figure 9a) and diamond–quartz (Figure 9b). A greater number of interfacial C–O bonds are formed for quartz than calcite, which causes the higher friction (Figure 6). Previous NEMD simulations of dry silica–silica interfaces

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3 using ReaxFF have shown that a larger number of interfacial bonds resulted in higher friction.⁴⁷
4 The force needed to break a given type of interfacial bond does not have a fixed value; it
5 depends on the thermal state of the system and the rate at which the force is transmitted to
6 the bond.¹¹⁴
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11 When water is introduced at the diamond–calcite interface (Figure 9c and Figure 9e), the
12 number of interfacial C–O bonds decreases; however, many C–O–Ca and C–H–O bridging
13 bonds are formed. The C–O–Ca bridging bonds will be much stronger than the C–H–O
14 hydrogen bonds.¹¹⁵ Although they are relatively weak, interfacial hydrogen bonds have been
15 shown previously to enhance friction in water-lubricated silicon carbide contacts.¹⁰⁰ At low load
16 ($F_n < 25$ nN), the total number of interfacial bonds remains similar to the dry case for diamond–
17 calcite. At higher load ($F_n \geq 25$ nN), the number of interfacial bonds is higher when water
18 molecules are present at the interface. For diamond–quartz, interfacial C–O bonding
19 substantially reduces when water is added (Figure 9d and Figure 9f) and while some C–O–Si
20 and C–H–O bonds form, the overall number of interfacial bonds is always lower than for the
21 dry case. The percentage of intact water molecules was also monitored during the NEMD
22 simulations. The number of intact water molecules decreases much faster at higher load
23 (Figure S1), suggesting that this could also be a SATA process.¹⁰⁶ Water dissociation occurs
24 faster and to a greater degree at the diamond–calcite interface than diamond–quartz. This
25 dissociation facilitates a greater degree of interfacial bond formation through the O and H
26 atoms at diamond–calcite interfaces than diamond–calcite without over-coordination of the O
27 atoms.
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40 Previous ReaxFF⁶⁵ NEMD and first-principles⁹⁹ NEMD simulations of aqueous silica–silica
41 contacts showed that interfacial Si–O bonds formed during sliding at high pressure, leading to
42 increased friction. DFTB simulations of the dry diamond–silica interface have shown that both
43 interfacial C–O and C–Si bonds form at very high pressure (5 GPa) and sliding velocity (100
44 m s⁻¹).¹¹⁶ Furthermore, MD simulations with ReaxFF suggested that C–Si bonding occurs at
45 the interface between a silicon tip and a partially hydrogenated diamond substrate at high
46 pressure.¹¹⁷ Accompanying transmission electron microscopy (TEM) experiments showed that
47 adhesion at the diamond–silicon interface increased with sliding speed and applied normal
48 stress because these variables increased the number of bonds formed,¹¹⁷ as predicted by the
49 SATA model.¹⁰⁶
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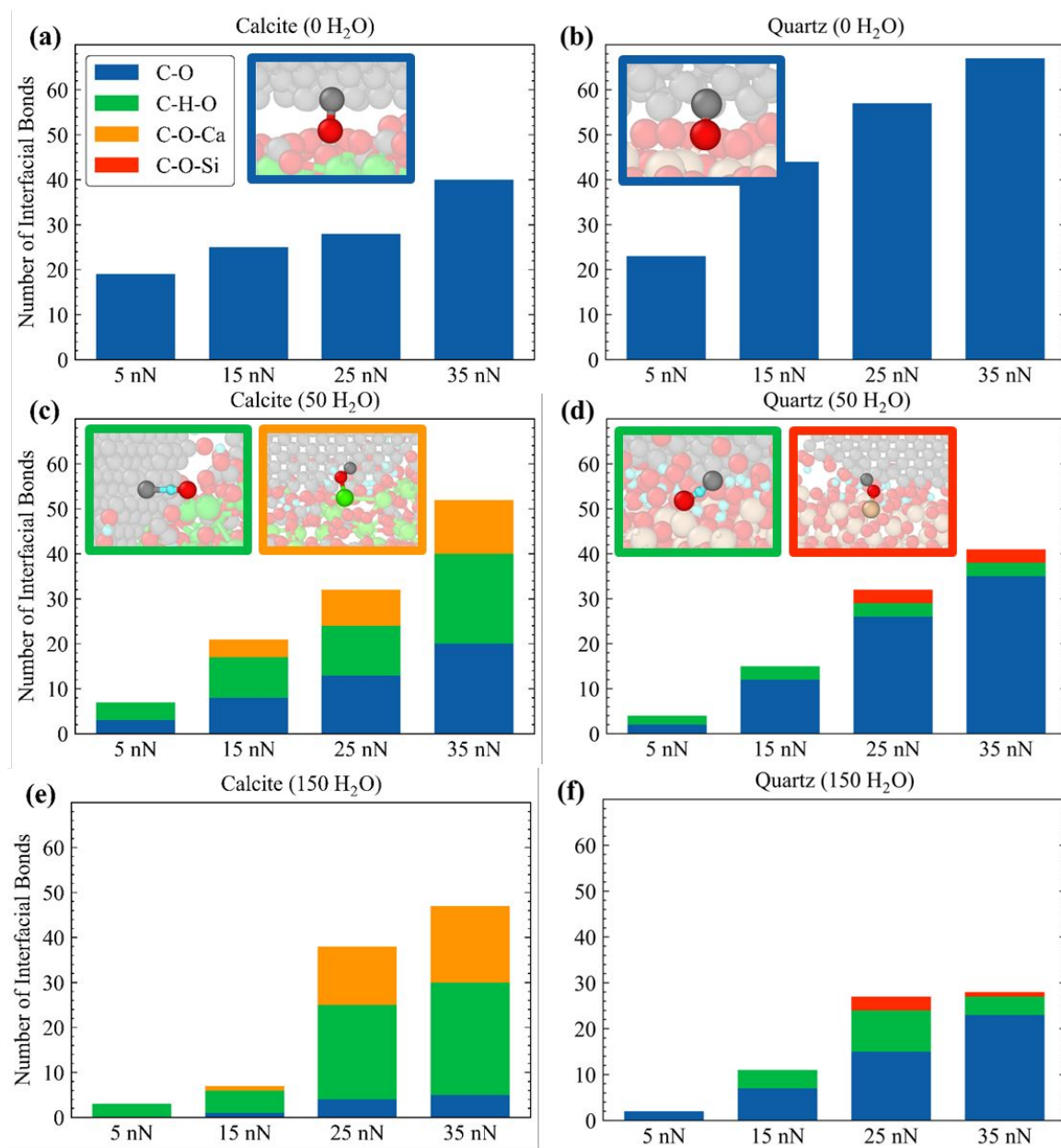


Figure 9. Type of interfacial bonds between the tip and the surface during steady-state sliding for: (a) diamond–calcite with 0 water molecules, (b) diamond–quartz with 0 water molecules, (c) diamond–calcite with 50 water molecules, (d) diamond–quartz with 50 water molecules, (e) diamond–calcite with 150 water molecules, and (f) diamond–quartz with 150 water molecules. Snapshots of each bond type are shown in the coloured boxes. Calcium atoms are shown in green, silicon in orange, carbon in grey, oxygen in red, and hydrogen in light blue. Rendered using OVITO.⁶⁷

As a final confirmation of our hypothesis that interfacial bonding controls friction at aqueous diamond–rock interfaces, the mean number of interfacial bonding was correlated with the mean friction force for the different systems and conditions studied. Figure 10 shows that, for the water-containing systems, the mean friction force increases approximately linearly with

the mean number of interfacial bonds for both diamond–calcite and diamond–quartz contacts. This observation is consistent with both the friction model due to Filippov et al.² and the NEMD simulation results of Mo et al.³, where the same relationship was observed for hydrogen-terminated amorphous carbon–diamond contacts. The gradient is steeper for diamond–calcite (Figure 10a) compared to diamond–quartz (Figure 10b), suggesting that the interfacial bonds are stronger and thus require more mechanical energy to break in the former case. The observation of superlinear friction–load behaviour in both the tribometer experiments (Figure 4) and NEMD simulations (Figure 6) suggest that interfacial bonding could also control friction in these systems not only at the nanoscale, but also at the macroscale.⁹³

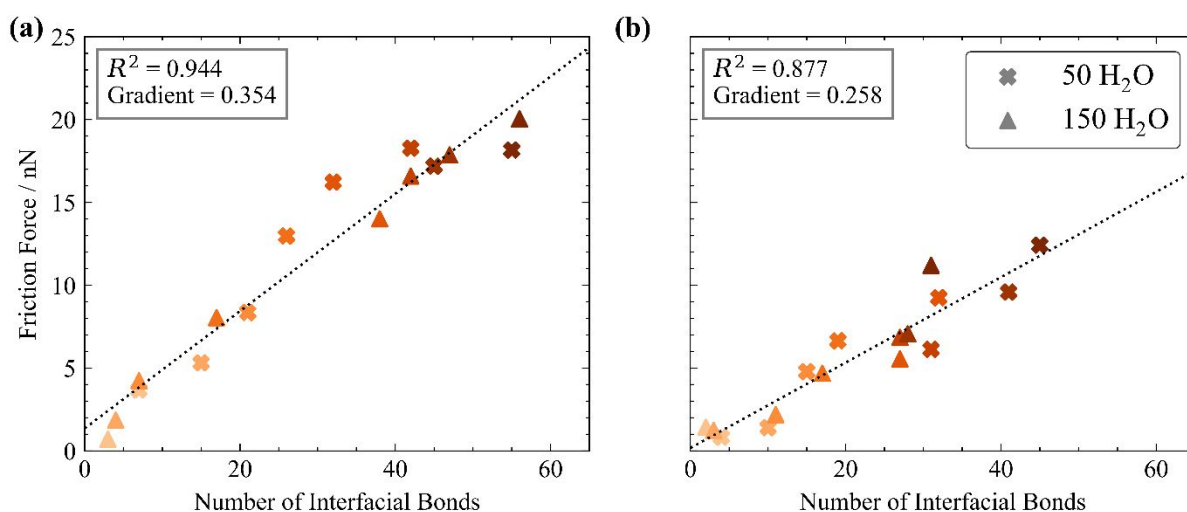


Figure 10. Correlation between the mean friction force and the mean number of interfacial bonds during steady-state sliding for diamond–calcite (a) and diamond–quartz (b). Crosses represent systems with 50 water molecules, triangles are 150 molecules, darker colours indicate higher loads.

Conclusions

In this study, macroscale tribometer experiments and NEMD simulations using ReaxFF have revealed why the friction of diamond–rock interfaces varies significantly depending on the rock type and the presence of water. Superlinear friction–load behavior is observed above a threshold pressure (2 GPa) in both the tribometer experiments in a humid air environment and NEMD simulations with water molecules present at the interface. The NEMD simulations show that this is due to interfacial bonding. The rate of interfacial bond formation increases exponentially with pressure, which is indicative of a SATA process. When water is present, the friction coefficient for diamond–calcite is much higher than for diamond–quartz in both the experiments and NEMD simulations. The NEMD simulations indicate that the higher friction coefficient for diamond–calcite than diamond–quartz contacts is due to a greater amount of

interfacial bonding. Finally, we show that the mean friction force is linearly dependant on the mean number of interfacial bonds during steady-state sliding. We expect that these findings will be useful to design new drill bit materials and coatings that minimise bit–rock interfacial bonding and thus friction.

Acknowledgements

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Supporting Information

Additional figures showing: surface analysis following the friction measurements (Figure S1), water dissociation (Figure S2), comparison of vibrational frequencies of CaCO_3 from ReaxFF and DFT (Figure S3 and Figure S4), the variation in friction force with sliding distance at different sliding velocities (Figure S5), indentation depth with sliding time (Figure S6), steady-state indentation depth with load (Figure S7), ploughing contribution to the friction coefficient (Figure 8), and change in contact area with load (Figure S9). Comparisons of heat of formation and heat of reaction of CaCO_3 (Table S1). ReaxFF parameters for CaCO_3 .

References

- (1) Vanossi, A.; Manini, N.; Urbakh, M.; Zapperi, S.; Tosatti, E. Colloquium: Modeling Friction: From Nanoscale to Mesoscale. *Rev. Mod. Phys.* **2013**, *85*, 529–552.
- (2) Filippov, A. E.; Klafter, J.; Urbakh, M. Friction through Dynamical Formation and Rupture of Molecular Bonds. *Phys. Rev. Lett.* **2004**, *92*, 135503.
- (3) Mo, Y.; Turner, K. T.; SzuLufarska, I. Friction Laws at the Nanoscale. *Nature* **2009**, *457*, 1116–1119.
- (4) Li, Q.; Tullis, T. E.; Goldsby, D.; Carpick, R. W. Frictional Ageing from Interfacial Bonding and the Origins of Rate and State Friction. *Nature* **2011**, *480*, 233–236.
- (5) Dieterich, J. H. Time-Dependent Friction in Rocks. *J. Geophys. Res.* **1972**, *77*, 3690–3697.
- (6) Cleveland, C. J. Net Energy from the Extraction of Oil and Gas in the United States. *Energy* **2005**, *30*, 769–782.
- (7) Moore, J. N.; Simmons, S. F. More Power from Below. *Science*. **2013**, *340*, 933–934.
- (8) Bui, M.; Adjiman, C. S.; Bardow, A.; Anthony, E. J.; Boston, A.; Brown, S.; Fennell, P. S.; Fuss, S.; Galindo, A.; Hackett, L. A.; et al. Carbon Capture and Storage (CCS): The Way Forward. *Energy Environ. Sci.* **2018**, *11*, 1062–1176.
- (9) Krall, L.; McCartin, T.; MacFarlane, A. Siting Deep Boreholes for Disposal of Radioactive Waste: Consequences for Tight Coupling between Natural and Engineered Systems. *Environ. Sci. Technol.* **2020**, *54*, 629–646.
- (10) Holmberg, K.; Erdemir, A. Influence of Tribology on Global Energy Consumption, Costs and Emissions. *Friction* **2017**, *5*, 263–284.
- (11) Teale, R. The Concept of Specific Energy in Rock Drilling. *Int. J. Rock Mech. Min. Sci.* **1965**, *2*, 57–73.
- (12) Zhou, Y.; Zhang, W.; Gamwo, I.; Lin, J. S. Mechanical Specific Energy versus Depth of Cut in Rock Cutting and Drilling. *Int. J. Rock Mech. Min. Sci.* **2017**, *100*, 287–297.
- (13) Perrott, C. M. Tool Materials for Drilling and Mining. *Ann. Rev. Mater. Sci.* **1979**, *9*, 23–50.
- (14) Lukawski, M. Z.; Anderson, B. J.; Augustine, C.; Capuano, L. E.; Beckers, K. F.; Livesay, B.; Tester, J. W. Cost Analysis of Oil, Gas, and Geothermal Well Drilling. *J. Pet. Sci. Eng.* **2014**, *118*, 1–14.
- (15) Lyons, K. D.; Honeygan, S.; Mroz, T. NETL Extreme Drilling Laboratory Studies High Pressure High Temperature Drilling Phenomena. *J. Energy Resour. Technol.* **2008**, *130*, 0431021.
- (16) Wentorf, R. H.; DeVries, R. C.; Bundy, F. P. Sintered Superhard Materials. *Science*. **1980**, *208*, 873–880.

- 1
- 2
- 3 (17) Appl, F. C.; Wilson, C. C.; Lakshman, I. Measurement of Forces, Temperatures and
- 4 Wear of PDC Cutters in Rock Cutting. *Wear* **1993**, *169*, 9–24.
- 5
- 6 (18) Pessier, R. C.; Fear, M. J. Quantifying Common Drilling Problems with Mechanical
- 7 Specific Energy and a Bit-Specific Coefficient of Sliding Friction. In *SPE Annual*
- 8 *Technical Conference and Exhibition*; Society of Petroleum Engineers: Washington
- 9 D.C., 1992; p SPE-24584.
- 10
- 11 (19) Wheeler, D. W. Applications of Diamond to Improve Tribological Performance in the
- 12 Oil and Gas Industry. *Lubricants* **2018**, *6*, 84.
- 13
- 14 (20) Glowka, D. A. The Thermal Response of Rock to Friction in the Drag Cutting Process.
- 15 *J. Struct. Geol.* **1989**, *11*, 919–931.
- 16
- 17 (21) Mehan, R. L.; Hibbs, L. E. Thermal Degradation of Sintered Diamond Compacts. *J.*
- 18 *Mater. Sci.* **1989**, *24*, 942–950.
- 19
- 20 (22) Burwell, J. T. Survey of Possible Wear Mechanisms. *Wear* **1957**, *1*, 119–141.
- 21
- 22 (23) Ersoy, A.; Waller, M. D. Wear Characteristics of PDC Pin and Hybrid Core Bits in
- 23 Rock Drilling. *Wear* **1995**, *188*, 150–165.
- 24
- 25 (24) Archard, J. F. Contact and Rubbing of Flat Surfaces. *J. Appl. Phys.* **1953**, *24*, 981.
- 26
- 27 (25) Kauzlarich, J. J.; Williams, J. A. Archard Wear and Component Geometry. *Proc. Inst.*
- 28 *Mech. Eng. Part J* **2001**, *215*, 387–398.
- 29
- 30 (26) Yahiaoui, M.; Gerbaud, L.; Paris, J.-Y.; Denape, J.; Dourfaye, A. A Study on PDC Drill
- 31 Bits Quality. *Wear* **2013**, *298–299*, 32–41.
- 32
- 33 (27) Yahiaoui, M.; Paris, J.-Y.; Delbé, K.; Denape, J.; Gerbaud, L.; Colin, C.; Ther, O.;
- 34 Dourfaye, A. Quality and Wear Behavior of Graded Polycrystalline Diamond Compact
- 35 Cutters. *Int. J. Refract. Met. Hard Mater.* **2016**, *56*, 87–95.
- 36
- 37 (28) Wang, C.; Li, S.; Zhang, L. Evaluation of Rock Abrasiveness Class Based on the
- 38 Wear Mechanisms of PDC Cutters. *J. Pet. Sci. Eng.* **2019**, *174*, 959–967.
- 39
- 40 (29) Beste, U.; Lundvall, A.; Jacobson, S. Micro-Scratch Evaluation of Rock Types - A
- 41 Means to Comprehend Rock Drill Wear. *Tribol. Int.* **2004**, *37*, 203–210.
- 42
- 43 (30) Bex, P. A.; Shafto, G. R. The Influence of Temperature and Heating Time on PCD
- 44 Performance. *Ind. Diam. Div. Commun.* **1978**, *44*, 128–132.
- 45
- 46 (31) Rabinowicz, E. Abrasive Wear Resistance as a Materials Test. *Lubr. Eng.* **1977**, *33*,
- 47 378–381.
- 48
- 49 (32) Urbakh, M.; Klafter, J.; Gourdon, D.; Israelachvili, J. The Nonlinear Nature of Friction.
- 50 *Nature* **2004**, *430*, 525–528.
- 51
- 52 (33) Richard, T.; Gernay, C.; Detournay, E. A Simplified Model to Explore the Root Cause
- 53 of Stick-Slip Vibrations in Drilling Systems with Drag Bits. *J. Sound Vib.* **2007**, *305*,
- 54 432–456.
- 55
- 56 (34) Kovalyshen, Y. Understanding Root Cause of Stick-Slip Vibrations in Deep Drilling
- 57
- 58
- 59
- 60

- with Drag Bits. *Int. J. Non. Linear. Mech.* **2015**, *67*, 331–341.
- (35) Chen, S.; Wisinger, J.; Dunbar, B.; Propes, C. Identification and Mitigation of Friction-And Cutting Action-Induced Stick-Slip Vibrations with PDC Bits. *SPE Drill. Complet.* **2020**, *35*, 576–587.
- (36) Carpenter, C. Resolving Torsional Vibration in Limestone Reservoirs Reduces Equipment Damage. *J. Pet. Technol.* **2019**, *71*, 68–69.
- (37) Dagrain, F.; Richard, T. On the Influence of PDC Wear and Rock Type on Friction Coefficient and Cutting Efficiency. In *Eurock 2006: Multiphysics Coupling and Long Term Behaviour in Rock Mechanics*; Liege, Belgium, 2006; pp 577–584.
- (38) Tian, K.; Gosvami, N. N.; Goldsby, D. L.; Carpick, R. W. Stick-Slip Instabilities for Interfacial Chemical Bond-Induced Friction at the Nanoscale. *J. Phys. Chem. B* **2018**, *122*, 991–999.
- (39) Rehbinder, P. A.; Shchukin, E. D. Surface Phenomena in Solids during Deformation and Fracture Processes. *Prog. Surf. Sci.* **1972**, *3*, 97–187.
- (40) Westwood, A. R. C.; Ahearn, J. S.; Mills, J. J. Developments in the Theory and Application of Chemomechanical Effects. *Colloids Surf.* **1981**, *2*, 1–35.
- (41) Mills, J. J.; Westwood, A. R. C. Influence of Chemomechanically Active Fluids on Diamond Wear during Hard Rock Drilling. *J. Mater. Sci.* **1978**, *13*, 2712–2716.
- (42) Mills, J. J.; Westwood, A. R. C. Influence of Adsorption Kinetics on Chemomechanically Enhanced Hard Rock Drilling. *J. Mater. Sci.* **1980**, *15*, 3010–3016.
- (43) Cooper, G.; Berlie, J. On the Influence of the Flushing Fluid during Diamond Drilling. *J. Mater. Sci.* **1976**, *11*, 1771–1775.
- (44) Menezes, P. L.; Lovell, M. R.; Avdeev, I. V.; Higgs III, C. F. Studies on the Formation of Discontinuous Rock Fragments during Cutting Operation. *Int. J. Rock Mech. Min. Sci.* **2014**, *71*, 131–142.
- (45) Cheng, Z.; Li, G.; Huang, Z.; Sheng, M.; Wu, X.; Yang, J. Analytical Modelling of Rock Cutting Force and Failure Surface in Linear Cutting Test by Single PDC Cutter. *J. Pet. Sci. Eng.* **2019**, *177*, 306–316.
- (46) Ewen, J. P.; Heyes, D. M.; Dini, D. Advances in Nonequilibrium Molecular Dynamics Simulations of Lubricants and Additives. *Friction* **2018**, *6*, 349–386.
- (47) Li, A.; Liu, Y.; Szlufarska, I. Effects of Interfacial Bonding on Friction and Wear at Silica/Silica Interfaces. *Tribol. Lett.* **2014**, *56*, 481–490.
- (48) Wang, Y.; Xu, J.; Ootani, Y.; Bai, S.; Higuchi, Y.; Ozawa, N.; Adachi, K.; Martin, J. M.; Kubo, M. Tight-Binding Quantum Chemical Molecular Dynamics Study on the Friction and Wear Processes of Diamond-Like Carbon Coatings: Effect of Tensile Stress. *ACS Appl. Mater. Interfaces* **2017**, *9*, 34396–34404.

- 1
2
3 (49) van Duin, A. C. T.; Dasgupta, S.; Lorant, F.; Goddard III, W. A. ReaxFF: A Reactive
4 Force Field for Hydrocarbons. *J. Phys. Chem. A* **2001**, *105*, 9396–9409.
5
6 (50) Plimpton, S. J.; Thompson, A. P. Computational Aspects of Many-Body Potentials.
7 *MRS Bull.* **2012**, *37*, 513–521.
8
9 (51) Senftle, T. P.; Hong, S.; Islam, M. M.; Kylasa, S. B.; Zheng, Y.; Shin, Y. K.;
10 Junkermeier, C.; Engel-Herbert, R.; Janik, M. J.; Aktulga, H. M.; et al. The ReaxFF
11 Reactive Force-Field: Development, Applications and Future Directions. *npj Comput.*
12 *Mater.* **2016**, *2*, 15011.
13
14 (52) Martini, A.; Eder, S. J.; Dörr, N. Tribochemistry: A Review of Reactive Molecular
15 Dynamics Simulations. *Lubricants* **2020**, *8*, 44.
16
17 (53) Newsome, D. A.; Sengupta, D.; Foroutan, H.; Russo, M. F.; Van Duin, A. C. T.
18 Oxidation of Silicon Carbide by O₂ and H₂O: A ReaxFF Reactive Molecular Dynamics
19 Study, Part I. *J. Phys. Chem. C* **2012**, *116*, 16111–16121.
20
21 (54) Dougherty, P. S. M.; Pudjoprawoto, R.; Higgs III, C. F. Bit Cutter-on-Rock Tribometry:
22 Analyzing Friction and Rate-of-Penetration for Deep Well Drilling Substrates. *Tribol.*
23 *Int.* **2014**, *77*, 178–185.
24
25 (55) Reeves, M. J. Rock Surface Roughness and Frictional Strength. *Int. J. Rock Mech.*
26 *Min. Sci.* **1985**, *22*, 429–442.
27
28 (56) Greenwood, J. A.; Johnson, K. L.; Matsubara, E. A Surface Roughness Parameter in
29 Hertz Contact. *Wear* **1984**, *100*, 47–57.
30
31 (57) Lai, P.; Moulton, K.; Krevor, S. Pore-Scale Heterogeneity in the Mineral Distribution
32 and Reactive Surface Area of Porous Rocks. *Chem. Geol.* **2015**, *411*, 260–273.
33
34 (58) Van der Molen, I. The Shift of the α - β Transition Temperature of Quartz Associated
35 with the Thermal Expansion of Granite at High Pressure. *Tectonophysics* **1981**, *73*,
36 323–342.
37
38 (59) Levenson, Y.; Emmanuel, S. Pore-Scale Heterogeneous Reaction Rates on a
39 Dissolving Limestone Surface. *Geochim. Cosmochim. Acta* **2013**, *119*, 188–197.
40
41 (60) De Leeuw, N. H.; Higgins, F. M.; Parker, S. C. Modeling the Surface Structure and
42 Stability of α -Quartz. *J. Phys. Chem. B* **1999**, *103*, 1270–1277.
43
44 (61) Kerisit, S.; Parker, S. C.; Harding, J. H. Atomistic Simulation of the Dissociative
45 Adsorption of Water on Calcite Surfaces. *J. Phys. Chem. B* **2003**, *107*, 7676–7682.
46
47 (62) Pashley, R. M.; Kitchener, J. A. Surface Forces in Adsorbed Multilayers of Water on
48 Quartz. *J. Colloid Interface Sci.* **1979**, *71*, 491–500.
49
50 (63) Stipp, S. L. S.; Hochella, M. F. Structure and Bonding at the Calcite Surface as
51 Observed with X-Ray Photoelectron Spectroscopy (XPS) and (LEED). *Geochim.*
52 *Cosmochim. Acta* **1991**, *55*, 1723–1736.
53
54 (64) Yang, J.; Wang, E. G. Water Adsorption on Hydroxylated α -Quartz (0001) Surfaces:
55
56
57
58
59
60

- 1
2
3 From Monomer to Flat Bilayer. *Phys. Rev. B* **2006**, *73*, 035406.
- 4
5 (65) Yue, D. C.; Ma, T. B.; Hu, Y. Z.; Yeon, J.; van Duin, A. C. T.; Wang, H.; Luo, J.
6
7 Tribochemical Mechanism of Amorphous Silica Asperities in Aqueous Environment: A
8
9 Reactive Molecular Dynamics Study. *Langmuir* **2015**, *31*, 1429–1436.
- 10
11 (66) Brazil, O.; Pharr, G. M. Direct Observation of Partial Slip in Micrometre-Scale Single
12
13 Asperity Contacts. *Tribol. Int.* **2021**, *155*, 106776.
- 14
15 (67) Stukowski, A. Visualization and Analysis of Atomistic Simulation Data with OVITO-the
16
17 Open Visualization Tool. *Model. Simul. Mater. Sci. Eng.* **2010**, *18*, 015012.
- 18
19 (68) Chenoweth, K.; van Duin, A. C. T.; Goddard III, W. A. ReaxFF Reactive Force Field
20
21 for Molecular Dynamics Simulations of Hydrocarbon Oxidation. *J. Phys. Chem. A*
22
23 **2008**, *112*, 1040–1053.
- 24
25 (69) Aktulga, H. M.; Fogarty, J. C.; Pandit, S. A.; Grama, A. Y. Parallel Reactive Molecular
26
27 Dynamics: Numerical Methods and Algorithmic Techniques. *Parallel Comput.* **2012**,
28
29 *38*, 245–259.
- 30
31 (70) Rappe, A. K.; Goddard III, W. A. Charge Equilibration for Molecular Dynamics
32
33 Simulations. *J. Phys. Chem.* **1991**, *95*, 3358–3363.
- 34
35 (71) Nakano, A. Parallel Multilevel Preconditioned Conjugate-Gradient Approach to
36
37 Variable-Charge Molecular Dynamics. *Comput. Phys. Commun.* **1997**, *104*, 59–69.
- 38
39 (72) Buehler, M. J.; van Duin, A. C. T.; Goddard III, W. A. Multiparadigm Modeling of
40
41 Dynamical Crack Propagation in Silicon Using a Reactive Force Field. *Phys. Rev.*
42
43 *Lett.* **2006**, *96*, 095505.
- 44
45 (73) van Duin, A. C. T.; Strachan, A.; Stewman, S.; Zhang, Q.; Xu, X.; Goddard III, W. A.
46
47 ReaxFFSiO Reactive Force Field for Silicon and Silicon Oxide Systems. *J. Phys.*
48
49 *Chem. A* **2003**, *107*, 3803–3811.
- 50
51 (74) Fogarty, J. C.; Aktulga, H. M.; Grama, A. Y.; van Duin, A. C. T.; Pandit, S. A. A
52
53 Reactive Molecular Dynamics Simulation of the Silica-Water Interface. *J. Chem. Phys.*
54
55 **2010**, *132*, 174704.
- 56
57 (75) Chenoweth, K.; Cheung, S.; van Duin, A. C. T.; Goddard III, W. A.; Kober, E. M.
58
59 Simulations on the Thermal Decomposition of a Poly(Dimethylsiloxane) Polymer
60
61 Using the ReaxFF Reactive Force Field. *J. Am. Chem. Soc.* **2005**, *127*, 7192–7202.
- 62
63 (76) Kumar, S.; Parks, D.; Kamrin, K. Mechanistic Origin of the Ultrastrong Adhesion
64
65 between Graphene and A-SiO₂: Beyond van Der Waals. *ACS Nano* **2016**, *10*, 6552–
66
67 6562.
- 68
69 (77) Pitman, M. C.; van Duin, A. C. T. Dynamics of Confined Reactive Water in Smectite
70
71 Clay-Zeolite Composites. *J. Am. Chem. Soc.* **2012**, *134*, 3042–3053.
- 72
73 (78) Manzano, H.; Pellenq, R. J. M.; Ulm, F. J.; Buehler, M. J.; van Duin, A. C. T.
74
75 Hydration of Calcium Oxide Surface Predicted by Reactive Force Field Molecular
76
77

- Dynamics. *Langmuir* **2012**, *28*, 4187–4197.
- (79) Raiteri, P.; Demichelis, R.; Gale, J. D.; Kellermeier, M.; Gebauer, D.; Quigley, D.; Wright, L. B.; Walsh, T. R. Exploring the Influence of Organic Species on Pre- and Post-Nucleation Calcium Carbonate. *Faraday Discuss.* **2012**, *159*, 61–85.
- (80) Gale, J. D.; Raiteri, P.; van Duin, A. C. T. A Reactive Force Field for Aqueous-Calcium Carbonate Systems. *Phys. Chem. Chem. Phys.* **2011**, *13*, 16666–16679.
- (81) Bochevarov, A. D.; Harder, E.; Hughes, T. F.; Greenwood, J. R.; Braden, D. A.; Philipp, D. M.; Rinaldo, D.; Halls, M. D.; Zhang, J.; Friesner, R. A. Jaguar: A High-Performance Quantum Chemistry Software Program with Strengths in Life and Materials Sciences. *Int. J. Quantum Chem.* **2013**, *113*, 2110–2142.
- (82) Sherrill, C. D.; Takatani, T.; Hohenstein, E. G. An Assessment of Theoretical Methods for Nonbonded Interactions: Comparison to Complete Basis Set Limit Coupled-Cluster Potential Energy Curves for the Benzene Dimer, the Methane Dimer, Benzene-Methane, and Benzene-H₂S. *J. Phys. Chem. A* **2009**, *113*, 10146–10159.
- (83) Kresse, G.; Hafner, J. Ab Initio Molecular Dynamics for Liquid Metals. *Phys. Rev. B* **1993**, *47*, 558.
- (84) Kresse, G.; Furthmuller, J. Efficiency of Ab-Initio Total Energy Calculations for Metals and Semiconductors Using a Plane-Wave Basis Set. *Comput. Mater. Sci.* **1996**, *6*, 15–50.
- (85) Kresse, G.; Furthmuller, J. Efficient Iterative Schemes for Ab Initio Total-Energy Calculations Using a Plane-Wave Basis Set. *Phys. Rev. B* **1996**, *54*, 11169.
- (86) Kresse, G.; Joubert, D. From Ultrasoft Pseudopotentials to the Projector Augmented-Wave Method. *Phys. Rev. B* **1999**, *59*, 1758–1775.
- (87) Perdew, J. P.; Burke, K.; Ernzerhof, M. Generalized Gradient Approximation Made Simple. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868.
- (88) Monkhorst, H. J.; Pack, J. D. Special Points for Brillouin-Zone Integrations. *Phys. Rev. B* **1976**, *13*, 5188–5192.
- (89) Plimpton, S. Fast Parallel Algorithms for Short-Range Molecular-Dynamics. *J. Comput. Phys.* **1995**, *117*, 1–19.
- (90) Verlet, L. Computer “Experiments” on Classical Fluids. I. Thermodynamical Properties of Lennard-Jones Molecules. *Phys. Rev.* **1967**, *159*, 98.
- (91) Ewen, J. P.; Ayestarán Latorre, C.; Gattinoni, C.; Khajeh, A.; Moore, J. D.; Remias, J. E.; Martini, A.; Dini, D. Substituent Effects on the Thermal Decomposition of Phosphate Esters on Ferrous Surfaces. *J. Phys. Chem. C* **2020**, *124*, 9852–9865.
- (92) Dieterich, J. H.; Conrad, G. Effect of Humidity on Time- and Velocity-Dependent Friction in Rocks. *J. Geophys. Res.* **1984**, *89*, 4196–4202.
- (93) Ouyang, W.; Cheng, Y.; Ma, M.; Urbakh, M. Load-Velocity-Temperature Relationship

- 1
2
3 in Frictional Response of Microscopic Contacts. *J. Mech. Phys. Solids* **2020**, *137*,
4 103880.
5
6 (94) Ouyang, W.; Ramakrishna, S. N.; Rossi, A.; Urbakh, M.; Spencer, N. D.; Arcifa, A.
7 Load and Velocity Dependence of Friction Mediated by Dynamics of Interfacial
8 Contacts. *Phys. Rev. Lett.* **2019**, *123*, 116102.
9
10 (95) Yahiaoui, M.; Paris, J.-Y.; Delbé, K.; Denape, J.; Gerbaud, L.; Dourfaye, A.
11 Independent Analyses of Cutting and Friction Forces Applied on a Single
12 Polycrystalline Diamond Compact Cutter. *Int. J. Rock Mech. Min. Sci.* **2016**, *85*, 20–
13 26.
14
15 (96) Tian, K.; Gosvami, N. N.; Goldsby, D. L.; Liu, Y.; Szlufarska, I.; Carpick, R. W. Load
16 and Time Dependence of Interfacial Chemical Bond-Induced Friction at the
17 Nanoscale. *Phys. Rev. Lett.* **2017**, *118*, 076103.
18
19 (97) Patton, S. T.; Cowan, W. D.; Eapen, K. C.; Zabinski, J. S. Effect of Surface Chemistry
20 on the Tribological Performance of a MEMS Electrostatic Lateral Output Motor. *Tribol.*
21 *Lett.* **2001**, *9*, 199–209.
22
23 (98) De Barros Bouchet, M.-I.; Zilibotti, G.; Matta, C.; Righi, M. C.; Vandenbulcke, L.;
24 Vacher, B.; Martin, J.-M. Friction of Diamond in the Presence of Water Vapor and
25 Hydrogen Gas. Coupling Gas-Phase Lubrication and First-Principles Studies. *J. Phys.*
26 *Chem. C* **2012**, *116*, 6966–6972.
27
28 (99) Ootani, Y.; Xu, J.; Hatano, T.; Kubo, M. Contrasting Roles of Water at Sliding
29 Interfaces between Silicon- Based Materials: First-Principles Molecular Dynamics
30 Sliding Simulations. *J. Phys. Chem. C* **2018**, *122*, 10459–10467.
31
32 (100) Liu, Y.; Szlufarska, I. Effect of Trace Moisture on Friction. *Appl. Phys. Lett.* **2010**, *96*,
33 101902.
34
35 (101) Gao, H.; Ewen, J. P.; Hartkamp, R.; Müser, M. H.; Dini, D. Scale-Dependent Friction-
36 Coverage Relations and Nonlocal Dissipation in Surfactant Monolayers. *Langmuir*
37 **2021**, *37*, 2406–2418.
38
39 (102) Broz, M. E.; Cook, R. F.; Whitney, D. L. Microhardness, Toughness, and Modulus of
40 Mohs Scale Minerals. *Am. Mineral.* **2006**, *91*, 135–142.
41
42 (103) Bowden, F.; Tabor, D. Friction, Lubrication and Wear: A Survey of Work during the
43 Last Decade. *Br. J. Appl. Phys.* **1966**, *17*, 1521–1544.
44
45 (104) Yeon, J.; van Duin, A. C. T.; Kim, S. H. Effects of Water on Tribochemical Wear of
46 Silicon Oxide Interface: Molecular Dynamics (MD) Study with Reactive Force Field
47 (ReaxFF). *Langmuir* **2016**, *32*, 1018–1026.
48
49 (105) Wang, M.; Duan, F.; Mu, X. Effect of Surface Silanol Groups on Friction and Wear
50 between Amorphous Silica Surfaces. *Langmuir* **2019**, *35*, 5463–5470.
51
52 (106) Spikes, H. A. Stress-Augmented Thermal Activation: Tribology Feels the Force.
53
54
55
56
57
58
59
60

- 1
2
3 *Friction* **2018**, *6*, 1–31.
- 4
5 (107) Zhang, J.; Ewen, J. P.; Ueda, M.; Wong, J. S. S.; Spikes, H. A. Mechanochemistry of
6 Zinc Dialkyldithiophosphate on Steel Surfaces under Elastohydrodynamic Lubrication
7 Conditions. *ACS Appl. Mater. Interfaces* **2020**, *12*, 6662–6676.
- 8
9 (108) Gotsmann, B.; Lantz, M. A. Atomistic Wear in a Single Asperity Sliding Contact. *Phys.*
10 *Rev. Lett.* **2008**, *101*, 125501.
- 11
12 (109) Yeon, J.; He, X.; Martini, A.; Kim, S. H. Mechanochemistry at Solid Surfaces:
13 Polymerization of Adsorbed Molecules by Mechanical Shear at Tribological Interfaces.
14 *ACS Appl. Mater. Interfaces* **2017**, *9*, 3142–3148.
- 15
16 (110) Jacobs, T. D. B.; Carpick, R. W. Nanoscale Wear as a Stress-Assisted Chemical
17 Reaction. *Nat. Nanotechnol.* **2013**, *8*, 108–112.
- 18
19 (111) Chen, L.; Wen, J.; Zhang, P.; Yu, B.; Chen, C.; Ma, T.; Lu, X.; Kim, S. H.; Qian, L.
20 Nanomanufacturing of Silicon Surface with a Single Atomic Layer Precision via
21 Mechanochemical Reactions. *Nat. Commun.* **2018**, *9*, 1542.
- 22
23 (112) Tayebi, N.; Conry, T. F.; Polycarpou, A. A. Determination of Hardness from
24 Nanoscratch Experiments: Corrections for Interfacial Shear Stress and Elastic
25 Recovery. *J. Mater. Res.* **2003**, *18*, 2150–2162.
- 26
27 (113) Vorholzer, M.; Vilhena, J. G.; Perez, R.; Gnecco, E.; Dietzel, D.; Schirmeisen, A.
28 Temperature Activates Contact Aging in Silica Nanocontacts. *Phys. Rev. X* **2019**, *9*,
29 041045.
- 30
31 (114) Ghatak, A.; Vorvolakos, K.; She, H.; Malotky, D. L.; Chaudhury, M. K. Interfacial Rate
32 Processes in Adhesion and Friction. *J. Phys. Chem. B* **2000**, *104*, 4018–4030.
- 33
34 (115) Steiner, T. C-H...O Hydrogen Bonding in Crystals. *Crystallogr. Rev.* **2003**, *9*, 177–228.
- 35
36 (116) Peguiron, A.; Moras, G.; Walter, M.; Uetsuka, H.; Pastewka, L.; Moseler, M. Activation
37 and Mechanochemical Breaking of C-C Bonds Initiate Wear of Diamond (110)
38 Surfaces in Contact with Silica. *Carbon*. **2016**, *98*, 474–483.
- 39
40 (117) Milne, Z.; Schall, J. D.; Jacobs, T. D. B.; Harrison, J.; Carpick, R. W. Covalent
41 Bonding and Atomic-Level Plasticity Increase Adhesion in Silicon-Diamond
42 Nanocontacts. *ACS Appl. Mater. Interfaces* **2019**, *11*, 40734–40748.
- 43
44
45
46
47
48
49
50
51
52
53
54
55
56
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TOC Graphic

