## Supporting information for: Electron-phonon coupling and hot electron thermalization in titanium nitride

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DFT results for gold and all the TiN systems considered: Au,  $TiN_{0.80}O_{0.20}$ ,  $TiN_{0.85}O_{0.15}$ , TiN<sub>0.90</sub>O<sub>0.10</sub>,  $TiN_{0.95}O_{0.05}$ ,  $TiN_{1.00}$ ,  $TiN_{0.97}$ ,  $TiN_{0.94}$ ,  $TiN_{0.91}$ ,  $TiN_{0.88}$ ,  $TiN_{0.84}$ . TiN systems have been ordered with respect to the number of electrons per unit cell.



Figure S1: DFT results for Au. a) Electron band structure and DOS (DOS values in the range 0 to 5 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 200$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.06 states/eV/unitcell and 0 to 0.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S2: DFT results for  $\text{TiN}_{0.80}O_{0.20}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S3: DFT results for TiN<sub>0.85</sub>O<sub>0.15</sub>. a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S4: DFT results for  $\text{TiN}_{0.90}O_{0.10}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S5: DFT results for  $\text{TiN}_{0.95}O_{0.05}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S6: DFT results for TiN. a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S7: DFT results for  $\text{TiN}_{0.97}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S8: DFT results for  $\text{TiN}_{0.94}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S9: DFT results for  $\text{TiN}_{0.91}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S10: DFT results for  $\text{TiN}_{0.88}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.



Figure S11: DFT results for  $\text{TiN}_{0.84}$ . a) Electron band structure and DOS (DOS values in the range 0 to 16 states/eV/unitcell). b) Phonon band structure, DOS, phonon linewidths (magnification  $\times 2$ ) and Eliashberg function (DOS and  $\alpha^2 F$  in the range 0 to 0.12 states/eV/unitcell and 0 to 1.3, respectively). c) Electron and phonon heat capacities. d) Electron-phonon coupling parameter and hot electron thermalisation time.