

1 **Currents Associated with Saturn's Intra-D Ring Azimuthal Field Perturbations**

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10 *Three significant points -*

11 We calculate ionospheric and field-aligned currents associated with the intra-D ring azimuthal fields
12 observed on Cassini's proximal passes

13 Ionospheric currents are 0.5-1.5 MA rad⁻¹ similar to auroral values, while current densities are 5-10
14 nA m⁻² more than an order smaller

15 Complex current patterns often show close north-south conjugacy on larger spatial scales consistent
16 with a variable interhemispheric system

17 Draft A: Submitted to *Journal of Geophysical Research: Space Physics*, 4th February 2019

18 Draft B: Submitted to *Journal of Geophysical Research: Space Physics*, 4th May 2019

19 Draft C: Submitted to *Journal of Geophysical Research: Space Physics*, 21st June 2019

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21 **Abstract** During the final 22 full revolutions of the Cassini mission in 2017, the spacecraft passed
22 at periapsis near the noon meridian through the gap between the inner edge of Saturn's D ring and
23 the denser layers of the planet's atmosphere, revealing the presence of an unanticipated low-latitude
24 current system via the associated azimuthal perturbation field peaking typically at $\sim 10\text{-}30$ nT.
25 Assuming approximate axisymmetry, here we use the field data to calculate the associated horizontal
26 meridional currents flowing in the ionosphere at the feet of the field lines traversed, together with the
27 exterior field-aligned currents required by current continuity. We show that the ionospheric currents
28 are typically $\sim 0.5\text{--}1.5$ MA per radian of azimuth, similar to auroral region currents, while the field-
29 aligned current densities above the ionosphere are typically $\sim 5\text{-}10$ nA m⁻², more than an order less
30 than auroral values. The principal factor involved in this difference is the ionospheric areas into
31 which the currents map. While around a third of passes exhibit unidirectional currents flowing
32 northward in the ionosphere closing southward along exterior field lines, many passes also display
33 layers of reversed northward field-aligned current of comparable or larger magnitude in the region
34 interior to the D ring, which may reverse sign again on the innermost field lines traversed. Overall,
35 however, the currents generally show a high degree of north-south conjugacy indicative of an
36 interhemispheric system, certainly on the larger overall spatial scales involved, if less so for the
37 smaller-scale structures, possibly due to rapid temporal or local time variations.

38 1. Introduction

39 On the final 22 proximal orbits of the Cassini mission at Saturn between late April and mid-September
40 2017, corresponding to spacecraft revolutions (Revs) 271-292, the spacecraft passed through the
41 equatorial plane near periapsis in the noon sector at variable altitudes between ~ 2000 and ~ 4000 km
42 above the 1 bar atmospheric layer, in the narrow gap between the inner boundary of Saturn's ring
43 system and the denser layers of the planet's atmosphere. The mission ended in the upper atmosphere
44 pre-periapsis on Rev 293. An unanticipated feature of the magnetic data in the previously unexplored
45 equatorial region is the presence of a distinctive signature in the azimuthal field component confined
46 to field lines threading the tenuous inner D ring of the planet, and field lines interior thereto, a region
47 that we will term the intra-D ring region. The azimuthal field was usually positive in the sense of
48 planetary rotation, a few tens of nT in amplitude, and approximately symmetrical in form about the
49 magnetic equator (Dougherty et al., 2018).

50 Such field perturbations are suggestive of the presence of an interhemispheric field-aligned current
51 that usually flows north to south on and inside D ring field lines, which closes south to north in the
52 region below the spacecraft, presumably in the Pedersen layer of the planetary ionosphere centered
53 ~ 1000 km above 1 bar (Galand et al., 2011). Estimates of the total current flowing suggest values
54 ~ 0.25 - 1.5 MA per radian of azimuth (Dougherty et al., 2018), with a simple overall best-fit model
55 constructed by Khurana et al. (2018) carrying a current of 1.15 MA rad^{-1} . Such currents are notably
56 similar in magnitude to those flowing on auroral region field lines at northern and southern latitudes
57 poleward of $\sim 70^\circ$ (Hunt et al., 2014, 2015, 2018a; Bradley et al., 2018). However, the field lines on
58 which these intra-D ring currents flow map to the ionosphere within $\sim 30^\circ$ of the equator in the north
59 and within $\sim 25^\circ$ in the south, the north-south asymmetry being due principally to the strong
60 quadrupole planetary field component. Khurana et al. (2018) suggested that the currents are driven
61 by shears in neutral atmospheric wind between the northern and southern ionospheric ends of the
62 field lines, noting the strong latitudinal gradients in tropospheric wind associated with the equatorial
63 jet (e.g., García-Melendo et al., 2011), combined with the above north-south asymmetry in

64 ionospheric field line latitudes. Comparison of the currents involved with those in the auroral regions
65 is not, therefore, intended to imply close commonality of physical origin.

66 While the papers by Dougherty et al. (2018) and Khurana et al. (2018) discuss the data from 9 initial
67 proximal passes, Revs 271-280, omitting Rev 277, a subsequent paper by Provan et al. (2019) has
68 overviewed the data from all 23 proximal Revs, including final partial Rev 293. They showed that
69 the azimuthal field profiles exhibit considerable pass to pass variability, including cases with intervals
70 of strong negative azimuthal field, implying related variability in the strength and direction of the
71 current flow. They also showed that the poloidal (B_r and B_θ) field components measured
72 simultaneously display similar smoothly-varying profiles pass to pass irrespective of the nature of the
73 variable azimuthal field, with no evidently related variations on similar spatiotemporal scales (see
74 Figures 2 and 3 of Provan. (2019)). These findings thus support the picture suggested by Dougherty
75 et al. (2018) and Khurana et al. (2018) that the azimuthal fields relate to an interhemispheric
76 magnetosphere-ionosphere coupling current system which is at least somewhat azimuthally extended
77 in nature, but which is significantly temporally variable on proximal orbit period intervals of ~ 6.5
78 days. In this paper we show that given this inference, it is possible to simply calculate the
79 interhemispheric currents flowing in the meridian from the observed azimuthal field profiles, and to
80 estimate the associated current densities. Simple estimates of the total currents flowing were
81 previously made on a related basis by Provan et al. (2019). Here we show that the horizontal
82 meridional ionospheric currents and integrated field-aligned currents are typically $\sim 0.5-1.5$ MA rad⁻¹
83 in magnitude, in conformity with previous approximate estimates, while newly showing that the
84 associated field-aligned current densities are typically $\sim 5-15$ nA m⁻², both just above the ionosphere
85 and at spacecraft altitudes. While the total current values are similar to those associated with the
86 auroral currents, as previously pointed out by Dougherty et al. (2018) and Khurana et al. (2018), the
87 current densities in the equatorial system are more than an order of magnitude lower. We elucidate
88 the reasons for this difference.

89 2. Data Analysis Procedures

90 2.1. Observational and Theoretical Scenario

91 Observational and theoretical conditions related to this study are illustrated in Figure 1, where we
 92 show views of a meridian plane in cylindrical (ρ, z) coordinates, where ρ is perpendicular distance
 93 from the planetary spin/magnetic axis, and z is distance along the axis from the equatorial plane
 94 positive northward. In both panels of the figure the orange spheroid corresponds to the body of the
 95 planet shown extending to the ionospheric conducting layer ~ 1000 km above the 1 bar surface, thus
 96 with polar and equatorial radii of 55,364 and 61,268 km, respectively. The arrowed black solid lines
 97 show the background field lines obtained by using the principal first three terms (dipole, quadrupole,
 98 and octupole) of the axisymmetric Dougherty et al. (2018) internal field model, plus the Bunce et al.
 99 (2007) ring current model for a nominal subsolar magnetopause radius of 22 R_s . (R_s is Saturn's 1
 100 bar equatorial radius equal to 60,268 km.) The darker blue area shows the field lines passing through
 101 the main ring region extending to $\sim 2.27 R_s$ in the equatorial plane (horizontal dotted line),
 102 corresponding to the outer boundary of the A ring. The lighter blue area shows the field lines passing
 103 through the innermost D ring at equatorial distances between 1.11 and 1.24 R_s , on and inside of which
 104 (white area) the intra-D ring azimuthal field perturbations are observed.

105 In Figure 1a the trajectories of two typical proximal Revs are shown projected into the meridian with
 106 the arrows indicating the direction of motion, from inbound in the northern hemisphere to outbound
 107 in the southern hemisphere. Specifically, we show the trajectories of Revs 287 (red) and 288 (blue)
 108 whose field data (amongst other Revs) are analyzed in section 3, representative of proximal Revs
 109 with larger and smaller periapsides, respectively. The solid circles just north of the equator mark the
 110 points where the trajectories in the meridian lie tangent to the field lines, corresponding to the points
 111 where they map along field lines to the ionosphere closest to the equator, corresponding for Rev 287
 112 to colatitudes from the northern pole of $\sim 72^\circ$ in the northern hemisphere and $\sim 98^\circ$ in the southern
 113 hemisphere, and for Rev 288 to $\sim 76^\circ$ in the northern hemisphere and $\sim 94^\circ$ in the southern hemisphere.

114 These points will be referred to below as the “field-parallel” points on each pass, the concurrent
 115 eastward motion of the spacecraft from morning to afternoon local times (LTs) notwithstanding. The
 116 open circles south of the equator show the periapsis points, at radial distances of 1.047 and 1.027 R_s
 117 for Revs 287 and 288, respectively. The time spent on and inside main ring field lines on each pass
 118 was ~ 1 h, of which the central ~ 28 min was located in the intra-D ring region, the latter spanning LTs
 119 between ~ 10.7 h inbound and ~ 12.4 h outbound on the passes shown.

120 The green lines in Figure 1b show the current system envisaged, consisting of a latitudinally variable
 121 meridional current I_m flowing in the ionosphere, taken positive northward, with current continuity
 122 maintained by distributed field-aligned currents, j_{\parallel} , positive southward along the background field
 123 direction, confined to the intra-D ring region (light blue and white areas). These solenoidal currents
 124 then generate an azimuthal field B_{ϕ} within the intra-D ring region, positive in the sense of planetary
 125 rotation (into the plane of the diagram) for the sense of current flow depicted. We then consider the
 126 observation of azimuthal field B_{ϕ} at some arbitrary point inside the current region with perpendicular
 127 distance ρ from the planetary spin/magnetic axis, as shown by the small black circle. Assuming
 128 axisymmetry, Ampère’s circuital law shows that the total current I^* passing through any surface
 129 bounded by an axial circle radius ρ passing through the point of measurement is given by

$$130 \quad I^* = \frac{2\pi\rho B_{\phi}}{\mu_o}, \quad (1)$$

131 where μ_o is the permeability of free space. In Figure 1b we consider two such surfaces of revolution
 132 about the planetary axis, indicated in the meridian by the blue and red solid and dashed lines. These
 133 extend along the field lines from the point of observation to the ionosphere in the north and south as
 134 shown by the blue and red solid lines, respectively, and then pass through the body of the planet in
 135 some arbitrary manner indicated by the blue and red dashed lines. Since the current passing through
 136 these surfaces in their field-aligned portion (solid lines) is zero from the assumed geometry of the
 137 current system, and since the net current flowing through them within the body of the planet inside

138 of the ionosphere (dashed lines) must also zero, the interior planetary currents forming a closed
 139 system, the total current flowing through these surfaces is just the meridional ionospheric current at
 140 the two ends of the field line, both north and south. Dividing by 2π , equation (1) shows that the
 141 meridional ionospheric current per radian of azimuth, positive northward, flowing at the feet of the
 142 field lines north and south are equal, and given by

$$143 \quad I_m = \frac{\rho B_\phi}{\mu_o} . \quad (2)$$

144 We note current continuity requires that the currents given by equations (1) and (2) are also equal to
 145 the total field-aligned currents flowing on intra-D ring field lines passing outside of the axial circle
 146 considered, as required by current continuity. This can be shown directly by alternatively applying
 147 Ampère's law to a surface bounded by the axial circle that instead passes outward across the full
 148 width of the intra-D ring field lines outside of the circle in Figure 1b, closing north or south over or
 149 through the planet outside of the intra-D ring field region.

150 The values of the field-aligned current density (nA m^{-2}) flowing on the field lines above the
 151 ionospheric layer can thus be determined from current continuity by considering the rate of change
 152 of I_m across the intra-D ring field lines. In Appendix A we show that the associated field-aligned
 153 current density just above the ionosphere, positive southward along the background field, is given by

$$154 \quad j_{\parallel i}(\theta_i) = \frac{n_r(\theta_i)}{R_i^2(\theta_i) \sin \theta_i} \left(\frac{B_i(\theta_i)}{B_{ni}(\theta_i)} \right) \frac{dI_m(\theta_i)}{d\theta_i} , \quad (3)$$

155 where θ_i is the ionospheric colatitude of the spacecraft's magnetic foot point as measured from the
 156 north pole, $R_i(\theta_i)$ is the radial distance of the ionosphere from the planet's center taken to be a
 157 spheroid of revolution with equatorial and polar radii 1000 km above the 1 bar surface as above,
 158 $n_r(\theta_i)$ is the radial component of the outward unit normal to the ionospheric surface, $B_i(\theta_i)$ is the
 159 ionospheric field strength, $B_{ni}(\theta_i)$ is the field normal to the ionospheric surface positive outward,

160 and $I_m(\theta_i)$ positive northward is given by equation (2). From current continuity the current density
 161 at any other point (r, θ) on the same field line, in particular that at the spacecraft, is given by

$$162 \quad j_{\parallel}(r, \theta) = \left(\frac{B(r, \theta)}{B_i(\theta_i)} \right) j_{\parallel i}(\theta_i) \quad . \quad (4)$$

163 In Appendix B we show that equations (1)-(4) remain approximately valid if the solenoidal current
 164 structure is of finite azimuthal length, or varies significantly with azimuth, provided that the azimuthal
 165 length scale concerned is somewhat larger than the dimensions in the meridian of the effective
 166 solenoid. If from Figure 1b we take the latter dimension to be, e.g., $\sim 0.25 R_s$, then we require the
 167 azimuthal length scale to be at least, e.g., $\sim 0.5 R_s$, corresponding to ~ 2 h of LT (see further in
 168 Appendix B). The data discussed by Provan et al. (2019) demonstrate directly from the LT coverage
 169 on each pass (~ 1.5 h LT), and over the proximal orbit data set as a whole (~ 3.5 h LT), that the
 170 corresponding structures are at least as azimuthally extended as this.

171 **2.2. Data Set and Analysis Methodology**

172 Figure 2 shows azimuthal field data from the four representative proximal periapsis passes analyzed
 173 in detail here, plotted over the interval ± 40 min about the time of the field-parallel point taken as $t = 0$
 174 (see Figure 1a). The UT times at this point are given in the figure caption. The 80 min interval shown
 175 encompasses the full pass across the ring region field lines as indicated by the set of vertical lines,
 176 the outer pair of red dashed lines corresponding to the field line passing through the outer boundary
 177 of the A ring, while the inner pair of blue lines similarly correspond to the field lines passing through
 178 the outer (solid) and inner (dashed) boundaries of the D ring. The fields as measured are plotted in
 179 Figures 2a-2d, clearly showing the intra-D ring field features, approximately symmetrical about the
 180 field-parallel point, superposed on a more slowly-varying ring region background. These data have
 181 been derived from measurements using the highest range of the fluxgate magnetometer for total field
 182 strengths above 10,000 nT, with digitization steps of 5.4 nT (Dougherty et al., 2004). They have been
 183 averaged here to 10 s resolution to reduce the corresponding digitization noise to the few-nT level
 184 that remains evident, e.g., in the region of more slowly varying fields outside of the D ring region.

185 Initial analysis of the data follows the methodology adopted by Provan et al. (2019). To isolate the
 186 main intra-D ring B_ϕ feature we first fit a fourth order polynomial to the data over the interval shown,
 187 but excluding the intra-D ring data between the middle pairs of blue dashed lines in the figure. These
 188 fits are shown by the red lines in Figures 2a-2d, taken to form an appropriate interpolated baseline
 189 for the measurements in the intra-D ring region. This baseline is subtracted from the azimuthal
 190 magnetic field data to yield the profiles shown in Figures 2e-2h, which are employed to derive the
 191 associated ionospheric meridional current per radian of azimuth at the feet of the field lines, I_m , using
 192 equation (2). We note with Provan et al. (2019) that since the perpendicular distance ρ remains near
 193 $\sim 1 R_s$ on these passes (Figure 1a), equation (2) may be approximated for rough estimates by
 194 $I_m \approx 0.048 B_\phi$ (nT) MA rad⁻¹, though the full formula is employed here. The currents are then
 195 projected to the ionosphere as a function of colatitude from the northern pole, θ_i , using the same field
 196 model as employed in Figure 1. The choice of subsolar magnetopause stand-off distance for the Bunce
 197 et al. (2007) ring current model has a negligible effect (less than 0.1°) on the determined colatitude
 198 as the field model is dominated by the planetary field close to the planet.

199 The field-aligned current density flowing immediately above the ionospheric conducting layer is then
 200 calculated from the meridional current profile using equation (3), and the current density at the
 201 spacecraft using equation (4). Since these quantities require estimation of the gradient of the
 202 meridional current with colatitude, the time series I_m data are first smoothed using a running average
 203 with a window width of 2.5 min, which removes the small-scale fluctuations while preserving the
 204 overall field structure and its gradients. We note that projection of the currents along field lines to
 205 the ionosphere inescapably leaves a “gap” in the ionospheric current profile across the equator
 206 corresponding to field lines that lie “beneath” the spacecraft trajectory that are not crossed during the
 207 pass. These cross-equatorial gaps are $\sim 25^\circ$ wide for passes with larger periapsides such as Rev 287,
 208 decreasing to $\sim 20^\circ$ wide for passes with smaller periapsides such as Rev 288. Small variations in the
 209 smoothed currents near the “ends” of this gap north and south, mapping to increasingly small

210 latitudinal segments of the ionospheric layer, can also lead to sharp unphysical spikes in the estimated
 211 current density at these points. We have therefore imposed an empirically determined limit to the
 212 second derivative with respect to colatitude of the smoothed ionospheric current, related to the rate
 213 of change of the current density with colatitude through equation (3), which eliminates this effect.
 214 Specifically, we impose $d^2 I_m / d\theta_i^2 \leq 0.5$, with I_m in MA rad⁻¹ and θ_i in degrees. This procedure
 215 widens the gap to $\sim 26^\circ$ for passes with larger periapsides, decreasing to $\sim 21^\circ$ for passes with smaller
 216 periapsides.

217 **3. Results**

218 We now present current and current density results as described above for four representative intra-
 219 D ring passes. Provan et al. (2019) have recently suggested a broad division of passes into four
 220 categories, though noting that the data generally display more a continuum of behaviors rather than
 221 completely distinct types. In essentially all cases the field profiles show approximate symmetry about
 222 the magnetic equator, though differing in the number, form, and sign of the peaks in field observed.
 223 In category A, comprising $\sim 35\%$ of the passes (8 out of 23), the azimuthal field forms one central
 224 near-symmetric peak of magnitude $\sim 20\text{-}40$ nT, as indicated in the initial presentations of Dougherty
 225 et al. (2018) and Khurana et al. (2018). In category B, comprising a further $\sim 30\%$ of the passes (7
 226 out of 23), the field has two near-symmetric peaks typically of smaller $\sim 10\text{-}20$ nT magnitude located
 227 near to or just inside of the inner D ring boundary field line, sometimes with a third peak of
 228 comparable magnitude centered near the field-parallel point. In sub-category C, consisting of $\sim 15\%$
 229 of the passes (3 out of 23), the peak fields remain of similar reduced magnitude but show irregular
 230 forms with significant asymmetries about the field-parallel point. Finally, in category U passes,
 231 comprising $\sim 20\%$ of cases (5 out of 23) the fields have a well-defined near-symmetric profile but one
 232 which is unique within the proximal data set, including cases with negative azimuthal fields which
 233 are as strong as the positive fields in category A and B cases. Here we present analyses of data from
 234 category A pass Rev 287, category B passes Revs 273 and 288 with and without strong central

235 maxima, and category U pass 292 which exhibits strong central negative fields. Asymmetric sub-
 236 category C passes are not fully amenable to the analysis outlined above which assumes approximate
 237 axisymmetry, and are not examined further.

238 **3.1. Rev 287**

239 We begin by examining category A pass Rev 287, with results shown in Figure 3. As in Figure 2,
 240 the vertical lines indicate field lines that map to the outer boundary of the A ring, and the outer and
 241 inner boundaries of the D ring. Figure 3a shows the ionospheric meridional current, I_m , positive
 242 northwards, derived from the azimuthal field data in Figure 2e using equation (2), and mapped to the
 243 ionosphere using the model field employed in Figure 1 where it is plotted as a function of colatitude
 244 from the northern pole θ_i . The black line shows the current calculated from the 10 s data, while the
 245 purple line shows the smoothed profile using the 2.5 mins sliding window as described in section 2.2.
 246 It can be seen that the smoothed profile appropriately removes the small-scale fluctuations while
 247 preserving the large-scale features. As indicated above, the central near-equatorial gap in the 10 s
 248 data corresponds to inner field lines not crossed on the spacecraft trajectory. It can be seen that the
 249 current begins to increase to positive values on D ring field lines both north and south, and continues
 250 to increase near-linearly with colatitude in the region inside the D ring, reaching peak values of ~ 1.5
 251 MA rad⁻¹ at the largest colatitudes reached, corresponding to $\sim 71^\circ$ in the northern hemisphere and
 252 $\sim 98^\circ$ in the southern hemisphere. This value is similar to those presented by Dougherty et al. (2018),
 253 Khurana et al. (2018), and Provan et al. (2019). It seems clear from this profile, however, that the
 254 current is still rising strongly with colatitude in the innermost part of the region sampled, with the
 255 actual peak northward current flowing across the equatorial region remaining undetermined. The
 256 truncated rise in azimuthal field values in the central region of the pass seen in Figures 2a and 2e is
 257 thus essentially a geometric effect as the spacecraft moves increasingly tangentially to the field lines.
 258 To assess the degree of north-south symmetry of the current system we have mapped the smoothed
 259 northern current profile into the southern hemisphere along model field lines, shown by the blue line

260 in Figure 3a, and also the southern current profile into the northern hemisphere, shown by red lines.
261 Comparing the red and blue profiles to the purple profiles in each hemisphere, it can be seen that the
262 profiles are closely symmetrical, consistent with an interhemispheric field-aligned current flow. Any
263 small departures from conjugacy could result from temporal, local time, or field model variations.
264 However, the precise origin of these variations are beyond the focus of the present paper which is the
265 currents' strength and density.

266 The positive gradient of the ionospheric current with colatitude in the northern hemisphere is
267 indicative of an upward field-aligned current (flowing away from the ionosphere), while the negative
268 gradient in the southern hemisphere indicates a downward field-aligned current (flowing towards the
269 ionosphere). The corresponding field-aligned current densities just above the ionosphere derived
270 using equation (3) are similarly shown versus northern colatitude in Figure 3b, where it can be seen
271 that the currents rise from small values on central D ring field lines and plateau at positive values ~ 6
272 nA m^{-2} near and just inside the inner D ring boundary in both hemispheres. As indicated in section
273 2.1 and Appendix A, positive values indicate field-aligned current flow in the same direction as the
274 background field in both hemispheres, while negative values indicate current flow opposite to the
275 field direction in both hemispheres. Thus as required by the northward sense of the ionospheric
276 current, the field-aligned currents flow away from the ionosphere in the northern hemisphere where
277 the field points outward, and towards the ionosphere in the southern hemisphere where the field points
278 inward, i.e., a north to south directed current flow along the field lines. The high degree of
279 interhemispheric symmetry is again seen from mapping the northern current density profile along
280 field lines into the southern hemisphere (blue line), and similarly the southern profile along field lines
281 into the northern hemisphere (red lines). However, a further sharp increase in current density is
282 derived from the northern ionospheric current profile near the largest colatitudes reached, not
283 mirrored in the southern profile. This is due to a sudden small change in I_m occurring over a small
284 range of colatitudes close to the edge of the main current.

285 Figure 3c shows the corresponding field-aligned current density local to the spacecraft, $j_{\parallel SC}$, derived
 286 using equation (4), shown as a function of time from the field-parallel point. Due to the low altitude
 287 nature of the pass (radial distance 1.054 R_S at the field-parallel point), the down-scaling of the current
 288 density relative to the ionospheric value resulting from the relative field strengths is seen to be modest,
 289 with values plateauing at $\sim 5 \text{ nA m}^{-2}$ just inside the D ring inner boundary.

290 3.2. Rev 273

291 In Figure 4 we present results for category B pass Rev 273, in the same format as Figure 3. As can
 292 be seen from Figure 2f, the azimuthal field on this pass has two well-defined peaks located just inside
 293 of the inner boundary of the D ring, together with a central field maximum of slightly larger
 294 magnitude. The mapped ionospheric current in Figure 4a correspondingly has two peaks just inside
 295 the inner D ring boundary, $\sim 0.8 \text{ MA rad}^{-1}$ at $\theta_i \approx 72^\circ$ in the northern hemisphere, and moderately
 296 larger at $\sim 1.1 \text{ MA rad}^{-1}$ at $\theta_i \approx 102^\circ$ in the southern ionosphere. The red and blue mapped profiles
 297 show that these two features are closely conjugate, but highlight the north-south difference in
 298 magnitude. The currents then increase once more to peak at $\sim 1.3 \text{ MA rad}^{-1}$ in the inner region. The
 299 strongly rising form of these inner currents again make it clear that the actual peak northward current
 300 flowing across the equatorial region remains undetermined.

301 We note that the reversal in the gradient of I_m across the peaks is indicative of a reversal in the
 302 direction of the field-aligned current from southward in the outer region mapping to the D ring to
 303 northward interior to the peaks. The field-aligned current then reverses sign again to southward as
 304 the meridional current subsequently increases once more towards its central peak. These variations
 305 are clearly seen in Figure 4b, where the ionospheric field-aligned current density initially rises from
 306 small positive values at the outer boundary of the D ring, directed from north to south along the
 307 background field, to a positive peak of $\sim 7\text{-}8 \text{ nA m}^{-2}$ at or near the inner boundary of the D ring field
 308 line. The field-aligned current then near-conjugately reverses to a negative peak $\sim 5 \text{ nA m}^{-2}$ inside of
 309 the inner D ring boundary, directed from south to north opposite to the background field, before

310 reversing once more to a positive north to south value of $\sim 10\text{-}15 \text{ nA m}^{-2}$ in the region of the central
311 maximum. Once again, these features are reproduced in the current density at the spacecraft with
312 only a small reduction in magnitude, as shown in Figure 4c.

313 **3.3. Rev 288**

314 In Figure 5 we show results for category B pass Rev 288, the general form of which is similar to Rev
315 273 in Figure 4. The azimuthal field in Figure 2g again has two positive peaks located just inside the
316 D ring inner boundary field line, though of lesser magnitude than Rev 273 in Figure 2e, interior to
317 which the fields remain smaller and more irregular in form. The ionospheric current in Figure 5a
318 shows corresponding behavior, with near-conjugate peaks of $\sim 0.8 \text{ MA rad}^{-1}$ lying just inside the inner
319 boundary of the D ring, but with variable currents differing north-south in the interior region, as
320 shown by the red and blue mapped profiles. The corresponding ionospheric field-aligned currents in
321 Figure 5b are positive on D ring field lines, rising to near-conjugate peaks of $\sim 5 \text{ nA m}^{-2}$ just outside
322 of the inner boundary of the D ring, before falling non-conjugately to negative values of $\sim -5 \text{ nA m}^{-2}$
323 closer to the boundary in the northern hemisphere than in the southern, as is clear from comparison
324 with the blue and red mapped profiles. The field-aligned currents in the northern hemisphere then
325 show further non-conjugate reversals of a similar magnitude that are not present in the southern
326 hemisphere, associated with a partially-resolved small-scale meridional current (and azimuthal field)
327 structure that is present in the northern hemisphere data but not in the southern (Figure 2g). These
328 results in which field-aligned currents apparently flow in opposite directions along field lines in the
329 northern and southern hemispheres might be taken as evidence of cross-field current flow in the
330 region between. Alternatively, given the overall nature of the phenomenon it seems plausible that
331 they are possibly due to few-minute fluctuations in the fields and currents on the time scale of the
332 pass, or to small-scale azimuthal variations in the currents given the $\sim 1.7 \text{ h}$ increase in LT across the
333 noon meridian that occurred within the intra-D ring region, or to variations in background magnetic
334 field not captured by the planetary field model employed. It is important to note that only one other
335 category B pass (Rev 284) shows a similar non-conjugacy.

336 **3.4. Rev 292**

337 In Figure 6 we show results for one of the more prominent “unique” cases, Rev 292, which exhibits
338 a central negative azimuthal field, peaking near the field-parallel point, whose magnitude is
339 comparable to that of the central positive field peaks of the category A passes. As can be seen in
340 Figure 2h, however, the field perturbations are initially positive starting on D region field lines, before
341 peaking just inside the inner boundary of the D ring, and then falling to negative values in the interior
342 region. A prominent field fluctuation is also seen in the northern hemisphere in the negative field
343 regime, which is only partially marked at the corresponding position in the southern hemisphere.
344 Figure 6a shows the ionospheric meridional current correspondingly rising near-conjugately (shown
345 by the red and blue lines) from small values at the outer boundary of the D ring to positive peaks of
346 $\sim 0.8 \text{ MA rad}^{-1}$ just inside the inner D ring boundary, similar to Figures 4 and 5. However, the current
347 then falls to negative (southward) values reaching $\sim -1.2 \text{ MA rad}^{-1}$ in the interior region. The current
348 remains strongly falling with colatitude in the innermost region sampled, again indicating that the
349 actual peak southward current flowing in the equatorial region, together with the peak negative
350 azimuthal field, remains undetermined. The smaller-scale field fluctuations in the negative field
351 region noted above are also seen to lead to significant inflections in the smoothed ionospheric current
352 profiles in Figure 6a.

353 The field-aligned currents shown in Figure 6b peak at $\sim 5 \text{ nA m}^{-2}$ near to or just outside of the inner
354 boundary of D ring field lines, before falling near-conjugately to strongly negative (northward) values
355 in both hemispheres just inside the inner D ring boundary, with peak values of $\sim -18 \text{ nA m}^{-2}$ in the
356 northern hemisphere and $\sim -10 \text{ nA m}^{-2}$ in the southern hemisphere. The current inflection associated
357 with the small-scale field features (only partially resolved in the northern hemisphere) is associated
358 with the calculated negative current density reducing near to zero near-conjugately in both
359 hemispheres, before resuming comparably large ~ -15 to -20 nA m^{-2} values in the inner field region
360 sampled.

361 **4. Discussion**

362 The analysis in section 3 shows that the integrated currents flowing in the intra-D ring current sheet
 363 are of typical magnitude $\sim 0.5\text{-}1.5 \text{ MA rad}^{-1}$, consistent with the initial estimates of Dougherty et al.
 364 (2018), Khurana et al. (2018), and Provan et al. (2019). As these authors noted, such currents are
 365 comparable in magnitude to those flowing in the main current sheets at auroral latitudes (Hunt et al.,
 366 2014, 2015, 2018a; Bradley et al., 2018). However, as also shown in section 3, the field-aligned
 367 current densities in the intra-D ring layers are typically $\sim 5\text{-}10 \text{ nA m}^{-2}$, more than an order of
 368 magnitude smaller than the auroral current densities of typically $\sim 50\text{-}150 \text{ nA m}^{-2}$ (e.g., Bunce et al.,
 369 2008; Hunt et al., 2014). We now briefly explore the origins of this difference by making some
 370 simple estimates.

371 For these purposes we approximate equation (3) as

$$372 \quad j_{\parallel i}(\theta_i) \approx \frac{1}{R_i^2(\theta_i) \sin \theta_i |\cos \alpha_i(\theta_i)|} \frac{\Delta I_m}{\Delta \theta_i}, \quad (5)$$

373 where ΔI_m is the total current per radian of azimuth flowing in the current sheet, $\Delta \theta_i$ is the
 374 ionospheric latitudinal width of the sheet, θ_i is taken as the center colatitude of the sheet, α_i is the
 375 angle of the ionospheric magnetic field to the ionospheric normal $\alpha_i(\theta_i) = \cos^{-1}(B_{ni}(\theta_i)/B_i(\theta_i))$,
 376 and we note that $n_r(\theta_i)$ in equation (3) is equal to unity to within less than 1% throughout.

377 We first consider the auroral current sheets, focusing specifically on the main upward current sheet
 378 associated with the auroral oval, whose properties observed in the near-midnight southern hemisphere
 379 on a sequence of Cassini orbits in 2008 are summarized in Table 2 of Hunt et al. (2014). Considering
 380 only the mean values in the table, we find $\Delta I_m \approx 2.7 \text{ MA rad}^{-1}$, $\Delta \theta_i \approx 1.7^\circ$, and colatitude from the
 381 southern pole $\theta_{is} \approx 18^\circ$, such that $R_i \approx 55855 \text{ km}$ (equation (A1)), and $|\cos \alpha_i| \approx 0.965$. Substitution
 382 into equation (5) yields $j_{\parallel i} \approx 97 \text{ nA m}^{-2}$ in line with the above comments. The average over the
 383 individual current density estimates given by Hunt et al. (2014) is 128 nA m^{-2} .

384 The results in section 3 then show that a typical equatorial current layer may be taken to be of strength
 385 $\sim 1 \text{ MA rad}^{-1}$, centered near the inner D ring field line boundary mapping in the northern ionosphere
 386 to northern colatitude $\sim 65.5^\circ$, and with a colatitudinal width of $\sim 5^\circ$ (spanning $\sim 1.08\text{-}1.14 R_s$ in the
 387 equatorial plane). The conjugate values in the southern ionosphere are a southern colatitude of
 388 $\sim 74.5^\circ$, with a width of $\sim 5.6^\circ$. The ionospheric radii are $\sim 60113 \text{ km}$ in the north and 60781 km in the
 389 south, with field tilt angle factors $|\cos\alpha_i|$ of 0.444 in the north and 0.456 in the south. From equation
 390 (5), the estimated ionospheric current densities are then $\sim 8 \text{ nA m}^{-2}$ in the north and $\sim 6 \text{ nA m}^{-2}$ in the
 391 south, in line with the results in section 3 shown in Figures 3-6. These simple estimates thus yield
 392 equatorial current densities that are a factor ~ 15 smaller than corresponding auroral values.

393 Examining the terms that lead to this difference, we note that (a) the currents in the auroral sheets are
 394 typically larger than those in the equatorial sheets by a factor of ~ 3 , (b) the ionospheric latitudinal
 395 width of the auroral current layers are smaller than those of the equatorial current layers by a factor
 396 of ~ 3 , and (c) the ionospheric circumferential length per radian in the auroral region is smaller than
 397 that in the equatorial region by a factor of ~ 3 . Thus, the area into which the auroral currents map is
 398 an order of magnitude smaller than the area into which the equatorial currents map, and given the
 399 factor of ~ 3 enhancement of the total auroral current relative to the equatorial, these three factors
 400 would combine to make the auroral current density ~ 30 times the equatorial value. However, this
 401 factor is mitigated by the field tilt angle effect $|\cos\alpha_i|^{-1}$, which is a factor of ~ 2 larger for the
 402 equatorial current than for the auroral, so that the overall value is a factor of ~ 15 .

403 **5. Summary and Conclusions**

404 Following the initial reports of the presence of the intra-D ring azimuthal field perturbations from the
 405 early proximal orbit magnetic field data by Dougherty et al. (2018) and Khurana et al. (2018), and
 406 the first survey of all the proximal data by Provan et al. (2019), in this paper we have examined the
 407 ionospheric meridional currents and related field-aligned current densities associated with the
 408 observed field signatures, assuming approximate local axisymmetry. We have shown (Appendix B)

409 that the latter assumption requires the current structures to be at least ~ 2 h LT wide about the point
410 of field measurement, which should usually be well satisfied given the observed systematics of the
411 field data across ~ 1.5 h LT ranges on each pass, and across ~ 3.5 h LT about noon over the data set as
412 a whole. We find on this basis that the horizontal ionospheric meridional currents are typically ~ 0.5 –
413 1.5 MA rad^{-1} , while the associated field-aligned current densities in the intra-D ring layers are
414 typically ~ 5 – 10 nA m^{-2} . While the integrated meridional currents per radian of azimuth are thus
415 comparable in strength to the auroral region currents, within a factor of ~ 3 , the associated field-
416 aligned current densities just above the equatorial ionosphere are typically more than an order of
417 magnitude lower than the field-aligned current densities just above the auroral ionosphere. We have
418 shown that this is due to four factors, (a) the currents in the auroral layers are typically larger by a factor
419 of ~ 3 , (b) the colatitudinal width of the auroral layers are smaller by a factor ~ 3 , (c) the ionospheric
420 circumferential length per radian in the auroral region is smaller than that in the equatorial region by
421 a factor of ~ 3 , leading overall to a factor of 30, but (d) the field tilt angle effect is a factor of ~ 2 greater
422 in the equatorial region compared to the auroral region leading to larger equatorial current densities
423 than auroral by a factor 2. The combined factor is thus ~ 15 larger for the auroral current densities
424 above the ionosphere than for the near-equatorial. Due to the low altitude of the proximal passes, the
425 field-aligned currents at the spacecraft are similar to those just above the ionosphere.

426 As discussed previously by Provan et al. (2019), while $\sim 35\%$ of the passes (category A) are associated
427 with a consistently northward-directed ionospheric current peaking near the equator, and a
428 consistently southward directed field-aligned current flowing on and inside of D ring field lines as
429 initially described, typically the currents have a more complex structure. In a further 30% of the
430 passes (category B), for example, the field-aligned currents reverse to flow northward with
431 comparable or larger magnitudes in narrower layers on field lines inside of the D ring interior to the
432 outer southward currents, and may or may not reverse sign again on the innermost field lines
433 traversed. In many cases the field and meridional current near the center of the pass peak in such a
434 manner that it is clear that the actual peak fields and currents present on field lines not traversed by

435 the spacecraft could be significantly larger than those determined directly from the data, by factors
436 of at least two, if one extrapolates the I_m profiles to field lines “beyond” the spacecraft (see, e.g.,
437 Figures 3, 4, and 6). The “rounding” of field maxima observed across the equator in these cases is
438 essentially a geometric effect caused by the spacecraft moving near-tangentially along the current-
439 carrying field lines.

440 While in this paper we show two of the final five deepest orbits (Rev 288 and Rev 292 periapsis
441 altitudes at ~ 1700 km above the 1 bar pressure surface); we conclude these signatures do not indicate
442 dipping into the ionospheric current layer containing the south-north return current (I_m in Figure 1b).
443 Our reasoning is as follows; the effect of this would be a reduction in the B_ϕ magnitude, down to zero
444 if the spacecraft fully crossed the layer. It would not produce a reversal in B_ϕ underneath the
445 ionospheric current layer. In addition, Provan et al., (2019) showed the azimuthal field signatures to
446 be independent of periapsis altitude with equally variable signatures in the various altitude ranges
447 (see their Table 1). This includes the category B signatures with a reduction of B_ϕ , these were
448 observed at all altitude ranges. Furthermore, Hadid et al., (2018a) showed the peak electron density
449 to only be encountered on Cassini’s final plunge (Rev 293) at an altitude of ~ 1550 km, some 200 km
450 below the minimum altitude of Revs 288 and 292. Therefore, the peak of the ionospheric current layer
451 was likely below the spacecraft on these Revs too.

452 Generally, the currents show a high degree of north-south conjugacy consistent with the presence of
453 an interhemispheric current system, certainly on the larger overall spatial scales involved. Khurana
454 et al. (2018) have suggested this is driven by thermospheric azimuthal wind shears at the two ends of
455 the field lines threading the intra-D ring region. If so, the overall results discussed above show that
456 these wind shears must be highly variable in nature over the relatively short ~ 1 week pass to pass
457 time scales. The issue of the origin of the pass to pass variability has previously been discussed by
458 Provan et al. (2019), who showed no link could be detected to the altitude of the pass, the LT of the
459 pass (~ 2 h), the phases of the global Saturn planetary period oscillations, or the phase of the prominent

460 asymmetry in Saturn ring structure associated with the D68 ringlet. The physical reason for the
 461 variability thus remains to be elucidated. However, the evidence points towards a significant role for
 462 variability in thermospheric winds, likely in combination with ionospheric conductivities (Hadid et
 463 al., 2018a,b; Wahlund et al., 2018), and possibly influenced by the variable inflow of $\sim 10^4$ kg s⁻¹ of
 464 volatiles and dust into equatorial atmosphere (Hsu et al., 2018; Mitchell et al., 2018; Perry et al.,
 465 2018; Waite et al., 2019). Significant non-conjugacy in the field and current profiles is also often
 466 present on smaller spatial scales. These variations may possibly result from rapid temporal changes
 467 in the currents on the ~ 30 min time scale of each intra-D ring pass. We note that the Alfvén bounce
 468 time is of the order of 4-5s in this region, therefore the time to reach Alfvénic equilibrium is much
 469 less than the time scale of the intra-D ring crossing. Additionally, azimuthal changes in the current
 470 structure over the ~ 1.5 h LT extent of each pass, or variations in background magnetic field not
 471 captured by the field model employed in the ionospheric mapping could result in the variations.

472 **Appendix A: Calculation of Ionospheric Current Density**

473 The field-aligned current density just above the ionosphere associated with the intra-D ring current
 474 system is calculated from the colatitudinal variation of the northward ionospheric current $I_m(\theta_i)$
 475 given by equation (2) assuming axisymmetry. The limitations imposed by the axisymmetric
 476 assumption are explored in Appendix B. The ionosphere is taken to be located at 1000 km above the
 477 1 bar radius, thus at equatorial and polar radii of $R_{ei} = 61,268$ km and $R_{pi} = 55,364$ km, respectively.

478 The ionospheric radial distance at colatitude θ_i is then given by the spheroidal surface

$$479 \quad R_i(\theta_i) = \frac{R_{ei}}{(1 + \varepsilon \cos^2 \theta_i)^{1/2}} \quad , \quad (\text{A1})$$

480 with

$$481 \quad \varepsilon = \left(\frac{R_{ei}}{R_{pi}} \right)^2 - 1 \quad . \quad (\text{A2})$$

482 From current continuity the current density normal to the ionospheric surface $j_{ni}(\theta_i)$, taken positive
 483 directed outward from the surface, satisfies

$$484 \quad j_{ni}(\theta_i)R_i(\theta_i)\sin\theta_i ds = I_m(\theta_i + d\theta_i) - I_m(\theta_i) = dI_m, \quad (\text{A3})$$

485 where $I_m(\theta_i)$ is given by equation (2), ds is the element of length along the ionosphere in the
 486 meridian between θ_i and $\theta_i + d\theta_i$ given by

$$487 \quad ds = \frac{R_i(\theta_i)d\theta_i}{n_r(\theta_i)}, \quad (\text{A4})$$

488 where $n_r(\theta_i)$ is the radial component of the outward unit normal to the surface given by equations
 489 (A1) and (A2). This unit normal is given by

$$490 \quad \hat{n}(\theta_i) = n_r(\theta_i)\hat{r} + n_\theta(\theta_i)\hat{\theta} = \frac{\left[(1 + \varepsilon \cos^2 \theta_i)\hat{r} - (\varepsilon \sin \theta_i \cos \theta_i)\hat{\theta} \right]}{\left[(1 + \varepsilon \cos^2 \theta_i)^2 + (\varepsilon \sin \theta_i \cos \theta_i)^2 \right]^{1/2}}. \quad (\text{A5})$$

491 From equations (A3) and (A4) we then have

$$492 \quad j_{ni}(\theta_i) = \frac{n_r(\theta_i)}{R_i^2(\theta_i)\sin\theta_i} \frac{dI_m}{d\theta_i}. \quad (\text{A6})$$

493 The field-aligned current density just above the ionosphere is then given by

$$494 \quad j_{\parallel i}(\theta_i) = \left(\frac{B_i(\theta_i)}{B_{ni}(\theta_i)} \right) j_{ni}(\theta_i) = \frac{n_r(\theta_i)}{R_i^2(\theta_i)\sin\theta_i} \left(\frac{B_i(\theta_i)}{B_{ni}(\theta_i)} \right) \frac{dI_m}{d\theta_i}, \quad (\text{A7})$$

495 where $B_i(\theta_i)$ is the field strength in the ionosphere, and $B_{ni}(\theta_i)$ is the normal component positive
 496 outwards. We note that with these definitions of $j_{ni}(\theta_i)$ and $B_{ni}(\theta_i)$, both positive outward from
 497 the ionosphere, the field-aligned current density $j_{\parallel i}(\theta_i)$ as defined by equation (A7) is positive when
 498 directed parallel to the ionospheric field and negative when antiparallel, in both hemispheres. From
 499 current continuity, the local field-aligned current density at any other point (r, θ) along these field
 500 lines, including the point of observation, is then given by

$$501 \quad j_{\parallel} = \left(\frac{B(r, \theta)}{B_i(\theta_i)} \right) j_{\parallel i}(\theta_i) \quad , \quad (A8)$$

502 where $j_{\parallel i}(\theta_i)$ and $B_i(\theta_i)$ are the ionospheric field-aligned current density and ionospheric field
 503 strength at the feet of the field line at either end.

504 **Appendix B: Limitations of the Axisymmetric Current Assumption**

505 In this appendix we explore the limitations on the validity of equations (2) and (3) if the current
 506 system illustrated in Figure 1b is not exactly axisymmetric. To do this, we assume instead that the
 507 effective solenoid is of azimuthal length L given approximately by

$$508 \quad L \approx R_s \Delta \varphi \quad , \quad (B1)$$

509 where R_s is Saturn's 1 bar equatorial radius (60,268 km) and $\Delta \varphi$ is the azimuthal extent of the
 510 current system. We first note with Provan et al. (2019) that while the azimuthal field inside the
 511 solenoid may be somewhat variable in magnitude, associated with varying currents, it is nevertheless
 512 (with one exception shown in Figure 2h) generally unidirectional, positive in the sense of planetary
 513 rotation. Then the magnetic flux within the solenoid is given by

$$514 \quad \Phi = \bar{B}_{\varphi} A \approx \bar{B}_{\varphi} Z \Delta \rho \quad (B2)$$

515 where \bar{B}_{φ} is the mean (positive) azimuthal field within cross-sectional area A of the solenoid, the area
 516 being given approximately by the product of Z , the north-south extent of the solenoid, and $\Delta \rho$ its
 517 cylindrical radial width. From Figure 1b it can be seen that we may take $Z \approx 0.4 R_s$ and $\Delta \rho \approx 0.1 R_s$
 518 , given that the flux lies principally interior to the D ring field lines. At the ends of the solenoid,
 519 however, this flux spreads out into the exterior region to close around the solenoid in the usual quasi-
 520 dipolar pattern, in principle extending to infinity, but with the flux being confined principally to
 521 surrounding distances of order $\sim L$, at least above the ionosphere. We thus estimate the perturbation
 522 field strength outside of the solenoid b as

$$523 \quad b \approx \frac{\Phi}{L^2} \approx \frac{\bar{B}_{\varphi} Z \Delta \rho}{L^2} \quad . \quad (B3)$$

524 We then consider applying Ampère's law to the perimeter of a surface whose section in the meridian
 525 is again shown by either the red or blue lines in Figure 1b, but is of finite azimuthal extent $\Delta\varphi$ given
 526 by the azimuthal extent of the solenoidal current. We take the azimuthal field within the solenoid,
 527 i.e., at the small black circle in Figure 1b, to have some particular value B_φ , related to the mean field
 528 \bar{B}_φ by $B_\varphi = f\bar{B}_\varphi$, where over most of the area $f \sim 1$. The contribution to the line integral of \mathbf{B} on the
 529 circular segment inside the solenoid is $\mathcal{J}_1 \approx B_\varphi L$, while now in general we also have equal
 530 contributions from the two field-aligned portions of the path on either side of the solenoid of length
 531 $\Delta z \approx Z/2$, which will thus sum to be of order $\mathcal{J}_2 \approx 2b\Delta z \approx bZ$. The net contributions from inside the
 532 planet remain zero. For a given current per radian of azimuth within the azimuthal sector $\Delta\varphi$, the
 533 validity of equation (2) thus requires that \mathcal{J}_1 is large compared with \mathcal{J}_2 , i.e., we require $B_\varphi L > bZ$.
 534 Introducing b from equation (B3) then gives the geometric condition

$$535 \quad L^3 \gg \frac{Z^2 \Delta \rho}{f}, \quad (\text{B4})$$

536 i.e., the length L must be sufficiently large compared with the transverse dimensions of the solenoid,
 537 or

$$538 \quad L > \sqrt[3]{\frac{Z^2 \Delta \rho}{f}}. \quad (\text{B5})$$

539 We note that if L exceeds the right-hand side of equation (B5) by at least a factor of two, this is
 540 sufficient to give at least an order of magnitude difference in the condition in equation (B4), given
 541 the cubic power on the left side. Since $\sqrt[3]{f}$ will generally be close to unity over nearly all of the area
 542 of interest, it is sufficient to consider $f = 1$ in equation (B5). Introducing the dimensions for Z and
 543 $\Delta\rho$ given above into equation (B4) then gives $\sqrt[3]{Z^2 \Delta\rho} \approx 0.25 R_S$. Thus, as a simple estimate we
 544 require $L \geq 0.5 R_S$ as a lower bound for the approximate validity of equation (2). This corresponds
 545 to $\sim 30^\circ$ of longitude around the planet, or ~ 2 h of LT. We know from direct observation on individual
 546 passes that the effective length of the solenoid is generally at least ~ 1.5 h, while over the proximal
 547 orbits as a whole, such field structures have been directly observed over ~ 3.5 h of LT, from ~ 10 h

548 pre-noon to ~13.5 h LT post noon. It thus seems entirely plausible that conditions under which
549 equation (2) is valid are generally maintained in the Saturn system.

550 **Acknowledgements.** Work at Imperial College was supported by STFC grant ST/N000692/1. Work
551 at the University of Leicester was supported by STFC grant ST/N000749/1. EJB is supported by a
552 Royal Society Wolfson Research Merit Award. MKD is funded by Royal Society Research
553 Professorship RP140004. H.C. is funded by the Cassini project through NASA Jet Propulsion
554 Laboratory (JPL) contract 1579625. We thank Steve Kellock and the Cassini magnetometer team at
555 Imperial College for access to processed magnetic field data. Calibrated magnetic field data from the
556 Cassini mission are available from the NASA Planetary Data System at the Jet Propulsion Laboratory
557 (<https://pds.jpl.nasa.gov/>).

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635 **Figure Captions**

636 **Figure 1.** Plots of Saturn inner field line regimes in a meridian plane in cylindrical (ρ, z)
637 coordinates, where ρ is the perpendicular distance from the spin/magnetic axis and z is distance along
638 the axis positive northward. The outer edge of the planetary body (orange spheroid) is taken to be
639 the main conducting ionospheric layer 1000 km above the 1 bar reference spheroid, while the arrowed
640 black lines show model field lines derived using the first 3 terms of the Dougherty et al. (2018)
641 planetary field model plus the Bunce et al. (2007) ring current model for a typical subsolar
642 magnetopause radius of 22 R_s . The darker blue areas indicate field lines passing through the main
643 ring region in the planet's equatorial plane (black dotted line), bounded by the field line passing
644 through the outer boundary of the A ring. The lighter blue area corresponds to field lines passing
645 through the innermost D ring. In Figure 1a polar field lines have been drawn at 5° colatitude intervals
646 from the southern pole between 0° and 30° , together with their northern conjugate counterparts, while
647 the purple areas indicate the approximate conjugate locations of the main auroral field-aligned
648 currents in both hemispheres. Cassini trajectories for Revs 287 (blue) and 288 (red) are shown
649 projected into the meridian, representative of those with larger and smaller proximal periapsides.
650 Spacecraft motion is from north to south. Small solid circles just north of the equator indicate the
651 field-parallel points where the trajectories in the meridian lie tangent to the field lines, corresponding
652 to the points where they attain maximum mapped colatitudes (minimum mapped latitudes) in the
653 ionosphere, while small open circles located south of the equator indicate the periapsis points. Figure
654 1b shows the region containing the D ring field lines in the same format but on an expanded scale.
655 Arrowed green lines show the intra-D ring current system envisaged, consisting of a variable
656 meridional ionospheric current, I_m , positive northward as shown, closed by an outer field-aligned
657 current, j_{\parallel} , positive southward along the background field as shown, resulting in an interior positive
658 azimuthal perturbation field B_{φ} . The blue and red lines show cuts in the meridian through surfaces
659 of revolution about the z axis that are employed in section 2.1 in the application of Ampère's circuital

660 law to the observation of azimuthal field B_ϕ at the arbitrary intra-D ring point shown by the solid
 661 black circle. The solid portions of these lines follow field lines from the observation point to the
 662 conducting layer of the ionosphere, while the dashed portions complete the surface in some arbitrary
 663 manner through the body of the planet.

664 **Figure 2.** Plots showing the azimuthal field profiles of four representative proximal periapsis passes
 665 examined in detail in section 3, namely category A pass 287, category B passes 273 and 288, and
 666 category U pass 292. Figures 2a-2d show the field as measured over a ± 40 min interval centered on
 667 the field-parallel point (vertical black dotted line) taken as $t = 0$, while Figures 2e-2h show the field
 668 with baseline removed. The baseline is formed from a fourth order polynomial fit to the data in
 669 Figures 2a-2d excluding the intra-D ring data. The UT times of the field parallel points are 17:18.5
 670 UT (h:min) on day 219 for Rev 287, 06:12.3 UT on day 129 for Rev 273, 04:18.2 UT on day 226 for
 671 Rev 288, and for 00:04.7 UT on day 252 Rev 292 (all 2017). The vertical lines indicate field lines
 672 passing through the equatorial plane at ring boundaries. The outer pair of red dashed lines correspond
 673 to the outer boundary of the A ring, while the inner pair of blue lines correspond to the outer (solid)
 674 and inner (dashed) D ring boundaries.

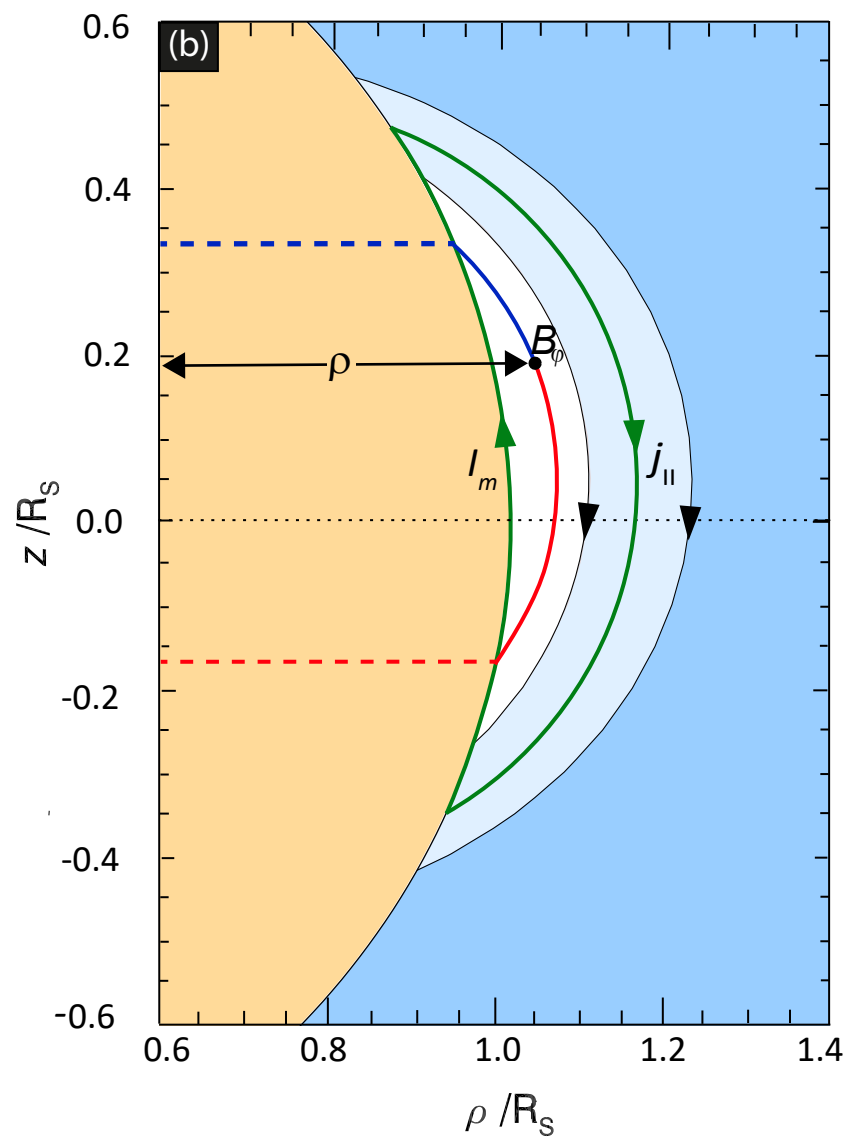
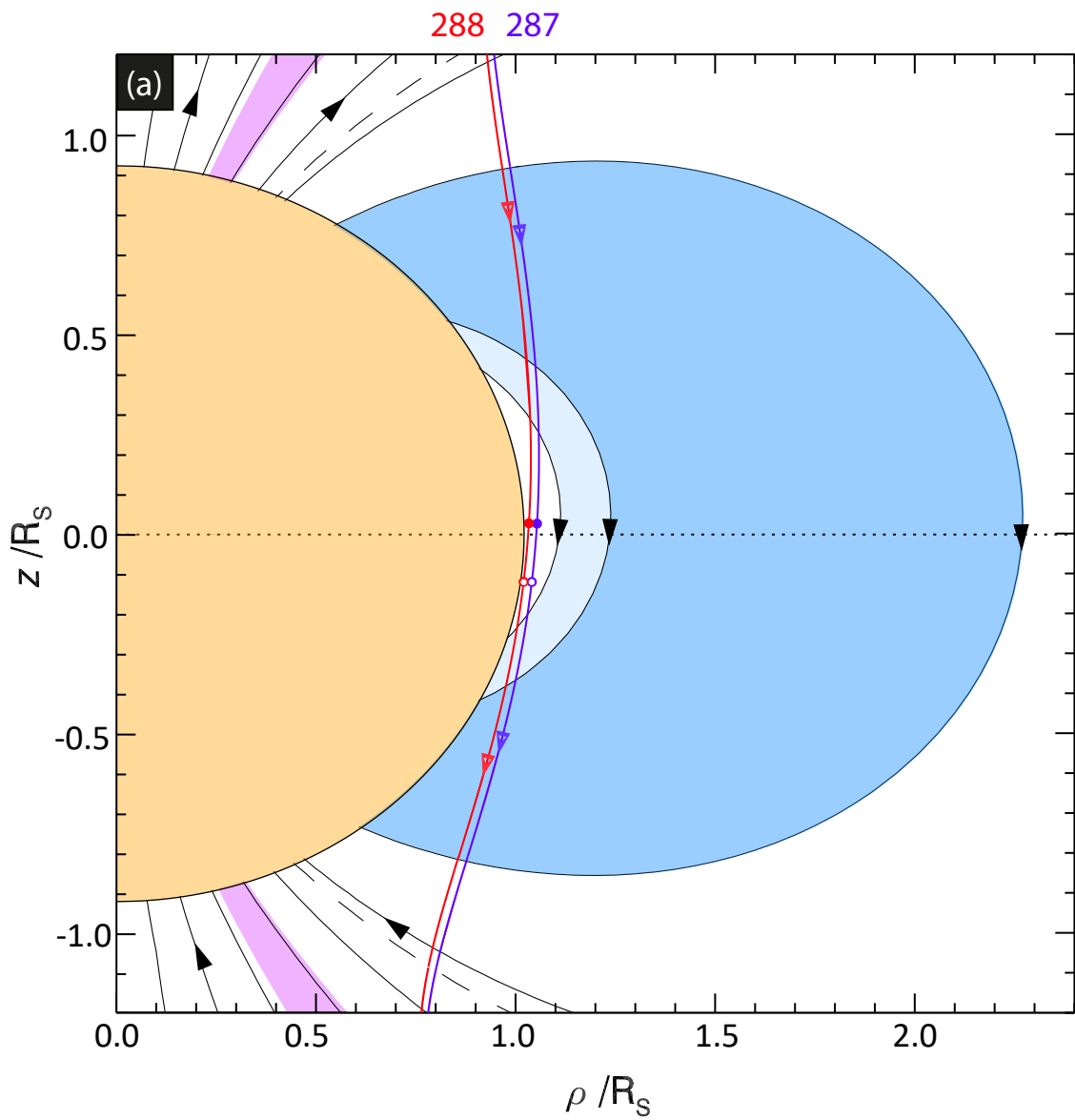
675 **Figure 3.** Ionospheric current per radian of azimuth and field-aligned current density profiles derived
 676 from the azimuthal magnetic field data shown in Figure 2e for category A Rev 287. As in Figure 2,
 677 the vertical lines indicate the locations/times where the magnetic field lines map to the outer edge of
 678 the A ring (red dashed lines), and the outer (blue solid lines) and inner (blue dashed lines) edges of
 679 the D ring. Figure 3a shows the ionospheric meridional current, I_m (MA rad⁻¹), positive northward,
 680 plotted versus ionospheric colatitude, θ_i (deg), measured from the northern pole. The black line
 681 shows the value calculated directly from the 10 s field data using equation (2), while the purple line
 682 shows the smoothed profile using a sliding 2.5 min window. The blue and red lines show the northern
 683 profile mapped along field lines into the southern hemisphere, and the southern profile mapped along
 684 field lines to the northern hemisphere, respectively. In Figure 3b the black line shows the field-

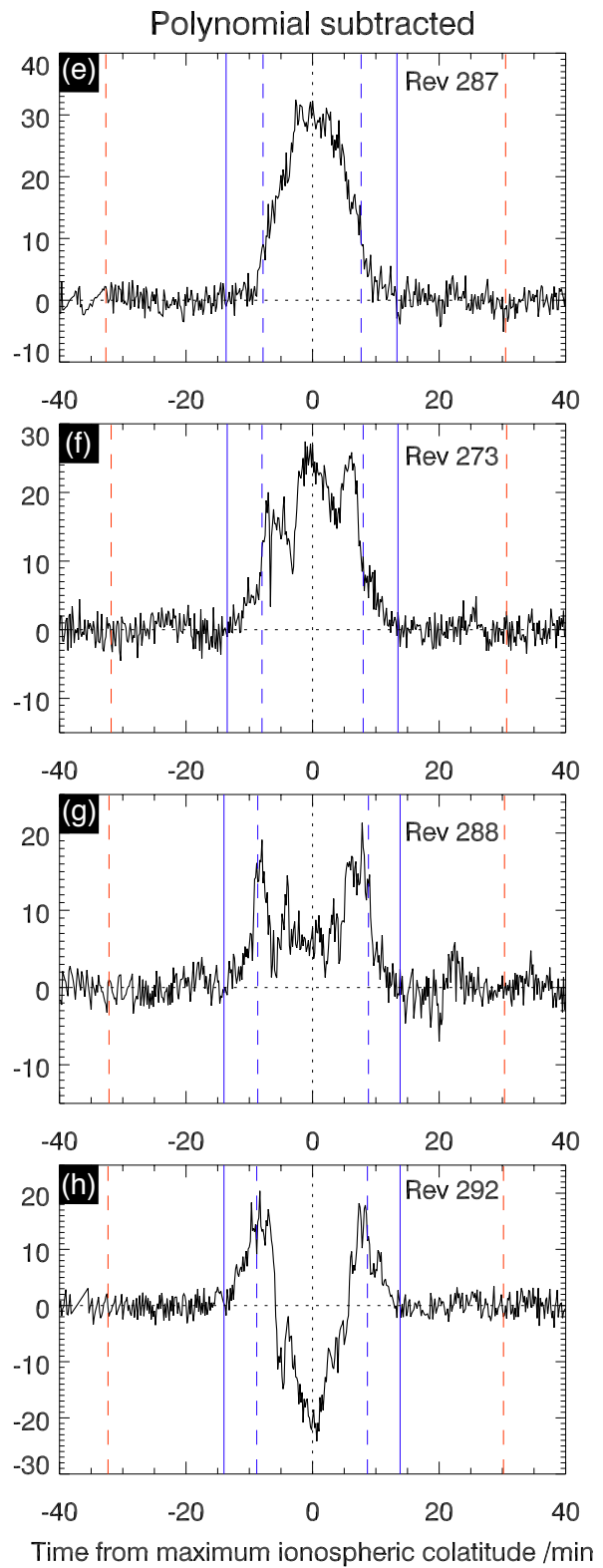
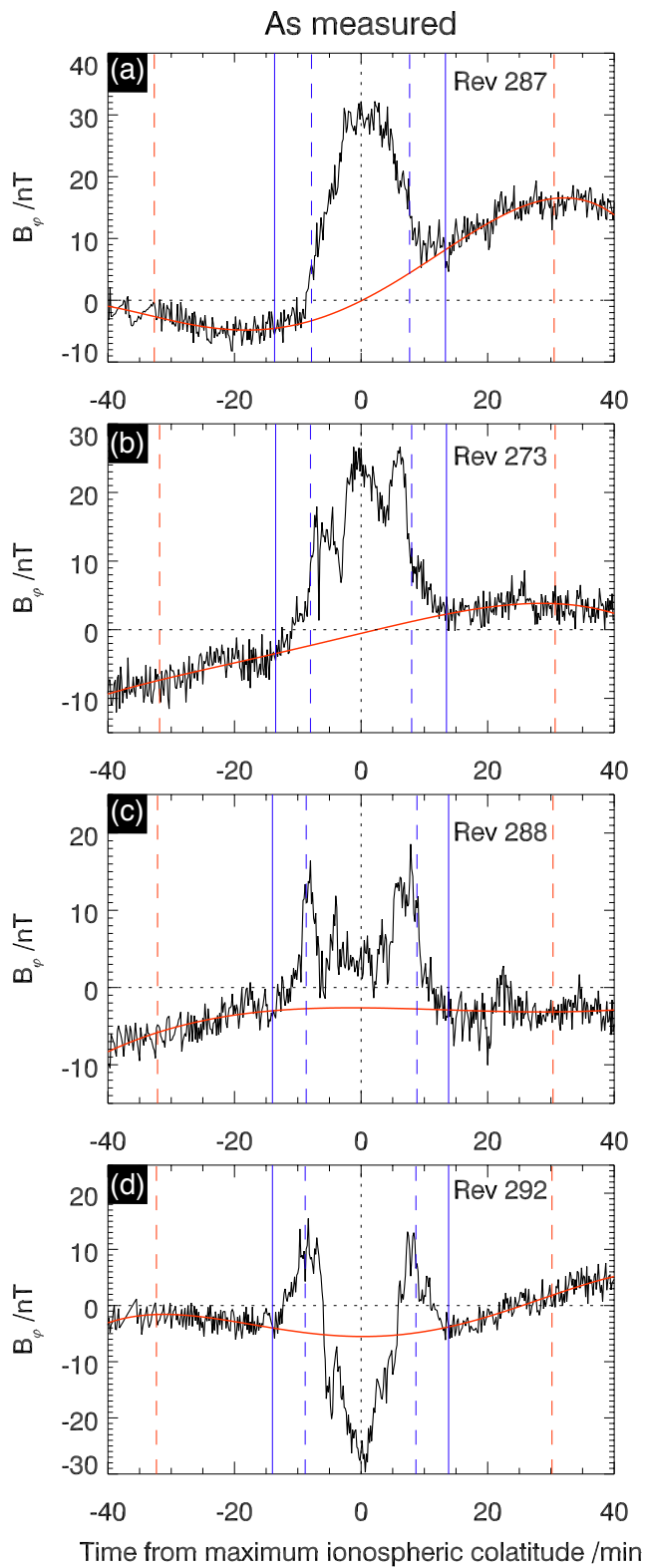
685 aligned current density just above the conducting layer of the ionosphere, positive along the
686 background field direction, calculated from the gradient of the smoothed ionospheric current profile
687 using equation (3). The blue line shows the northern current density profile mapped along field lines
688 into the southern hemisphere, while the red line shows the southern current density profile mapped
689 into the northern hemisphere. Figure 3c shows the current density local to the spacecraft as a function
690 of time relative to the field-parallel point.

691 **Figure 4.** Ionospheric current and field-aligned current density profiles derived from the azimuthal
692 magnetic field data shown in Figure 2f for category B Rev 273. The format is the same Figure 3.

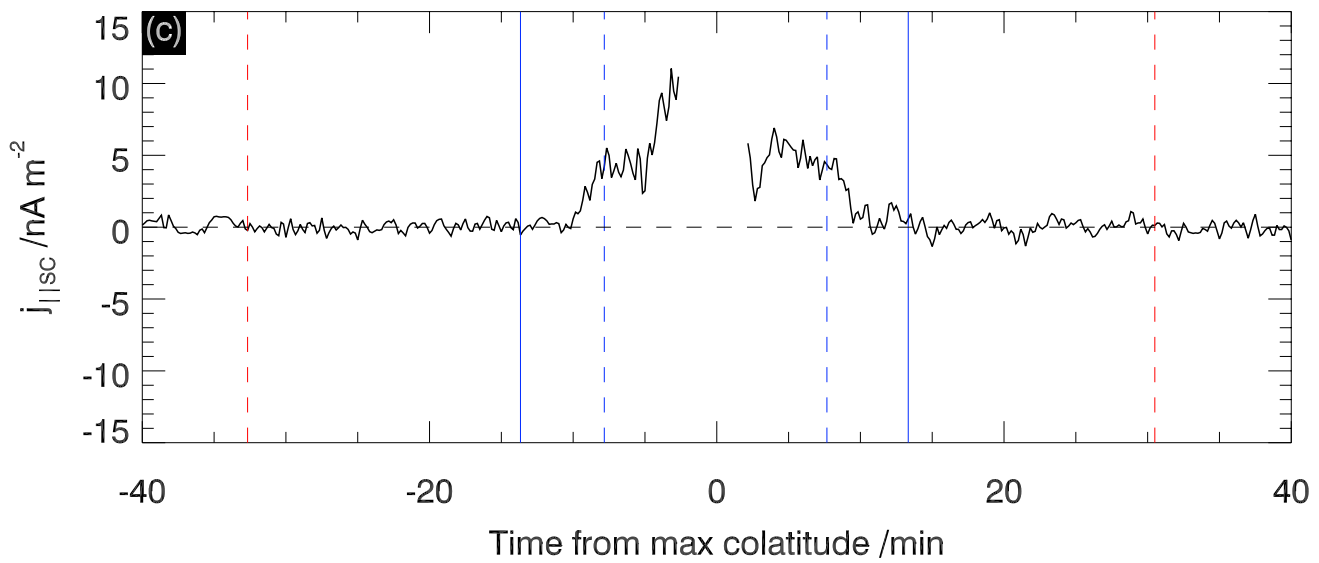
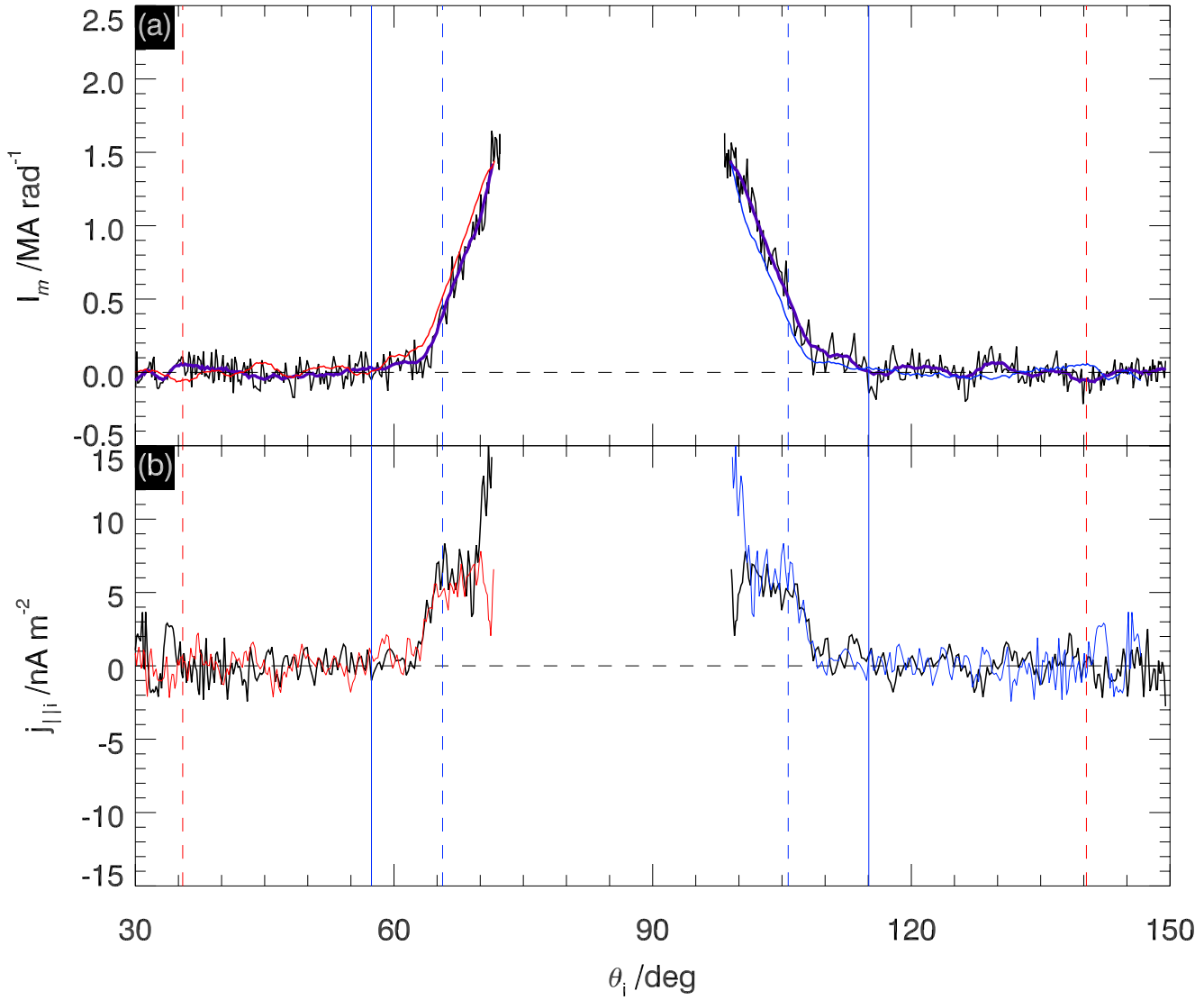
693 **Figure 5.** Ionospheric current and field-aligned current density profiles derived from the azimuthal
694 magnetic field data shown in Figure 2g for category B Rev 288. The format is the same Figure 3.

695 **Figure 6.** Ionospheric current and field-aligned current density profiles derived from the azimuthal
696 magnetic field data shown in Figure 2h for category U Rev 292. The format is the same Figure 3.

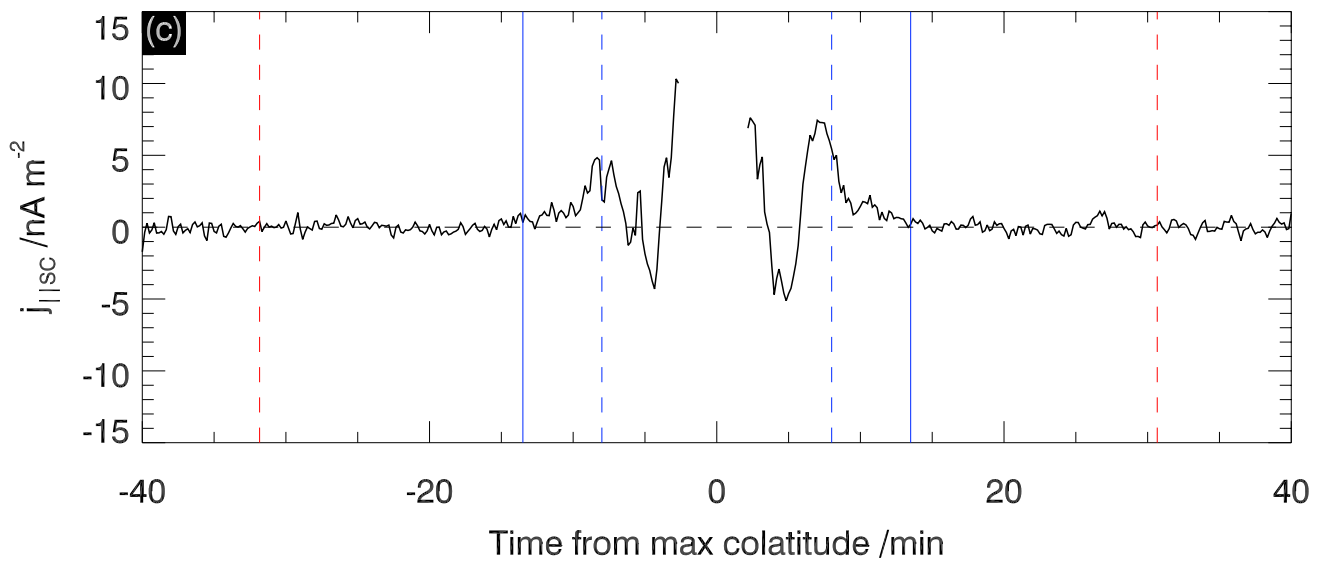
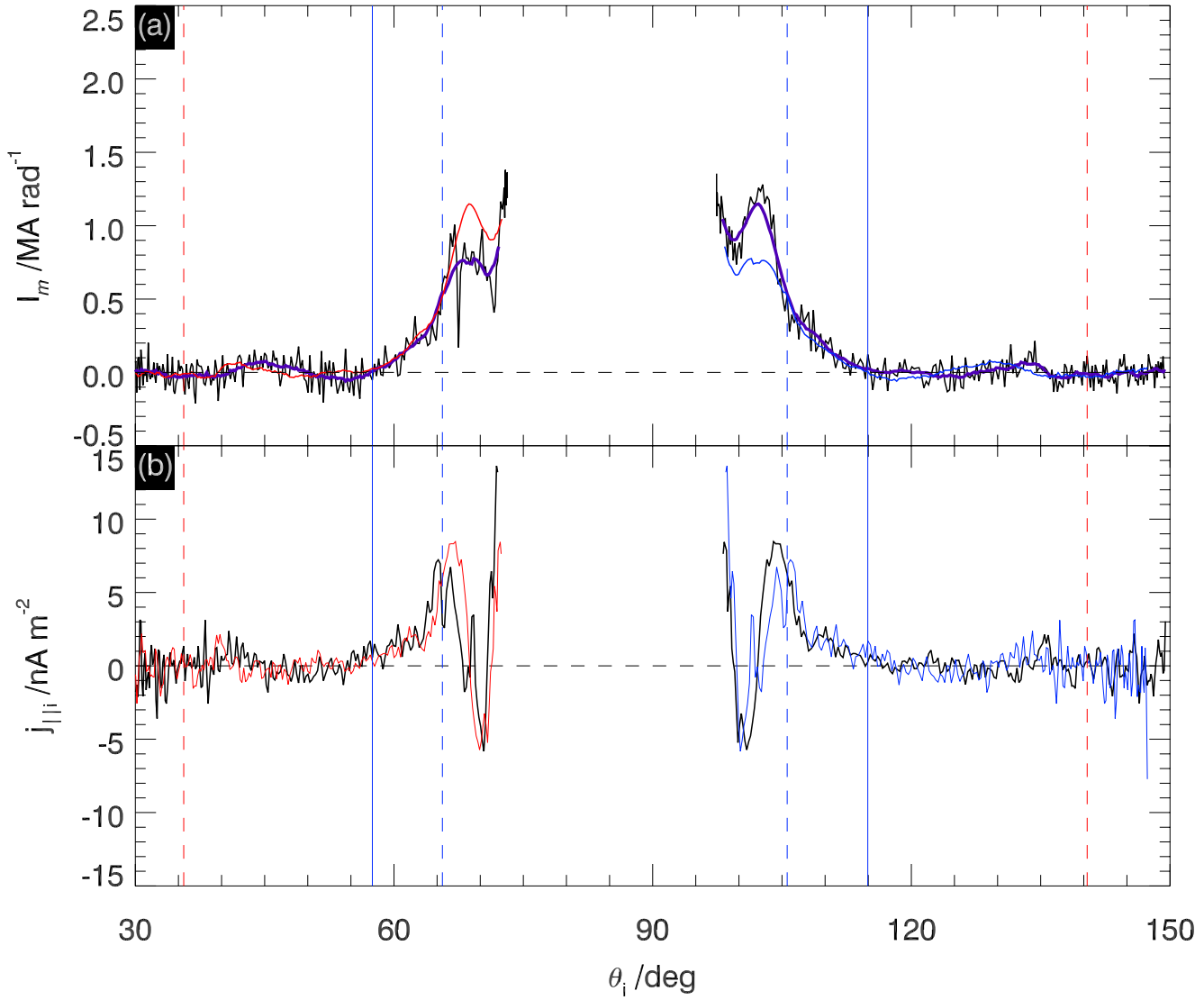




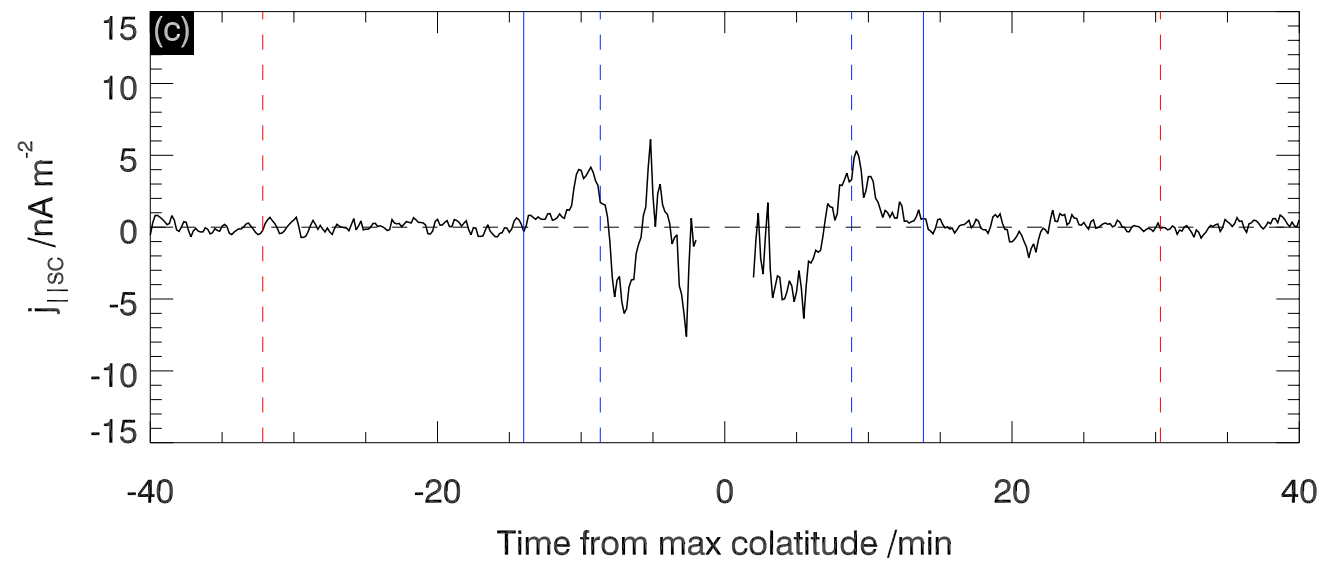
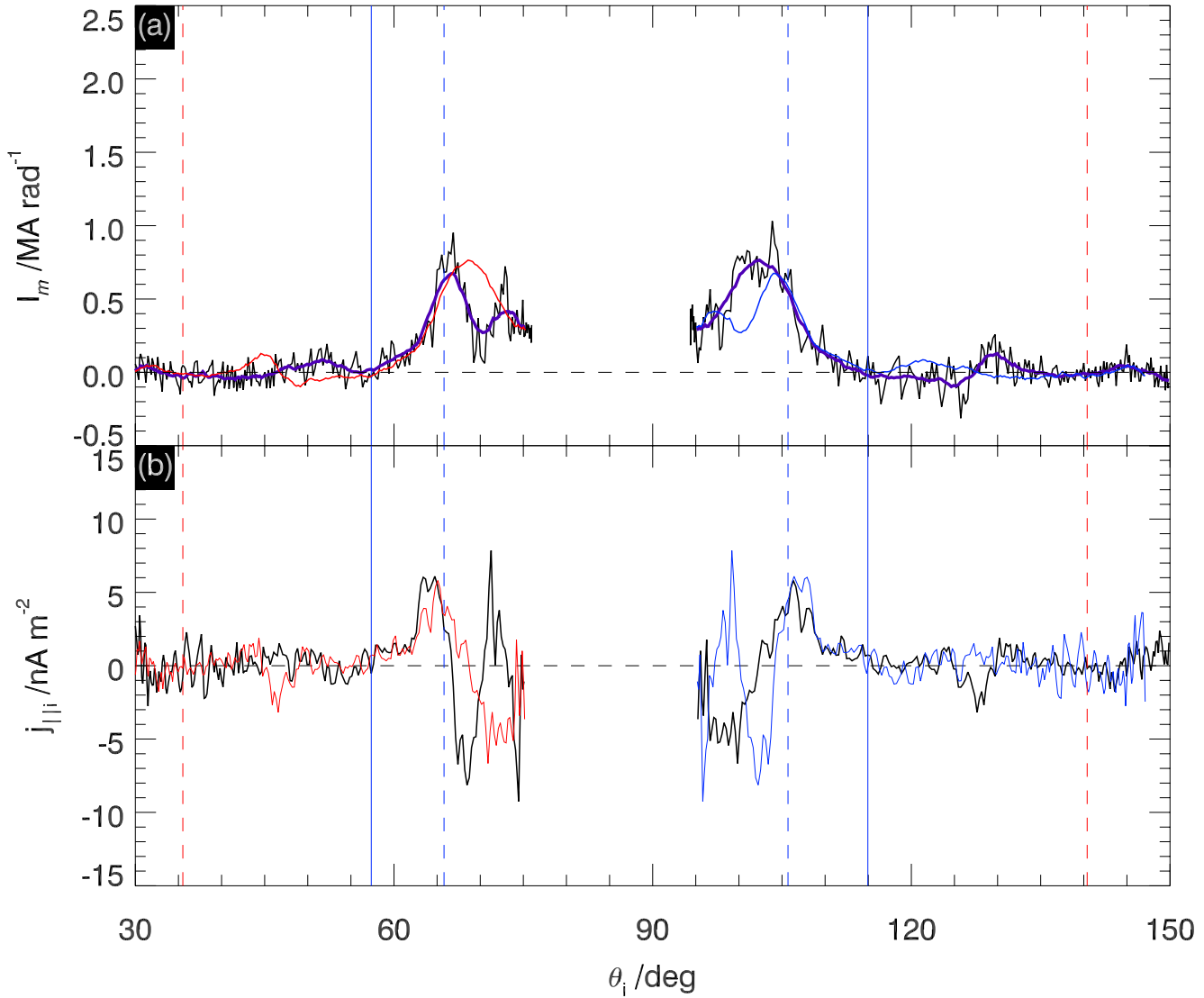
Rev 287



Rev 273



Rev 288



Rev 292

