Thermodynamic and thermal comfort optimisation of a coastal social house considering the influence of the thermal breeze

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Abstract

Tropical coastal areas are characterised by high levels of wind and solar resources with large potentials to be utilised for low-energy building design. This paper presents a multi-objective optimisation framework capable of evaluating cost-efficient and low-exergy coastal building designs considering the influence of the thermal breeze. An integrated dynamic simulation tool has been enhanced to consider the impacts of the sea-land breeze effect, aiming at potentiating natural cross-ventilation to improve occupant’s thermal comfort and reduce cooling energy demand. Furthermore, the technological database considers a wide range of active and passive energy conservation measures. As a case study, a two-storey/two-flat detached social house located in the North-Pacific coast of Mexico has been investigated. The optimisation problem has considered the minimisation of: i. annual exergy consumption, ii. life cycle cost, and iii. thermal discomfort. Optimisation results have shown that adequate building orientation and window opening control to optimise the effects of the thermal breeze, combined with other passive and active strategies such as solar shading devices, an improved envelope’s physical characteristics, and solar assisted air source heat pumps have provided the best performance under a limited budget. Compared to the baseline design, the closest to utopia design has increased thermal comfort by 93.8% and reduced exergy consumption by 10.3% whilst increasing the life cycle cost over the next 50 years by 18.5% (from US$39,864 to US$47,246). The importance of renewable generation incentives is further discussed as a counter effect measure for capital cost increase as well as unlocking currently high-cost low-exergy technologies.

Keywords: low-energy building, optimisation, solar design, exergy analysis, thermal breeze, thermal comfort

1. Introduction

Due to natural resource availability in coastal areas, the regional population and infrastructure are experiencing high growth rates, causing substantial socio-economic and environmental changes.

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This has generated an increase in demand for affordable housing. On average, population densities in coastal cities are found to be three times higher compared to the world’s average [1]. Currently, it is estimated that 23% of the world’s population lives within 100 km distance of the coast and under 100 m above sea-level [2]. It is in these geographical locations where the sea-land breeze phenomena is mostly available.

In most developing economies, lack of appropriate building codes have caused housing designs to have poor energy and environmental performance [3]. However, most notorious have been the limited considerations for occupant’s comfort which in turn has caused a wide range of health issues [4]. As income and population increases, the demand for comfort levels and healthier environments also increases [5]. Both, poor building designs and increase in household income could be considered as the main drivers for high growth rates in energy demand in the building sector [6]. This has been exacerbated in hot and humid climates, where poor designs have led to the widespread installation of oversized artificial air conditioners (AC), usually considered by practitioners as the only measure to provide occupants with comfortable thermal conditions. As a result, artificial space cooling is the fastest growing energy service in the building sector. Global energy demand from AC is expected to triple by 2050, contributing 21% of the total increase in final electricity demand [7]. Reducing future building energy use, especially cooling and heating demands, would play a fundamental role to achieve emissions targets and limit global warming to well below 2 °C [8].

To tackle poor energy performance of social housing and its dependency on high quality energy sources (electricity, natural gas), policies and regulatory shifts are necessary to improve cross-sectoral efficiency. Giannetti et al. [9] demonstrated the importance of using local resources in the development of sustainable social housing. A bioclimatic-oriented design and the utilisation of local available resources (local materials as well as solar and wind resources) should be encouraged at the early design stage, aiming at maximising the sustainability of the national social house stock. Smart architectural design, improved envelope characteristics, and efficient passive and active systems could be essential to reducing the impact of mechanical cooling in coastal social housing, allowing low-income families to improve indoor environmental quality (IEQ) and reduce energy bills.

McCabe et al. [10] provided a systematic review of the potential of using low-energy architectural designs and renewable-based technologies for social housing. The authors demonstrated that the major historical barrier for its wider implementation has been the lack of appropriate tenant engagement and the over-complication of technological information. On the other hand, perceived economic benefits have the potential to act as the main motivational factor to installing renewable technologies in low-income houses. However, passive energy designs and optimal use of renewable energy technologies in the coast is more difficult, especially when the building faces the opposite direction to solar energy. Usually, it is necessary to find design trade-offs between improved thermal and visual comfort as well as optimal solar energy harvesting throughout the year. For example, studies focusing on the advantages of incorporating bioclimatic strategies in coastal housing have demonstrated that compared to active-oriented designs, optimal passive designs have improved IEQ and energy performance at lower capital and operational costs [11, 12]. On the contrary, Lebassi et al. [13] found that extensive installation of photovoltaic (PV) rooftops in coastal regions with hot climates have led to a positive thermal storage effect, increasing the Urban Heat Island (UHI)
effect by up to 0.2 °C.

1.1. The sea-land breeze effect and natural ventilation

Natural ventilation in buildings can be considered one of the most common bioclimatic strategies, with high energy efficiency potential in coastal buildings. Optimal utilisation of the thermal (sea-land) breeze can be found in vernacular architecture [11, 14], with limited incorporation in contemporary designs. However, in recent years, due to the expansion of offshore wind energy projects [15–17], knowledge on the onshore/offshore environment and coastal wind behaviour has substantially improved. Additionally, studies on wave energy resources [18], atmospheric research [19], air pollution transport and diffusion [20, 21] and island precipitation [22] have also contributed to the area. This has provided building energy researchers with a renewed awareness of understanding the thermal breeze behaviour, focusing on best ways of incorporating it into contemporary low-energy building designs [23].

Generally, the thermal breeze effect can be explained as follows: 1) during the day, land (which has a lower heat capacity than the sea) heats up quicker (heat island effect). As the air is heated up by conduction and rises due to its lower density, it starts to warm up the ‘land’s air’ upper layers by convection. At the sea, as the amount of heat at surface level is much lower, the air is denser, and therefore, it does not rise. As the air over the land escapes the surface, it generates a pressure gradient (lower pressure is created), and at the sea, the lack of rising air creates higher surface pressure relative to the land. Thus, thermal circulation of warm air from the land towards the sea is generated. 2) To make up for the air that escaped from the land, the high pressure ‘colder’ air from the sea flows towards it. This is considered as the ‘sea breeze’ effect. At night, the opposite effect occurs. As land cools faster than sea due to their difference in heat capacities, cool air sinks over the land, while warm air rises over the sea, causing the air to flow from the land to the sea. This is considered as the ‘land breeze’ effect. Figure 1 illustrates the entire phenomenon.

Figure 1: Sea-land breeze effect. On the left, the direction of the wind. On the right, atmospheric pressure at different altitudes (pressure decreases with increasing altitude)
In the built environment, an important research area that constantly studies the implications of thermal breezes is the UHI effect. UHI can cause micro-climate alterations [24], becoming a major concern for population’s health and building energy use [25], especially in large dense cities [26]. Ichinose et al. [27] studied the interactions between the sea breeze and the UHI in Tokyo, Japan. In Tokyo, hot water infrastructure for commercial buildings is considered the largest contributor of anthropogenic heat. The authors found that the sea breeze variation throughout the year causes different heat fluxes rates, with a higher UHI effect during the winter, due to a weaker sea breeze from the Tokyo Bay combined with higher hot water demands from buildings.

The cooling effect that the sea-land breeze has on mitigating high temperatures and improving human thermal comfort has been demonstrated [28–31]. Recently, Xie et al. [32] studied the convective heat transfer rate on vertical surfaces in island-reef buildings. The optimal rate has been found at 21.5 W/m² K⁻¹ under low-wind velocities, laying a solid foundation for the design of low-energy buildings in coastal areas. Locations close to large water bodies have the capacity to increase the cooling breeze effect. In coastal cities, many buildings, especially those located seaside, are designed with large windows facing the ocean to take advantage of the cooling sea breezes, avoiding heat storage during the day. At night, ventilation cools down the thermal mass, avoiding heat release during the day and therefore limiting over-utilisation of artificial cooling. Faggianelli et al. [33] investigated the use of thermal breezes to improve natural ventilation in houses located on the Mediterranean coast. To avoid complex modelling, the authors used a statistical wind rose supported by tracer gas measurements to investigate the implication of breezes in natural cross-ventilation flow rates. Outputs demonstrated that the best way of controlling air flow is by optimising building orientation and window opening angles, suggesting that minimal control on windows openings is necessary to maintain an airflow within comfortable conditions. However, the challenge is to detect optimal opening angles in real time, something that could be supported by building automation systems for ventilative cooling [34].

Bullen [35] investigated the design of coastal low-cost low-energy housing at a high wind speed location (Orkney Islands, Scotland). The main focus was to study the effects of sea breezes in cold climates. The author provided designs that minimise the exposure effects of high-wind and heavy-rain conditions while also considering building orientation, envelope thermal efficiency, solar gains, ‘heating, ventilation and air conditioning’ (HVAC) system efficiency, and draught-proofing. The final low-energy house design with improved thermal comfort conditions increased capital costs by 7.2% compared to a typical house in the region. Lebassi et al. [36] investigated how climatic variations in coastal California in the last thirty years have had an impact on degree-days and subsequently building energy demand. It was found that in coastal cities and near inland regions, cooling needs have asymmetrically increased in the last decades, reducing cooling degree-days (CDD) on the coast and increasing in inland regions. This has been mainly attributed to the sea breeze intensification, suggesting an increase in cold marine air, providing lower temperatures to coastal areas, thus reducing peak temperatures. Later, to understand this temperature asymmetry in the area, Lebassi et al. [13] investigated the environmental sustainability and thermodynamic implications of solar PV technologies, where large number of panels have been installed. Results showed that the large-scale presence of solar technologies have caused an increase in temperatures due to a net positive thermal storage effect. The authors discovered that this additional heat is being pushed inland as the sea breeze develops, warming further inland areas. Then, as the warmer
wind converges with the downwind from the hills, it produces additional hot spots inland. This effect have major implications for building adaptability, as current HVAC systems could become oversized/undersized, either increasing electricity demand or reducing occupant’s thermal comfort, especially in the hottest months [37].

However, the implications of the sea-land breeze at the coast also depends on other physical site conditions, such as location, terrain size, and particular surrounding characteristics [38]. For example, Rajagopalan et al. [39] examined the effect of the urban geometry of Muar, Malaysia on the city’s wind flow. The unplanned development of the city (a combination of tall buildings with narrow streets) has reduced sea-land breeze air flows, increasing temperatures inside buildings at city level. A step-up configuration has been recommended to allow wind flows to reach deeper into the land. In this sense, computational fluid dynamics (CFD) and robust thermodynamic analysis are essential methods to gain a deeper understanding of the patterns and effects of thermal breezes.

1.2. Building thermodynamic analysis

Exergy is a concept that arises from the first law (energy conservation) and second law (entropy generation) of thermodynamics. According to Szargut [40], exergy can be defined as the amount of work obtainable when some matter is brought to a state of thermodynamic equilibrium with the common components of its surrounding nature by means of reversible processes. Exergy can be a useful tool in explaining sustainability of different energy sources and technologies [41]. Its implementation overcomes the limitations of the first law of thermodynamics by indicating locations, causes, and magnitudes of energy degradation (irreversibilities or exergy destructions), able to calculate meaningful efficiencies [42]. Consequently, exergy analysis is a method widely used for process systems and power plant design and optimisation [43]. In energy systems design, exergy analysis does not have to be seen as a replacement of typical energy analysis, but instead as a supplement, as a more efficient system can be achieved when exergy consumption and avoidable losses are minimised [44].

The majority of exergy related research that was dedicated to improving energy performance in an urban context has been applied to large scale systems, especially for district heating and neighbourhood-scale networks [45–47]. Nevertheless, exergy as a concept is becoming more popular among building energy researchers, and most importantly, among policy makers and practitioners [48, 49]. The studies from Shukuya [50] and Nieuwlaar and Dijk [51] describing the exergy-entropy process of building energy systems can be regarded as pioneers in the building energy research area. Shukuya’s approach suggests that passive designs and not active systems are a prerequisite to realise exergy efficient systems. Other researchers, such as Meggers et al. [52], consider passive design too restrictive, suggesting that well-balanced designs between active and passive systems provide more design flexibility without compromising on exergy performance. Following, Meggers et al. [53] demonstrated that his hybrid approach provides better results in tropical climates by designing high-efficiency and high-temperature cooling systems. Also, thermal comfort has been studied using exergy. Assuming that thermal comfort is related to a minimum of exergy consumption, Schweiker and Shukuya [54] compared an exergetic comfort model (human body exergy consumption (HBx-) rate) with the established adaptive comfort model and predicted mean vote (PMV) model, finding a linear relation between adaptive and exergetic model under neutral conditions. A review on the most recent building exergy literature can be found in Hepbasli [55] and
The biggest limitation of using exergy analysis is concerning the selection of the reference temperature. The main difference with other research areas is that buildings’ systems work very close (thermodynamically speaking) to the reference environment. Several authors have discussed whether static or dynamic temperatures provide more realistic outcomes. The IEA-Annex 49 [57], one of the most comprehensive research studies concerning exergy in buildings, suggest that a quasi-steady-state approach is suitable if storage systems are not considered. If the storage effect is considered then a dynamic analysis is necessary. Angelotti et al. [58] developed a dynamic method accounting for storage processes, requiring hourly temperature data for its assessment. The author compared the dynamic method against a steady-state method by analysing a reversible air source heat pump (ASHP). It was concluded that although the dynamic method is more complex and time consuming, it provides a more comprehensive assessment, especially if cooling exergy is accounted for and the difference between internal and external temperature conditions are not greater than 10 K.

Choi et al. [59] presented a methodology for unsteady-state exergy analysis deriving energy, entropy and exergy governing equations to tackle transient heat conduction problems. The authors verified the method against steady-state and transient processes, providing exergetic behaviour that is not possible to capture with steady-state analysis. On the other hand, Pons [60] argues that a time-dependent dynamic reference environment might not be suitable as it could be biased to the fluctuations in ambient temperatures. Therefore, he suggests a static dead-state reference temperature to reduce uncertainties, demonstrating its applicability for both cooling and heating exergy demand. Li et al. [61], proposed to examine exergy flows based on "cool" and "warm" exergy using heat pumps as case study. This method allows to differentiate between exergy sources, tracking them throughout the whole building energy supply chain, identifying what type of systems are able to extract cool exergy from the environment. Similarly, Kazanci et al. [62], analysed the exergy performance of different space cooling systems by separating "cool" and "warm" exergy in the analysis, enabling designers to appropriately quantify the exergy content of a heat source or a sink. Nevertheless, more evidence is still required among the building research community in order to reach an agreement on the most appropriate reference temperature.

1.3. Building design optimisation

Optimisation has been a popular approach in building research in the last years [63, 64]. The most popular objectives to be optimised have been energy demand, capital and operational costs, carbon emissions, and occupant’s thermal comfort [63]. Stochastic methods based on genetic algorithms (GA) can be regarded as the most utilised method for building energy optimisation [64]. Recent optimisation studies have focused on the application of artificial neural networks for tool performance improvement [65] and novel mixed integer linear frameworks [66, 67]. In terms of technologies, recent studies have focused on the integration of renewable energy [68, 69] and thermal properties optimisation of state-of-the-art phase change materials (PCM) [70]. Most recently, Chen and Yang [71], by using a surrogate-based optimisation model and considering the improvement of energy performance and thermal comfort, investigated the influence of climate conditions on passively designed buildings, exploring optimal designs at different climates in mainland China.
The combination of exergy analysis and multi-objective optimisation studies applied to a combined passive and active building design has been rather limited. García Kerdan et al. [72], focusing on renovation projects, presented an optimisation framework considering the minimisation of exergy consumption throughout the entire building energy supply chain, exploring a wide range of active and passive measures in a commercial building located in a cold climate. Later, the framework was improved by including economic and exergoeconomic analyses [73]. Similarly, Di Somma et al. [74] applied an exergy-based multi-objective optimisation of distributed energy systems aiming at reducing project’s costs and improving exergy efficiency by considering energy qualities of different supply sources. Gas-fired combined heat and power (CHP) systems were found among the most efficient systems to reduce primary exergy input, while solar technologies provided the best exergetic performance due to the availability of free renewable exergy.

Still, more research is necessary that considers the implications and interactions of distinct active and passive systems in buildings, aiming at improving thermodynamic performance, reducing costs and increasing occupant’s thermal comfort, especially in locations where climatic conditions are most favourable due to the availability of renewable energy resources such as solar and wind.

1.4. Research gaps

After a thorough search of the relevant literature, it was found that there is limited thermodynamic-oriented modelling frameworks that appropriately consider the effects of local bioclimatic conditions, and especially the thermal breeze effect in coastal regions, for the optimal design of low-energy/exergy and cost-efficient buildings. Additionally, existing tools lack relevant databases which consider a wide range of passive and active technologies with robust techno-economic characterisation that could be applied indistinctly to any building and region. Therefore, the aim of this study is threefold. First, to include the dynamic effect of the thermal breeze in a recently developed exergy-based dynamic simulation tool. The tool provides EnergyPlus [75] with the capability of performing dynamic exergy calculations, thanks to an external Python-based subroutine. Secondly, to built a comprehensive database considering different passive and active technologies within the context of coastal regions. And thirdly, to demonstrate the model’s capabilities, a social house located in the Mexican North-Pacific coast is studied and optimised under different thermodynamic and economic objectives.

The paper is organized as follows. First, an overview of the optimisation framework, the selected wind energy and exergy methods and the description of building technologies are presented. Later, the case study and the optimisation problem formulation are given. Next, the paper presents the obtained results from the optimisation procedure, followed by a design comparison between a selected optimal design (obtained from the Pareto front) with the benchmark design. This is followed by discussions and finally conclusions arising from this study.

2. Methodology and case study

2.1. ExRET-Opt: a dynamic exergy analysis optimisation tool

ExRET-Opt [73], is a novel building energy/exergy optimisation open-source tool developed by the authors. It is based on EnergyPlus [75] for dynamic energy simulations, combined with Python-based [76] routines for dynamic exergy analysis and exergoeconomic accounting. The
model’s second law analysis module is capable of calculating thermodynamic indices such as exergy consumption, exergy efficiencies and exergoeconomic parameters throughout the entire energy supply chain providing a more comprehensive analysis for the researcher or building designer. The exergetic analysis is mainly based on the work from the ECB-Annex 49 methodology [57], while the exergoeconomic analysis is based on the SPECO method developed by Lazzaretto and Tsatsaronis [77]. Both methods were further improved and adapted for whole building energy systems in García Kerdan et al. [78]. An overview of the main exergy calculation method can be found in Appendix A.

An additional strength of the tool is the large techno-economic database of passive and active energy technologies that incorporates, allowing the exploration of a wide range of design combinations (>4 quadrillion different combinations). In this study, several technology options have been added (Section 2.3). As the search space can be too large to perform full-parametric studies, to reduce simulation times, the tool is capable to simulate a limited number of solutions by using different sampling methods (Monte Carlo, Morris method, and Latin Hypercube). Additionally, a multi-objective optimisation mode based on genetic algorithms (NSGA-II) is available to improve designs in time-constraint studies.

2.2. Thermal breeze wind analysis

The main focus of this study has been to understand the potential of the thermal breeze in the design of a low-exergy building, as such, this section illustrates the derived model integrated into the dynamic exergy calculation tool.

As the sea-land breeze effect is a three-dimensional and dynamic effect throughout the day, dynamic simulations are required to fully account for its impact in the building’s physics. EnergyPlus is able to calculate the thermal effect of wind for each exposed surface, necessary to account for exterior convection, as it alters infiltration and ventilation flows throughout the analysed thermal zones. Therefore, appropriate data on wind speed and direction are required to produce the climatological file (.epw file), which is an important input to the model. However, this kind of data is limited, as normally data at a given location and specific height is available. When this is the case, EnergyPlus calculates wind speeds at different altitudes by means of extrapolation using the following equation:

\[ v_z = v_{\text{met}} \left( \frac{\delta_{\text{met}}}{\delta} \right)^{\alpha} \left( \frac{z}{\delta} \right)^{\alpha} \]

where \( z \) is the altitude height above ground [m], \( v_z \) is the wind speed at altitude \( z \) [m s\(^{-1}\)], \( \alpha \) is the wind speed profile exponent at the site [-], \( \delta \) is the wind speed profile boundary layer thickness at the site [\( \cdot \)], while \( z_{\text{met}}, V_{\text{met}}, \alpha_{\text{met}} \) and \( \delta_{\text{met}} \) is the height above ground [m], wind speed measured [m s\(^{-1}\)], wind speed profile exponent [\( \cdot \)], and wind speed profile boundary layer thickness [m] respectively at the meteorological station. As wind parameters depend on the surroundings (type of terrain and nearby constructions), for the specific case of coastal areas, \( \alpha \) is assumed as 0.10 and \( \delta \) as 100 m.

With the complete wind profile, the ventilation flow rate given by the thermal breeze throughout the entire building envelope can be calculated as follows [79]:

8
\[ Q_w = C_w A\text{opening} F_{schedule} V \]  

where \( Q_w \) is the volumetric air flow rate driven by the breeze \([\text{m}^3 \text{ s}^{-1}]\), \( C_w \) is the opening effectiveness \([-]\), \( A\text{opening} \) is the opening area \([\text{m}^2]\), \( F_{schedule} \) is the open area fraction \([-]\) and \( V \) is the local wind speed \([\text{m} \text{ s}^{-1}]\). In EnergyPlus, these equations can be accessed by using the object: ZoneVentilation:WindandStackOpenArea and the Thermal Analysis Research Program (TARP) convection model algorithm \([75]\).

Then, it is necessary to calculate hourly building energy demand considering the effects of natural ventilation \( (q_{\text{dem,vent,i}}(t_k)) \). Commonly, due to temperature differences between the outside and the inside environments, energy flows would escape or enter the building through the envelope via transmission and ventilation. Using Eq. 3, the internal load can be calculated as follows \([79]\):

\[ q_{\text{dem,vent,i}}(t_k) = \rho C_p Q_w \Delta T(t_k) \]  

where \( \rho \) is the the outdoor air density \([\text{kg} \text{ m}^{-3}]\), \( C_p \) is the specific heat coefficient \([1.007 \text{ kJ kg}^{-1} \text{K}^{-1}]\), \( A \) is the thermal area \([\text{m}]\) of zone \( i \), and \( \Delta T \) the differential between the outdoor temperature \( (T(t_k)) \) and the indoor temperature \( (T_0(t_k)) \) \([\text{K}]\).

Finally, to obtain the exergy demand considering the ventilation flow due to the thermal breeze effect, the following formula based on the Carnot factor can be used:

\[ E_{x_{\text{dem,vent,zone}}}(t_k) = \sum_{i=1}^{n} \left( q_{\text{dem,vent,i}}(t_k) \times \left( 1 - \frac{T_0(t_k)}{T_i(t_k) - T_0(t_k)} \ln \frac{T_i(t_k)}{T_0(t_k)} \right) \right) \]  

where, \( T_i \) is the average inside temperature \([\text{K}]\), \( q_{\text{dem,vent}} \) is the energy demand due to ventilation \([\text{kWh}]\), \( t_k \) is the time-step \([-]\), and \( n \) is the number of analysed thermal zones. As typical convention, heating energy is regarded as positive \((q+)\) while cooling energy as negative \((q-)\), defining the direction of the energy flow. However, as defined by Shukuya \([80]\) and the ECB-Annex49 \([57]\) method, the exergy flow would depend not only the heat flow direction, but also on the indoor and ambient temperatures. In the case of space cooling, when the required indoor temperature is higher than the outside temperature (mainly due to high internal heat gains), it means that there is exergy available indoors that needs to be extracted, thus an exergy output is required \((E_{x-})\). On the other hand, when the required indoor temperature needs to be lower than the outside, an exergy input is required bringing cool exergy indoors \((E_{x+})\). In order to keep the indoor temperature at a comfortable range, it is required to supply cool exergy at a rate higher than the cool exergy escaping from the building.

This group of equations form the basis for the calculation of minimum amount of work (thermal exergy) necessary to cover thermal demands in buildings with high natural ventilation rates. Eq. 4 has been added to ExRET-Opt enabling the quantification of exergy demand considering both internal gains and ventilation effects due to thermal breezes.

2.3. Design strategies

The technological database has been expanded by including several solar passive and active strategies as well as other energy efficiency measures. Table 1 presents the techno-economic data for all possible energy efficiency measures available in this study.
Table 1: Techno-economic database of possible active and passive measures

<table>
<thead>
<tr>
<th>Type</th>
<th>Technology/measure</th>
<th>Description</th>
<th>Cost unitary/range</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Passive measures</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Glazing</td>
<td>Single pane</td>
<td>5mm clear pane</td>
<td>133 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Double-pane</td>
<td>5mm clear pane with 6 or 13mm gap filled with either air, argon or krypton</td>
<td>349-494 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Triple-pane</td>
<td>5mm clear pane with 6 or 13mm gap filled with either air, argon or krypton</td>
<td>624-873 US$ m⁻²</td>
</tr>
<tr>
<td>Insulation</td>
<td>Polyurethane</td>
<td>2 to 15 in 1 cm steps</td>
<td>8.87-31.01 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Extruded polystyrene (XPS)</td>
<td>1 to 15 in 1 cm steps</td>
<td>6.34-42.54 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Expanded polystyrene (EPS)</td>
<td>2 to 15 in 1 cm steps</td>
<td>5.78-13.23 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Cellular Glass</td>
<td>4 to 18 in 1 cm steps</td>
<td>21.55-97.01 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Glass fibre</td>
<td>6.7 7.5 8.5 and 10 cm</td>
<td>7.51-10.3 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Cork board</td>
<td>2 to 30 in 2 cm steps</td>
<td>7.40-114.11 US$ m⁻²</td>
</tr>
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<td></td>
<td>Phenolic foam board</td>
<td>2 to 10 in 1 cm steps</td>
<td>7.42-29.11 US$ m⁻²</td>
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<td></td>
<td>Aerogel</td>
<td>0.5 to 4 in 0.5 cm steps</td>
<td>35.64-259.53 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>PCM (u/board)</td>
<td>10 and 20 mm</td>
<td>76.8-143.3 US$ m⁻²</td>
</tr>
<tr>
<td>Solar protection</td>
<td>Overhangs</td>
<td>Material: PVC module with 20 mm width</td>
<td>39.9 US$ m⁻²</td>
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<tr>
<td></td>
<td>Fins</td>
<td>Length: 0.05 to 2.0 m</td>
<td></td>
</tr>
<tr>
<td><strong>Active measures</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>HVAC system</td>
<td>Air source heat pumps</td>
<td>COP: 2.5</td>
<td>601.6 US$ kW⁻¹</td>
</tr>
<tr>
<td></td>
<td>Ground source heat pumps</td>
<td>COP: 3.5 (horizontal boreholes)</td>
<td>1596 US$ kW⁻¹</td>
</tr>
<tr>
<td></td>
<td>District cooling + HX + radiant cooling</td>
<td>Trigeneration: single-effect indirect-fired CHP with absorption chiller</td>
<td>75 US$ kW⁻¹ district heat exchanger</td>
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<tr>
<td></td>
<td></td>
<td>with a COP of 0.7.</td>
<td>6140 US$ connection charge and 66.5 US$ m⁻³ insulation for pipes</td>
</tr>
<tr>
<td>Cooling emission system</td>
<td>Variable Air Volume (VAV) (GSHP and ASHP only)</td>
<td>Single duct VAV with cooling efficiency of 72.2% and auxiliary energy demand of 14.82 W m⁻²</td>
<td>931 US$ per system</td>
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<tr>
<td>Lighting</td>
<td>CFL lamps</td>
<td>Low wattage lamps with low ballast factor.</td>
<td>153 US$ kW⁻¹</td>
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<td></td>
<td>LED</td>
<td>Power density: 10.7 W m⁻²</td>
<td>295 US$ kW⁻¹</td>
</tr>
<tr>
<td>Active solar renewable</td>
<td>Solar PV</td>
<td>Monocrystalline silicon panels with module efficiency of 13-15%</td>
<td>852 US$ m⁻²</td>
</tr>
<tr>
<td></td>
<td>Solar collectors</td>
<td>Flat plate solar thermal collector (HSTC) with efficiency between 60-80%, 40% propylene glycol/water mixture and pump efficiency of 87%</td>
<td>382 US$ m⁻²</td>
</tr>
<tr>
<td>Other renewable</td>
<td>Wind turbines</td>
<td>Small scale wind turbines (micro) 1.0 - 1.5 kW</td>
<td>1000-3000 US$ per unit</td>
</tr>
<tr>
<td>Control</td>
<td>Window automatic control</td>
<td>Chain actuators with PID control</td>
<td>150 US$ per window plus home control system</td>
</tr>
</tbody>
</table>
Most of the passive strategies aim at optimising heat flows by improving building’s envelope physical characteristics. Constructive strategies such as the usage of an air gap in the composite walls as a means to reduce insulation thickness has been considered. Additionally, a window control system for opening at certain angles are simulated to allow for effective cross-ventilation and/or night flush cooling; while solar shading are considered as low-cost measures to minimise solar gains. For active solar systems, collectors and photovoltaic panels have been considered.

2.4. Case study: The Mexican coastal region

In 2015, the Mexican residential sector was responsible for 14.8 % (755 PJ) of the national energy demand [81], emitting around 21,280 Gg CO$_2$eq [82]. It was estimated that coastal housing was responsible for over 30% of these emissions [82]. Mexico’s coast extends over more than 11,000 km and it is considered one of the largest and most dynamic commercial areas, and key for the development of the country’s economy [83]. Around 15% of the population live in coastal areas and are currently experiencing higher population growth rates than inland cities [84]. Added to this, a constant increment in household income and demand increase for thermal comfort have led to a rise in the installation and energy demand of artificial cooling. According to McNeil et al. [85], 35% of households located in hot climates own an air conditioner (AC), with an average cooling capacity of 5.3 kW per household. By 2050, AC ownership is expected to reach 50%, while household cooling capacity to increase to 6.3 kW. Just emissions related to additional cooling demand could reach about 10,000 Gg CO$_2$eq by 2030. Therefore, new strategies and programmes are necessary to limit these emissions without compromising the health and life quality of the population.

To test the proposed optimisation framework, a social house in the city of ‘Cabo San Lucas, Baja California Sur (BCS)’, located in the Mexican North-Pacific coast has been selected as a case study (Figure 2). The city has a population of 85,000 inhabitants, with annual growth rates of about 3.8%, well above the national average of 1.3%. Generally, the BCS state is located in the arid climatic region; however, the southern region, where Cabo San Lucas is located, is considered tropical, lying just under the Tropic of Cancer. The climate throughout the year is mostly hot and humid, with daily average temperatures just over 30 °C during the summer. The region posses one of the highest solar irradiation potentials in the country, with levels above 5.8 kW m$^{-2}$ (Figure 2).

To justify the presence of artificial air conditioners in a social house in the region, according to government’s official figures [86], there is a probability of 32.3% that a social house in Cabos, BCS would have an air conditioning. For the lowest income groups living in social housing, the probability is as low as 15.4%, while for the highest income the probability is as high as 93.4%. The report also suggest that 46% of the total installed equipment are ‘window’ type while 54% are mini-splits.
For the climatological file, hourly data such as air temperature, relative humidity, atmospheric pressure, and radiation parameters have been collected from Meteonorm [88]. Additionally, data on wind speeds and wind directions from regional thermal breezes have also been collected. Figure 3 illustrates the distribution of wind direction and wind velocities for the city. It can be seen that most of the winds come from the south and west directions, with average air velocities of about 3.5 m s$^{-1}$; however, wind speeds over 5 m s$^{-1}$ are frequent.

To better appreciate the wind direction and speed in relation to the case study’s geography, a wind rose summarising the wind profile and the coast location is shown in Figure 4. As expected, the majority of the sea breeze, characterised by stronger winds, comes from the South and South-West, while land breezes are most predominant from the West and North-West regions. One of
the main advantages of thermal breezes is that directions remain fairly constant through the year, which provides an easier assessment for the development of optimal building orientation to improve cross-ventilation strategies.

![Wind Rose and location for Cabo San Lucas, Mexico](image)

Figure 4: Wind Rose (left) and location for Cabo San Lucas, Mexico (wind data: velocity in $\text{m s}^{-1}$ and frequency; Map source: Microsoft Bing Maps [89])

A two-storey/two-flat house has been chosen. This layout represents FOVISSSTE’s (the state’s housing fund) ‘duplex D’ archetype social house design. Detailed information can be found in the supplementary data (S.1). On average, social house under the defined category (duplex D) is about $51 \text{ m}^2$, while for the case study is around $62 \text{ m}^2$. Each flat is comprised of two bedrooms, a living-dining room, a kitchenette and a bathroom. Also, solar shading is considered in the base design as a low-cost measure. The 3D model is illustrated in Figure 5.

![3D model of the typical house layout](image)

Figure 5: Typical two storey/two flat social house layout in Mexico’s hot climates
2.5. Baseline thermal performance: Calibration

The baseline building energy performance has been calibrated based on electricity demand values obtained from several regional studies [90, 91]. As a pre-processing step, the ExRET-Opt optimisation mode has been used to reduce the difference between the model’s monthly energy use and the empirical data. This optimisation approach minimises the Coefficient of Variation of the Root Mean Squared Error (CVRMSE) [92].

\[
\text{min} [\text{CVRMSE} \%] = \sqrt{\frac{\sum_{i=1}^{N_p} (m_i - s_i)^2}{N_p \bar{m}^2}} \quad (5)
\]

where \(m_i\) is the empirical value for month \(i\), \(s_i\) is the predicted value for month \(i\), \(N_p\) is the sample size (\(N=12\)), and \(\bar{m}\) is the mean value of the empirical data (\(\sum_{i=1}^{N_p} (m_i/N_p)\)). When monthly data is used, a CVRMSE up to 0.15 is tolerable to consider a model calibrated.

For the calibration process, based on the current Mexican energy regulations [93], constrains on building physical characteristics (mainly envelope’s \(U\) values) and energy systems efficiency have been considered. Table 2 shows the main building design parameters and thermodynamic values obtained. The calibrated baseline building has a total energy use index (EUI) of 268.1 (kWh m\(^{-2}\)y\(^{-1}\)). Electricity represents 76% of the total energy use, while the rest is covered by liquefied petroleum gas (LPG). Cooling demand represents 46.5% of the total supplied electricity, followed by electric appliances (35.3%) and lighting (16.0%). The simulation process also estimated the cooling equipment installed capacity (4.9 kW for the bottom flat and 5.6 kW for the top flat), converging with those values presented in McNeil et al. [85] (\(\sim 5\) kW). On the other hand, LPG is mainly used for water heating (51%) and cooking (49%). Annual energy bills have been found just above US$ 1,100 per flat. The model has considered a price of 0.063 US$ kWh\(^{-1}\) for electricity and 0.052 US$ kWh\(^{-1}\) for LPG. Accounting for the whole energy supply chain, the building consumed exergy in the order of 513.6 kWh m\(^{-2}\)y\(^{-1}\), with an exergetic efficiency (\(\psi\)) of 11.3%. This value is found within range, compared to those found in other studies in similar climates (\(\psi = 9.0-12.1\%\)) [94].
### Table 2: Calibrated baseline model main characteristics

<table>
<thead>
<tr>
<th>Baseline characteristics</th>
<th>Social housing (North-west Mexico)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Year of construction</td>
<td>2018</td>
</tr>
<tr>
<td>Number of floors/flats</td>
<td>2/2</td>
</tr>
<tr>
<td>Total floor space (m²)</td>
<td>130 (65 m² per flat)</td>
</tr>
<tr>
<td>Orientation (°)</td>
<td>East-West (180° with respect to the north)</td>
</tr>
<tr>
<td>Infiltration rate (ach)</td>
<td>4.0</td>
</tr>
</tbody>
</table>

**Exterior Walls**
- Cavity Wall-Brick walls 130 mm brick with 20mm air gap + external insulation (50 mm expanded polystyrene)
  \[ U_{value} = 0.45 \text{ W m}^{-2} \text{K}^{-1} \]

**Roof**
- 160 mm concrete block + external insulation (130 mm expanded polystyrene)
  \[ U_{value} = 0.26 \text{ W m}^{-2} \text{K}^{-1} \]

**Ground floor**
- 100 mm concrete slab
  \[ U_{value} = 0.52 \text{ W m}^{-2} \text{K}^{-1} \]

**Windows**
- Single-pane clear glass (5mm thick)
  \[ U_{value} = 5.84 \text{ W m}^{-2} \text{K}^{-1} \]

**Glazing ratio**
- 7%

**HVAC System**
- Window air conditioning system
  - 4.9 kW bottom flat, 5.6 kW top flat
  - \( \eta = 90\% \)
  - No heating system

**Emission system**
- Fan system and natural ventilation

**Cooling Set Point (°C)**
- 22.5

**Occupancy (people)**
- 3-4 per flat

**Equipment (W m\(^{-2}\))**
- 3.9

**Lighting level (W m\(^{-2}\))**
- 10.7

**EUI_{electricity} (kWh m\(^{-2}\)y\(^{-1}\))**
- 211.3

**EUI_{LPG} (kWh m\(^{-2}\)y\(^{-1}\))**
- 66.8

**Annual energy bill (US$ y\(^{-1}\))**
- 1,105 per flat

**Thermal discomfort (hours)**
- 1,460

**CO\(_2\) emissions (energy) (Ton)**
- 8.2 per flat

**Life cycle cost - 50 years (US$)**
- 39,865

**Total annual exergy input (kWh m\(^{-2}\)y\(^{-1}\))**
- 579.2

**Annual exergy consumption (kWh m\(^{-2}\)y\(^{-1}\))**
- 513.6

**Building exergy efficiency (%)**
- \( \psi = 11.3 \)

### 2.6. Optimisation problem

The optimisation problem has been designed to simultaneously optimise the following three objectives:

- i. Building annual exergy consumption (\( E_\text{Ex,cons,bai} [\text{kWh m}^2 \text{ y}^{-1}] \)):  

15
\[ Z_1(x)_{\text{min}} = Ex_{\text{cons, bas}} = \left[ \sum_{f=1}^{f} Ex_{\text{prim}}(t_k) - \sum_{i=1}^{i} Ex_{\text{dem, enduse, } i} \right] \]  

(6)

where \( Ex_{\text{prim}} \) is the sum of primary exergy input from fuel \( f \) (\( f = \) electricity, gas, lpg) and \( Ex_{\text{dem, enduse, } i} \) is the exergy demand at end use service \( i \) (\( i = \) cooling, dhw, appliances, cooking).

ii. Occupant discomfort hours (based on the Predicted Mean Vote Index (PMV) expressed by the Fanger’s model \([95]\)):

\[ Z_2(x)_{\text{min}} = (|PMV| > 0.5) = |(0.303e^{-0.036M} + 0.028) L| > 0.5 \]  

(7)

where \( M \) is the metabolic rate \([W m^{-2}]\), \( L \) is the thermal load defined by the difference between the internal heat gains of occupancy per unit area and the heat loss to the environment \([W m^{-2}]\), and \( e \) is the Euler’s number \([e = 2.718]\). The index was primarily developed to assess the impacts of mechanically ventilated buildings in thermal comfort; thus, careful assessment needs to be made for natural ventilated (NV) buildings as PMV values could be over or under predicted.

iii. Life Cycle Cost - 50 years (US$):

\[ Z_3(x)_{\text{min}} = LCC_{50\text{years}} = \sum_{n=1}^{N} \left[ \frac{CF_n}{(1 + r_d)^n} \right] \]  

(8)

where \( CF_n \) is the annual cash flow of year \( n \) [US$ y^{-1}]\), \( N \) is the total years of evaluation, and \( r_d \) is the discount rate [%]. The annual cash flow can be calculated as follows:

\[ CF_n = \left[ (C_n^B + O&M_n^B) + (C_n + O&M_n) + (C_{en}) \right] \]  

(9)

where \( C_n^B \) is the baseline capital cost [US$], \( O&M_n^B \) is the baseline operation and maintenance cost [US$], \( C_n \) is the incremental capital cost in year \( n \) [US$], \( O&M_n \) is the incremental operation and maintenance cost in year \( n \) [US$], and \( C_{en} \) is the annual energy cost [US$].

Therefore, the optimisation model can be formulated as follows.

Given \( x = \left< X_{glaz}, X_{wall, ins}, X_{roof, ins}, X_{shade}, X_{HVAC}, X_{setpoint}, X_{light}, X_{PV}, X_{wind}, X_{col} \right> \)

in the solution space \( X \), find the vector(s) \( x \) that:

\[ \text{minimises} \quad Z(x^*) = Z_1(x^*), Z_2(x^*), Z_3(x^*) \]

The model has been constrained considering the following maximum costs and discomfort time values:
s.t:
\[
\begin{align*}
LCC(x) &\leq US\$ 90,000 \\
\text{Discomfort}(x) &\leq 10\% \text{ occupied time}
\end{align*}
\]

Table 3 shows the NSGA-II algorithm settings defined in the model. The NSGA-II procedure embedded within the ExRET-Opt tool is further explained in the Appendix B.

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Encoding scheme</td>
<td>Integer encoding (discretisation)</td>
</tr>
<tr>
<td>Population type</td>
<td>Double-Vector</td>
</tr>
<tr>
<td>Population size</td>
<td>50</td>
</tr>
<tr>
<td>Crossover Rate</td>
<td>100%</td>
</tr>
<tr>
<td>Mutation Rate</td>
<td>40%</td>
</tr>
<tr>
<td>Selection process</td>
<td>Stochastic fitness influenced</td>
</tr>
<tr>
<td>Tournament Selection</td>
<td>2</td>
</tr>
<tr>
<td>Elitism size</td>
<td>Pareto optimal solutions</td>
</tr>
<tr>
<td>Max Generations</td>
<td>100</td>
</tr>
<tr>
<td>Time limit (s)</td>
<td>(10^6)</td>
</tr>
<tr>
<td>Fitness limit</td>
<td>(10^{-6})</td>
</tr>
</tbody>
</table>

3. Results and discussion

3.1. Constrained solutions and adopted measures

Following the optimisation run, 4,800 distinct designs have been collected. Different to other optimisation approaches, solutions with high output heterogeneity can be found due to the gene crossover, mutation and selection processes. In this study, 25\% of the solutions were found in the constrained region. Figure 6 illustrates the final solutions as well as the Pareto front.
Generally, higher cost designs have provided the best comfort levels; however, at the expense of higher energy use and exergy consumption due to the more intensive utilisation of artificial cooling equipment, with average temperature set-points of around 23 °C. Additionally, these designs are mainly based on high insulation levels, triple-pane windows and oversized active solar technologies (collectors and PV panels), which in turn have increased capital expenditure.

Figure 7 illustrates the distributions of the most important active and passive design strategies found in the constrained region (see the Nomenclature section for labels). As shown, among the most popular adopted passive measures have been double-pane glazing (either filled with air, argon or krypton), expanded polyestyrène (EPS) and cellular glass with thickness between 2 and 12 cm for both wall and roof insulation, as well as solar shading devices (Appendix C, Figure C.1). The most common values for overhangs has been found at 0.95 m, while for right and left fins at 1.15 and 0.80 m respectively; however, optimal lengths for solar shading greatly depends on building’s solar gains and orientation. In this regard, the most common orientations have been found between 170-190° (east-west orientation considering the North as reference at 0°). Within this orientation range, the thermal breeze impacts the building’s main façade directly as the most frequent and strongest winds come from the south (sea breeze). When windows on both sides are open, this maximises cross-ventilation flow rates. During the day and with low wind speeds this provides comfort levels to the occupants; however, higher wind speeds (around 3 m s$^{-1}$), which are frequent in the analysed region, could produce discomfort. This could be addressed by controlling the window’s opening angles [33]. Among the most widely adopted active systems, solar PV panels covering between 10-30% of the roof area, 10-20 m$^2$ of solar collectors, LED lighting and ASHPs have been found.

The most frequent rejected measures, due to cost or performance issues, have been high surface areas of PV panels (> 60% roof area) and solar collectors (>40 m$^2$). Also, GSHPs and district cooling have not been as widely adopted as ASHPs, mainly due to high capital costs. However, designs based on GSHPs typically provided the lowest exergy consumption, while district cooling networks combined with wall emission systems provided the best solutions for thermal comfort.
Figure 7: Distribution (bars) and the fitted probability distribution (lines) of main design parameters for the constrained solutions
Among the analysed objective functions, the average values for exergy consumption, discomfort hours and LCC have been found at 617 kWh m$^{-2}$y$^{-1}$, 219 hours, and US$ 74,387 respectively. Compared to the baseline values, exergy consumption and LCC have increased due to dramatic improvements in thermal comfort. However, these designs count with a larger share of renewable generation (mainly from solar technologies) and low-exergy cooling equipment (such as heat pumps), which have increased capital costs considerably. As the exergy analysis method used in this model does not make a distinction between exergy use from fossil fuels or renewable energy, irreversibilities in the system using either grid electricity or from PV generation are regarded similarly. If renewable exergy use were not to be considered, the average consumption would be reduced to 522 kWh m$^{-2}$y$^{-1}$, similar to the baseline value. An important parameter that has been greatly improved thanks to on-site generation was the annual energy bill, as average values were found at US$ 703 per flat, representing savings in the order of 36.4%. This reduction has been achieved without considering the effect of feed-in tariffs or incentives from renewable generation, as these programmes are not yet implemented in the country. Otherwise, this would help minimise project’s life cycle cost and increase the return of investment, possibly unlocking other more expensive low-exergy technologies such as ground source heat pumps and/or high temperature district cooling systems.

3.2. Pareto front solutions and adopted measures

Figure 8 illustrates the design parameters distribution exclusively from the Pareto front (n=109) (Figure 6b). In these ‘optimal’ solutions, the most common measures have been the following: reduced area for PV panels (10% of roof area, equivalent to about 1.1 kWp), large solar collectors areas (up to 40 m$^2$, or 60% of the roof area), connection to a district cooling network, double-pane air filled glazing, 5 cm (range: 1-10 cm) of extruded polyethylene (XPS) for wall insulation, 9 cm (range: 1-15 cm) of polyurethane for roof insulation, and an orientation of 45° or 225° with respect to the north axis.

With regards to the building orientation, the most common Pareto values (45° and 225°) represent a further improvement compared to the mean value found in the constrained solution (170-190°). This affirmation is based on the study from Givoni [96], where the author recommended that angles between 30° and 60° relative to the main breeze axis allows for better pressure control and ventilation flow. However, he also mentioned that ventilation from thermal breezes will either reduce cooling requirements or improve thermal comfort, but not both. Therefore, the outputs from our Pareto front illustrate that optimal solutions preferred to use natural cross-ventilation and specific active and passive strategies for thermal comfort improvement (an increase of 99.2% compared to the baseline, reducing annual discomfort hours to 11 hours), while average exergy consumption were found at 915 kWh (an increase of 80.5%). High irreversibilities arise due to higher utilisation of the cooling equipment at night, as heat gains during day-time ventilation were being released by the building’s thermal mass at night. Night ventilation, which is the opposite strategy, could have been followed as it can cool the building mass and store cold to be utilised during the day; however, this strategy is optimised when the building has high insulation levels, an air-tight envelope, and closed windows throughout the day. This strategy deprives the design to take advantage of the day-time thermal breezes for thermal comfort.
Figure 8: Distribution (bars) and the fitted probability distribution (lines) of main design parameters for the Pareto front highlighting the 'closest to utopia' (CTU) design.
The Pareto designs have also come with a two-fold increase in life cycle cost, reaching an average value of US$ 82,413. At this point, it can be concluded that the optimisation procedure instead of converging on designs that utilised the sea-land breeze effect for high thermodynamic and low-cost performance, it was converging on designs where the thermal breeze (mainly sea breeze at day-time) was exploited for the improvement of thermal comfort. Also, when analysing the objective’s convergence (Figure 9), thermal comfort converged to its minimum value from the 2nd generation, while exergy consumption and life cycle cost did it at the 78th and 59th generation respectively. Therefore, most of the designs resulted in solutions with high cost, high exergy use and high thermal comfort due to what can be called an 'algorithm failure'. This takes place when at some point in the evolution process, the optimisation process between generations finds it difficult to move and find other more balanced solutions. The discussed designs that shift the objective function mean outputs, can be seen by the Pareto’s right 'tail' illustrated in Figure 6b.

![Figure 9: Convergence test of each objective function during the optimisation process](image)

3.3. Compromise programming: the closest to utopia (CTU) design

As part of the tool’s capabilities, a decision-making process has been implemented in order to choose a final optimal design that satisfies most of the objectives and to provide a comparative study with the baseline design. This would also locate those solutions that are weighting only one of the objectives exclusively, thus filtering those designs in the final consideration. From the Pareto front, and based on compromised programming, the Chebyshev distance ($\alpha_j$) minimisation method has been applied to screen all possible solutions. In this case, weights for each objective are initialised and screened to obtain a series of compromised solutions. The method transforms a multi-objective problem into a single-objective one. The corresponding weight factors ($p_j$) reflect the relative importance of each objective, where the sum of weight coefficient has to satisfy the following constraint:

$$\sum_{j=1}^{n} p_j = 1$$  (10)
Then, the Chebyshev distance can be calculated as follows:

$$\alpha_j \geq \left( \frac{|Z_j^* - Z_j(x)|}{|Z_j^* - Z_{xj}|} \right) \ast (p_j) \quad (11)$$

As the method scans all the feasible possible sets, it minimises the deviation from the ideal point, obtaining the minimum Chebyshev distance ($\min\alpha_j [\cdot]$) and therefore a final design. This provides the decision maker with different trade-off scenarios. The whole screening of the Pareto front using the Chebyshev method can be found in the Supplementary Data (S.2). As shown, the multi-criteria method has been able to filter most of the solutions with high capital cost and moved on rather quickly from the right tail located in the Pareto front. This is illustrated as ASHPs appear in most of the compromised solutions instead of District Cooling, even though the latter is found four times the former in the Pareto front.

For further analysis, the equal weight or ‘closest to utopia’ (CTU) design, where $p_{exergy}$, $p_{discomfort}$, and $p_{lcc}$ are all equal to 0.33, is selected. In Figure 8, the CTU design parameters have been highlighted. The CTU energy system schematic is represented in Figure 10, while the capital cost for energy-related measures is presented in Table 4. For this particular design, passive-related measures represent 54.2% of the design’s capital cost.

![Figure 10: Closest to utopia (CTU) solution HVAC and energy system schematic](image-url)
Table 4: Capital cost of energy related measures for the CTU solution [US$]

<table>
<thead>
<tr>
<th>CTU design technologies</th>
<th>Observations</th>
<th>Capital cost [US$]</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Active systems</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Air source heat pump</strong></td>
<td>2.4 kW</td>
<td>1,422</td>
</tr>
<tr>
<td><strong>HVAC distribution and emission system</strong></td>
<td>COP : 2.5 W/W insulated pipes, pumps and VAV systems</td>
<td>2,000</td>
</tr>
<tr>
<td><strong>Lighting</strong></td>
<td>LED lighting (power: 3.7 W/m²)</td>
<td>144</td>
</tr>
<tr>
<td><strong>PV panels</strong></td>
<td>1.1 kWp</td>
<td>5,794</td>
</tr>
<tr>
<td><strong>Solar collectors</strong></td>
<td>10 m²</td>
<td>3,820</td>
</tr>
<tr>
<td><strong>Windows control</strong></td>
<td>Actuators plus control system</td>
<td>2,000</td>
</tr>
<tr>
<td><strong>Passive systems</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Glazing</strong></td>
<td>double-pane</td>
<td>11,362</td>
</tr>
<tr>
<td></td>
<td>krypton filled</td>
<td></td>
</tr>
<tr>
<td><strong>Wall insulation</strong></td>
<td>8.5 cm glass fibre</td>
<td>3,263</td>
</tr>
<tr>
<td><strong>Roof insulation</strong></td>
<td>15 cm XPS</td>
<td>2,893</td>
</tr>
<tr>
<td><strong>Solar protection</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td><strong>Front façade:</strong></td>
<td>Overhangs 1.1 m</td>
<td>420</td>
</tr>
<tr>
<td></td>
<td>Right fins: 0.15 m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Left fins: 1.55 m</td>
<td></td>
</tr>
<tr>
<td><strong>Back façade:</strong></td>
<td>Overhangs 0.2 m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Right fins: 0.75 m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Left fins: 0.85 m</td>
<td></td>
</tr>
<tr>
<td><strong>Left side façade:</strong></td>
<td>Overhangs 1.2 m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Right fins: 0.35 m</td>
<td></td>
</tr>
<tr>
<td></td>
<td>Left fins: 1.3 m</td>
<td></td>
</tr>
</tbody>
</table>

Figure 11 presents the design day performance of the CTU design compared to the baseline. Wind directions (Figure 11a) and speeds (Figure 11b) for that specific day are illustrated. The evening peak demand (around 7 pm) has been greatly reduced due to optimal insulation levels and solar shading devices, as solar gains throughout the day were minimised which in turn reduced the amount of heat stored at the building’s thermal mass. The entering cool sea breeze, especially in the morning (from 2 am to 5 am) and in the evening (from 8 pm to 11 pm), results in the reduction of internal temperatures. Overall, as natural ventilation rates have improved thermal comfort sensation, this has resulted in a reduction in hourly cooling demand as set-points were able to be increased on average 1.5 °C. Orientation and window control has resulted in internal average window velocities of 0.33 m s⁻¹.

The building cooling energy demand for that specific day has been reduced from 223 kWh day⁻¹ to 154 kWh day⁻¹, while exergy demand has been reduced by two-thirds, from 50.4 kWh day⁻¹ to 19.3 kWh day⁻¹, due to an optimal use and harvest of cool exergy from the thermal breezes. Finally, thanks to a more constant indoor thermal environment, this would make artificial cooling equipment work on a more regular basis, increasing its performance as it would not require to be constantly turned on and off. This also increases equipment’s lifetime.
Lastly, Table 5 presents the annual performance comparison considering the main studied indicators. Although gross energy demand has not been greatly reduced, if on-site generation is considered, the building reduced around half of its baseline grid demand. Although it can not be regarded as a low-exergy building due to still high exergy consumption rates, it has to be considered that almost one-third of the primary exergy input now comes from renewable sources (especially solar-based electricity and hot-water generation). As previously discussed, the orientation of the CTU design has been optimised to 30° relative to north, to make the best use of sunlight and natural ventilation from thermal breezes. This single bioclimatic low-cost measure contributes importantly to the reduction of energy demand and exergy consumption from the whole energy
supply chain while considerably improving occupant thermal comfort.

Although capital costs are higher than the baseline, reduced annual energy bills have resulted in an LCC increase of just 18.5% or US$ 7,381 over a 50 year period. This represents an annual increase in expenditure of about US$ 53 per household. If some level of incentives were to be considered due to on-site renewable generation, this could easily offset this cost increase. Certainly, the cost increase can be justified by the considerable improvement of indoor environmental conditions. This could have other non-energy benefits such as improved health conditions and lifestyle performance, implications that were not considered in this particular study.

Table 5: A comparison of main indicators between baseline and CTU design

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Baseline</th>
<th>CTU</th>
<th>Difference (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Primary energy (kWh m² y⁻¹)</strong></td>
<td>620.1</td>
<td>290.3</td>
<td>-53.2%</td>
</tr>
<tr>
<td><strong>Site energy (kWh m² y⁻¹)</strong></td>
<td>278.1</td>
<td>250.2</td>
<td>-10.0%</td>
</tr>
<tr>
<td><strong>PV electricity generation (kWh m² y⁻¹)</strong></td>
<td>0.0</td>
<td>13.9</td>
<td>n/a</td>
</tr>
<tr>
<td><strong>Solar Thermal DHW generation (kWh m² y⁻¹)</strong></td>
<td>0.0</td>
<td>31.4</td>
<td>n/a</td>
</tr>
<tr>
<td><strong>Net site energy (kWh m² y⁻¹)</strong></td>
<td>278.1</td>
<td>131.4</td>
<td>-52.7%</td>
</tr>
<tr>
<td><strong>Primary exergy input (kWh m² y⁻¹)</strong></td>
<td>571.9</td>
<td>514.9</td>
<td>-10.0%</td>
</tr>
<tr>
<td><strong>Exergy consumption (kWh m² y⁻¹)</strong></td>
<td>507.2</td>
<td>454.7</td>
<td>-10.3%</td>
</tr>
<tr>
<td><strong>Building exergy efficiency</strong></td>
<td>11.3%</td>
<td>11.7%</td>
<td>3.3%</td>
</tr>
<tr>
<td><strong>Energy measures CAPEX (US$)</strong></td>
<td>11,295.2</td>
<td>33,117.6</td>
<td>193.2%</td>
</tr>
<tr>
<td><strong>Annual energy bill (US$)</strong></td>
<td>2,210.4</td>
<td>1,098.6</td>
<td>-50.3%</td>
</tr>
<tr>
<td><strong>Life Cycle Cost - 50 years (US$)</strong></td>
<td>39,864.6</td>
<td>47,245.7</td>
<td>18.5%</td>
</tr>
<tr>
<td><strong>Discomfort (hours)</strong></td>
<td>1,459.7</td>
<td>89.8</td>
<td>-93.8%</td>
</tr>
</tbody>
</table>

3.4. Discussion

With the intention to make exergy-oriented optimisation more available for design practice, it is fundamental to provide robust methodological frameworks that produce cost-effective and comfortable designs under low-uncertainty levels. This study has combined exergy and bioclimatic analysis with optimisation and multi-criteria decision frameworks, yielding final solutions that satisfied thermodynamic and thermal comfort objectives with minimal increase in cost. Additionally, the presented optimisation framework, has been adapted to analyse the thermodynamic influence of the sea-land breeze effect. The research has demonstrated the necessity to consider the local environment at an early stage in the building design process. Exergy optimisation can be regarded as a more comprehensive method as it accounts for true thermodynamic efficiencies and locates exact sources of irreversibilities that should be minimised.

The low-exergy and bioclimatic approaches present some similarities, as most bioclimatic strategies can be regarded as exergy efficient, where the energy quality of supply sources are close to the demand quality of services (e.g. natural light for lighting demand or natural ventilation to cover cooling demands). However, technically, due to energy harvest limitations and real environmental dynamics, it is recommended that passive strategies are supported by active measures to achieve a desired thermal performance. This study has considered this limitation, as the tool aimed to first account for local low-exergy resources and then, if necessary, supplement the building system.
with active measure with minimal thermodynamic losses. If the installation of artificial space conditioning is necessary, high-exergy efficient technologies should be encouraged (GSHP, low-exergy district cooling network); however, currently these come with considerable investments and operational costs. During the last decade, active solar technologies have experienced constant capital cost reduction resulting in higher uptake rates. A similar success could be expected for low-exergy technologies. An advantage of these technologies is that when in operation, they could provide an important reduction in primary energy demand as well as in operational cost while minimising the total environmental impact of the building and consequently the entire building stock. Nevertheless, cost-optimality of these measures will strongly depend on factors such as energy prices and government subsidies or incentives.

Although not part of this study, consideration of the urban design is also necessary. At a neighbourhood level, it is recommended for houses to be separated to optimise the breeze effect between buildings [14]. Poor urbanisation in the coast could limit the natural flow of sea-land breeze, leading to higher temperatures inland, negative health effects and large energy use by the intensification of cooling services. An increase in building standards that considers solar and wind resources in coastal areas, on both at building and urban levels, could support the development of a future decarbonised and more efficient housing stock.

4. Conclusions

Limited research has focused on optimising exergy and thermal comfort performance of coastal buildings located in tropical areas, where it is expected that artificial cooling will be responsible for a considerable share in future global electricity demand.

This study has included a wind energy/exergy analysis method that accounts for the thermodynamic performance of the thermal breeze in buildings. The model has been added into a multi-objective optimisation decision-support modelling tool capable of evaluating cost-efficient and low-exergy coastal housing designs with high thermal comfort performance. Additionally, specific active and passive strategies that aim at maximising the utilisation of local wind and solar resources have been developed. This approach supports building designers in complex decision making in coastal areas by considering the fundamental laws of thermodynamics.

The specific optimisation study has focused on performing a comprehensive exploration of a wide range state-of-the-art building energy technologies, with the intention to minimise energy use, improve thermodynamic performance as well as internal building thermal conditions with minimal life cycle cost increase. Overall, the main findings from this study confirmed the positive influence that the sea-land breeze effect could have when it is correctly adapted to the building design, as it improves the building’s thermodynamic and thermal comfort performance. In the case study, wind and solar resources have been essential to improve most of the objective functions. On average, it was found that an optimal orientation, solar shading and ventilation flow control decreased thermal discomfort hours and increased thermal set-points of AC equipment by an average of $1.5^\circ$. On the other hand, solar collectors have been the most cost-effective solutions to cover hot water demand throughout the year. This could have significant carbon emissions and exergy consumption footprints reductions in the region by decreasing the demand of grid electricity, LPG and natural gas.
An equal weight design solution, where all objective functions were equally considered, reduced thermal discomfort to almost zero as well as one-tenth of total exergy consumption, whilst increasing life cycle cost by less than 20%. The main strength of a combined exergy and economic optimisation is the ability to thermodynamically and economically improve the design by reducing unnecessary irreversibilities in a cost-effective way. Other important objectives such as indoor air quality should be explored, especially for coastal housing located in the tropics where high indoor humidity can be expected. Poor humidity control could cause high levels of condensation, deteriorating indoor air quality and living standards.

For future work, other passive and active cooling strategies will be explored. Specifically, solar chimneys, trombe walls, desiccant cooling systems, intermittent absorptive solar-cooling systems, and absorption solar cooling are of interest. Furthermore, urban level optimisation would be conducted by applying the framework at a district level. Different levels of feed-in-tariffs and renewable generation incentives would be considered to find optimal values that could unlock low-energy designs with high exergy-efficiency. Finally, it is intended to include carbon and exergetic life cycle analysis to understand the impact of embodied carbon and exergy footprint on construction materials and equipment.

5. Acknowledgements

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Nomenclature

Abbreviations

1P single-pane window
2P double-pane window
3P triple-pane window
AGEL aerogel
ASHP air source heat pump
CellG cellular glass
CFL compact fluorescent lamps
COP coefficient of performance
CorkB cork board
DHW domestic hot water
EPS expanded polystyrene
GFibre glass fibre
GSHP: ground source heat pump
HVAC: heating, ventilation and air conditioning
HX: heat exchanger
IEQ: indoor environmental quality
LED: light emitting diode
PHEN: phenolic foam board
PMV: predicted mean vote index
PUR: polyurethane
PV: photovoltaic
TARP: thermal analysis research program
UHI: urban heat island
VAV: variable air volume
XPS: extruded polystyrene

Greek symbols

\( \alpha \) wind speed profile exponent [-]
\( \alpha_j \) Chebyshev distance [-]
\( \Delta \) differential
\( \delta \) wind speed profile boundary layer thickness [-]
\( \eta \) energy efficiency [%]
\( \psi \) exergy efficiency [%]
\( \rho \) outdoor air density [kg m\(^{-3}\)]

Nomenclature

\( \dot{m} \) mass flow rate [kg s\(^{-1}\)]
\( A_{opening} \) opening area [m\(^2\)]
\( C_p \) specific heat coefficient [1.007 kJ kg\(^{-1}\)K\(^{-1}\)]
\( c_{p,heat} \) specific heat [J K\(^{-1}\)]
\( C_w \) opening effectiveness [dimensionless]
\( En \) energy [kWh]

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\begin{itemize}
  \item \textbf{Ex} \quad \text{exergy [kWh]}
  \item \textbf{F}_{\text{schedule}} \quad \text{open area fraction [m]}
  \item \textbf{G} \quad \text{incident solar radiation [W m}^2]\]
  \item \textbf{g} \quad \text{gravitational acceleration [9.81 m s}^{-2}\]
  \item \textbf{LCC} \quad \text{life cycle cost [US$]}
  \item \textbf{Q}_w \quad \text{volumetric air flow rate [m}^3\text{s}^{-1}\]
  \item \textbf{T}_0 \quad \text{outdoor temperature [deg]}
  \item \textbf{T}_i \quad \text{inside temperature [deg]}
  \item \textbf{U}_{\text{value}} \quad \text{thermal transmittance [W m}^{-2}\]
  \item \textbf{V} \quad \text{wind speed at altitude z [m s}^{-1}\]
  \item \textbf{Z} \quad \text{objective function}
  \item \textbf{C}_{e\text{n}} \quad \text{annual energy cost [US$]}
  \item \textbf{C}_n \quad \text{capital cost [US$]}
  \item \textbf{CF}_n \quad \text{annual cash flow [US$ y}^{-1}\]
  \item \textbf{F}_p \quad \text{fuel primary energy factor [-]}
  \item \textbf{F}_q \quad \text{fuel quality factor [-]}
  \item \textbf{O&\text{M}_n} \quad \text{operation and maintenance cost [US$]}
  \item \textbf{r}_d \quad \text{discount rate [%]}
\end{itemize}\vspace{1em}

\textbf{Subscripts and superscripts}
\begin{itemize}
  \item \textit{appl} \quad \text{appliances}
  \item \textit{arg} \quad \text{argon}
  \item \textit{col} \quad \text{solar collector}
  \item \textit{cons} \quad \text{consumption}
  \item \textit{cook} \quad \text{cooking}
  \item \textit{dem} \quad \text{demand}
  \item \textit{f} \quad \text{fuel type f}
  \item \textit{i} \quad \text{thermal zone i}
  \item \textit{krp} \quad \text{krypton}
\end{itemize}

30
meteorological station

number of thermal zones

primary energy

refrigeration

ventilation

height above ground of the wind speed sensor [m]

References


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Appendix A: Exergy analysis within ExRET-Opt

The building thermal exergy method used in ExRET-Opt is mainly based on the developments proposed by Schmidt [97] and Torio [98]. Originally, the method used an input-output approach based on seven different subsystems (only thermal systems) to calculate exergy consumption throughout the energy supply chain. In addition, EXRET-Opt is also capable of calculating exergy use throughout the DHW system level, refrigeration, cooking, and all electric-based equipment, thus allowing for a holistic exergy assessment. This holistic method provides comprehensive
means by which to understand the interactions between the building envelope and the building energy services. Figure A.1 presents the 11 subsystems and 13 exergy flows analysed in the tool.

Figure A.1: Energy supply chain and subsystems for exergy calculations. Based on the IEA ECB Annex 49 method calculation.

The basic formulas for guidance are presented in the following section; however, a complete assessment of exergy analysis covering all the end-use services can be found in García Kerdan et al. [73].

A.1. Building exergy analysis

A.1.1. Exergy demand

The total exergy demand at the building level \( E_{x_{dem,bui}} \) is obtained by adding all the demands for each end-use (VI. cooling and heating, IX. domestic hot water, and XI. appliances):

\[
E_{x_{dem,bui}}(t_k) = \sum_{i=1}^{i} E_{x_{dem,enduse,i}}(t_k)
\]  

(A.1)

where \( E_{x_{dem,enduse}} \) is the exergy demand by end-use \( i \).

Exergy demand for cooling purposes considering the effect of natural ventilation is calculated as showed in equation 3. For the rest of end use services, exergy demand is calculated as follows:

- Domestic hot water:
\[ Ex_{dem,DHW}(t_k) = E_{DHW}(t_k) \times \frac{\eta_{DHW}(t_k)}{F_q} \times \left(1 - \frac{T_0(t_k)}{T_{HW}(t_k)} \ln \frac{T_{HW}(t_k)}{T_0(t_k)}\right) \] (A.2)

where \( E_{DHW}(t_k) \) is the domestic hot water energy demand, \( \eta_{DHW} \) is the DHW equipment efficiency, \( q_{fuel} \) is the quality factor of the energy source used, and \( T_{HW} \) is the hot water temperature.

-Cooking:

\[ Ex_{dem,cook}(t_k) = E_{cook}(t_k) \times \frac{\eta_{cook}(t_k)}{q_{fuel}} \times \left(1 - \frac{T_0(t_k)}{T_{cook}(t_k)}\right) \] (A.3)

where \( E_{cook}(t_k) \) is the cooking energy demand, \( \eta_{cook} \) is the cooking equipment efficiency, and \( T_{cook}(t_k) \) is the cooking temperature. Depending on the energy source (electricity, LPG or natural gas), \( q_{fuel} \) might vary.

-Refrigeration:

\[ Ex_{dem,ref}(t_k) = E_{ref}(t_k) \times \text{COP}_{ref}(t_k) \times \left(\frac{T_0(t_k)}{T_{ref}(t_k)} - 1\right) \] (A.4)

where \( E_{ref} \) is the energy demand for refrigeration, \( \text{COP}_{ref} \) is the refrigerators coefficient of performance, and \( T_{ref} \) is the refrigerators working temperature.

-Appliances

Most electric-based equipment is considered to have the same exergy and energy efficiency values.

\[ Ex_{dem,el,appl}(t_k) = E_{dem,el,appl}(t_k) \times F_{q,elec} \] (A.5)

where \( E_{dem,el,appl}(t_k) \) is the energy demand for the electric-based equipment, and \( F_{q,elec} \) is the quality factor of electricity (Table A.1).

A.1.2. Primary exergy analysis

After calculating total exergy demand, the model calculates exergy consumption at each subsystem level until reaching the start of the supply chain (I. Primary Energy Transformation). Exergy equations at subsystem level can be found elsewhere ([57], [73])

For primary exergy (\( Ex_{prim} \)) at the primary energy transformation (subsystem I. in Figure A.1) is calculated as follows:

\[ Ex_{prim}(t_k) = \sum_{i=1}^{i} \left[ \frac{E_{gen,i}(t_k)}{\eta_{gen,i}(t_k)} \times F_{p,source,i} \times F_{q,source,i} \right] + \left[ Ex_{dem,el,appl} \times F_{p,elec} \right] \] (A.6)

where, \( E_{gen} \) is the energy source used by the building HVAC, DHW, cooking or refrigeration system, \( \eta_{gen} \) is the system efficiency, \( F_{p,source} \) is the fuel primary energy factor and \( F_{q,source} \) is the fuel quality factor (Table 2).
### Table A.1: Primary Energy Factors and Quality Factors by energy sources \[36,45\]

<table>
<thead>
<tr>
<th>Energy source</th>
<th>Primary energy factor ([\text{kWh/kWh}])</th>
<th>Quality factor ([\text{kWh}<em>{\text{ex}}/\text{kWh}</em>{\text{en}}])</th>
</tr>
</thead>
<tbody>
<tr>
<td>Natural gas</td>
<td>1.11</td>
<td>0.94</td>
</tr>
<tr>
<td>Electricity (Grid supplied)</td>
<td>2.58</td>
<td>1</td>
</tr>
<tr>
<td>District Energy</td>
<td>1.11</td>
<td>0.94</td>
</tr>
<tr>
<td>Oil</td>
<td>1.07</td>
<td>1</td>
</tr>
<tr>
<td>Biomass (Wood pellets)</td>
<td>1.2</td>
<td>1.05</td>
</tr>
</tbody>
</table>

If primary exergy comes from renewable sources and equipment this require a different exergy analysis from conventional systems as demonstrated by Torio et al. \[99\] While PV panels are regarded to have the same exergetic efficiency as its first law counterpart, for solar collectors is necessary a special assessment. To calculate the exergy of the incoming solar radiation to the equipment the following formula is used:

\[
E_{x_{\text{sun}}} (t_k) = G(t_k) \ast A_{col} \ast \left(1 - \frac{T_0(t_k)}{T_{\text{sun}}(t_k)}\right)
\] (A.7)

where \(G\) is the incident solar radiation, \(A_{col}\) is the collector surface area, \(T_0\) is the reference environment, and \(T_{\text{sun}}\) is the suns temperature, which is considered around 6000 K. This can be regarded as the first exergy input for the energy supply chain. Later, the output of the collector can be calculated as follows:

\[
E_{x_{\text{col}}} (t_k) = \dot{m}(t_k) \ast c_{p,\text{heat}} \ast \left[\left(T_{\text{out}}(t_k) - T_0(t_k) - T_{\text{in}}(t_k) \ast \ln\frac{T_{\text{out}}(t_k)}{T_{\text{in}}(t_k)}\right)\right]
\] (A.8)

where \(\dot{m}(t_k)\) is the mass flow rate \([\text{kg s}^{-1}]\), \(c_{p,\text{heat}}\) is the carrier specific heat \([\text{J K}^{-1}]\), \(T_{\text{out}}\) is the temperature provided by the collector, and \(T_{\text{in}}\) the return temperature to the collector. Finally, the exergy efficiency for solar collectors is obtained as follows:

\[
\psi_{\text{col}}(t_k) = \frac{E_{x_{\text{col}}}(t_k)}{E_{x_{\text{sun}}}(t_k)}
\] (A.9)

Finally, to calculate the total exergy consumed in the building supply chain, the following equation is used:

\[
E_{x_{\text{cons,bui}}}(t_k) = E_{x_{\text{prim}}}(t_k) - E_{x_{\text{dem,bui}}}(t_k)
\] (A.10)

### Appendix B: NSGA-II optimisation process

ExRET-Opt approaches multi-objective optimisation by using a Non-Dominated Sorting Genetic Algorithm (NSGA-II), based on Charles Darwin’s theory on evolution. Each of the building designs (or chromosomes) are composed of a set of design parameters (or genes). The selection of specific designs is undertaken through the ‘survival of the fittest’ principle, highlighting those that are closer to the desired objective(s). The most frequent design parameters located in the best designs often go through to the next generation, where new building designs with some (not all) characteristics have a better chance to be modelled. To avoid convergence into similar design parameters, the model simulates variability and recombination processes as some ‘good’ solutions
might have been lost in previous generations. Figure B.1 illustrates this process and the related software used in ExRET-Opt.

Figure B.1: Genetic algorithm optimisation process applied in ExRET-Opt[73]
Appendix C: Distributions of solar shading devices

Figure C.1: Distribution (bars) and the fitted probability distribution (lines) of solar shading for the constrained solutions