Electronic Supporting Information

The influence of nitrogen position on charge carrier mobility in enantiopure aza[6]helicene crystals

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General procedure
The charge hopping rate from molecule $i$ to $k$ is given by the Marcus equation:\textsuperscript{1}

$$\Gamma_{ik} = \frac{|J_{ik}|^2}{\hbar} \sqrt{\frac{\pi}{\lambda K_b T}} \exp \left\{ -\frac{\left(\Delta E_{ik} + \lambda\right)^2}{4 \lambda K_b T} \right\}$$

$J_{ik}$ is the transfer integral, $\Delta E_{ik}$ is the change in energy between molecules $i$ and $k$, and $\lambda$ is the reorganisation energy. The reorganisation energy is the sum of the energy cost associated with the rearrangement of the molecules involved in the hop and their surroundings, respectively called inner ($\lambda_{in}$) and outer ($\lambda_{ou}$) reorganisation energies. $\lambda_{in}$ is calculated with the 4-point method:\textsuperscript{2}

$$\lambda_{in} = (E_{n}^{+/0} - E_{c}^{+/0} + E_{c}^{0} - E_{n}^{0})$$

The superscript $+/-$ and 0 indicate the charged and neutral systems respectively and the subscript $n$ and $c$ indicate that the energy is calculated at the neutral or charged molecular geometry. The outer reorganisation energy is harder to quantify, so was approximated to 0.3 eV for all the structures studied. As the maximum transfer integral found was $\approx$0.07 eV and $\lambda$ was always higher than 0.4 eV, the assumption of weak coupling ($J \ll \lambda$) was valid. For all structures studied, the maximum transfer integral was less than 0.1 eV.

The change in energy between the sites is:

$$\Delta E_{ik} = \varepsilon_i - \varepsilon_k - qF \cdot r_{ik}$$

where $\varepsilon_i$ and $\varepsilon_k$ are the energies of frontier orbitals for molecule $i$ and $k$ respectively, $q$ is the charge on an electron, $F$ is the field vector and $r_{ik}$ is the distance vector between sites $i$ and $k$. As we do not include energetic disorder in the model, $\varepsilon_i = \varepsilon_k$ and the only contribution to $\Delta E_{ik}$ is given by the electric field. The angular dependent mobility was found with this method by applying a field of strength 10000 V cm$^{-1}$ at 10 degree intervals in each of the 3 planes. To obtain a mobility from the set of rates, we used a Master equation approach:\textsuperscript{3}

$$\frac{dP_k}{dP_i} = \sum_{i \neq k} \left[ \Gamma_{ik} P_i(t) - \Gamma_{ki} P_k(t) \right]$$

$P_k$ is the probability of site $k$ being occupied by a charge and $\Gamma_{ik}$ is the rate of hopping between sites $i$ and $k$. The equation is valid in the low charge limit. By considering a matrix $A$ defined as:

$$A_{ik} = \begin{cases} \Gamma_{ik}, & i \neq k \\ -\sum_{i \neq k} \Gamma_{ik}, & i = k \end{cases}$$

The master equation can be solved in steady state with $AP = 0$. The average velocity of charges can then be found through the steady state probabilities:

$$v = \sum_{i \neq k} \Gamma_{ik} A_{ik} P_k$$

The last step is to calculate the charge mobility:

$$\mu = \frac{\bar{v}}{F}$$
$ar{v}$ is the average velocity of the charges in the direction of the field and $F$ is the magnitude of the field.
Crystal cell similarity

<table>
<thead>
<tr>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>a (Å)</td>
<td>7.214</td>
<td>7.293</td>
<td>7.256</td>
<td>7.344</td>
<td>7.277</td>
<td>0.055</td>
</tr>
<tr>
<td>b (Å)</td>
<td>13.058</td>
<td>12.979</td>
<td>13.028</td>
<td>13.156</td>
<td>13.055</td>
<td>0.074</td>
</tr>
<tr>
<td>c (Å)</td>
<td>17.660</td>
<td>17.368</td>
<td>17.234</td>
<td>17.511</td>
<td>17.443</td>
<td>0.183</td>
</tr>
</tbody>
</table>

Table S1. Lengths of the (aza)[6]helicene enantiopure cells reported in the Cambridge Structural Database (CSD). Space group is always P2_12_12_1. Mean and standard deviation are reported to show the small differences between the crystal structures.

**Figure S1.** Overlay of HEXHEL (green) and PIHDOB (grey) crystal structures sharing the same supramolecular packing.
Geometrical Parameters

Figure S2. Plots of [6]helicenes geometrical parameters. (a) Pitch defined as distance between C1 and C16 (black dots) and distance between C2 and C15 (blue dots). (b) Interplanar angle between terminal rings (red dots) and between 2° and 5° ring (cyan dots). The variations over the series are quite small. The only exceptions occur when nitrogen is in position 1 because of the reduced steric hindrance given by the removed C-H bond(s).
**Molecular Orbitals**

<table>
<thead>
<tr>
<th></th>
<th>Carbo</th>
<th>1-aza</th>
<th>2-aza</th>
<th>3-aza</th>
<th>4-aza</th>
<th>1,16-diaza</th>
<th>5-aza</th>
<th>6-aza</th>
<th>7-aza</th>
<th>8-aza</th>
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</thead>
<tbody>
<tr>
<td><strong>LUMO</strong></td>
<td><img src="image1" alt="Image" /></td>
<td><img src="image2" alt="Image" /></td>
<td><img src="image3" alt="Image" /></td>
<td><img src="image4" alt="Image" /></td>
<td><img src="image5" alt="Image" /></td>
<td><img src="image6" alt="Image" /></td>
<td><img src="image7" alt="Image" /></td>
<td><img src="image8" alt="Image" /></td>
<td><img src="image9" alt="Image" /></td>
<td><img src="image10" alt="Image" /></td>
</tr>
<tr>
<td><strong>HOMO</strong></td>
<td><img src="image11" alt="Image" /></td>
<td><img src="image12" alt="Image" /></td>
<td><img src="image13" alt="Image" /></td>
<td><img src="image14" alt="Image" /></td>
<td><img src="image15" alt="Image" /></td>
<td><img src="image16" alt="Image" /></td>
<td><img src="image17" alt="Image" /></td>
<td><img src="image18" alt="Image" /></td>
<td><img src="image19" alt="Image" /></td>
<td><img src="image20" alt="Image" /></td>
</tr>
</tbody>
</table>

**Figure S3.** HOMO and LUMO orbitals for three of the isomers studied (isovalue 0.02). The HOMO is clearly localized far from the pyridinic ring in 1-aza and close to it in 7-aza. The opposite is true for LUMOs. In 8-aza, there is no big change between HOMO and LUMO in terms of localization areas. the carbo[6]helicene and 1,16-diaza, as they are C2 symmetric, do not show differences between two sides of the helicene. Nitrogen atoms are shown in blue.
Additional plots

Figure S4. Calculated properties for the hypothetical aza[6]helicene cells studied. The number of the x-axis entries indicates the position of the nitrogen in the aza[6]helicene scaffold. The entries C and 1,16 indicate the carbo[6]helicene (no nitrogen) and the 1,16-diaza[6]helicene, respectively. (a) Maximum transfer integral (b) The ratio between the maximum and minimum mobility as an indication of anisotropy. (c) The normalised standard deviation of anisotropy (i.e. divided by maximum mobility) as another indication of charge carrier anisotropy.
Figure S5. Average hole (a) and electron (b) mobility for cells containing helicene isomers with opposite occupancy. Maximum hole (c) and electron (d) mobility for cells containing helicene isomers with opposite occupancy.
Figure S6. Max transfer integrals (J) against (a) Average mobility and (b) Maximum mobility. Average mobility against transfer integrals for each dimer motif (c,d). Normalised standard deviation against average mobility (e).
Figure S7. HOMO-HOMO and LUMO-LUMO transfer integrals for all the dimers in all the hypothetical cells studied (from 1-aza to 16-aza) plotted against the nitrogen-nitrogen distance.

Figure S8. Transfer integral values against the shortest intermolecular distance (C···C or C···N) for the interlocked motif in all the monoaza[6]helicene crystal cells studied.
Table S2. Charge mobility related properties for the aza[6]helicenes analysed in this work. The anisotropy here is calculated as normalised standard deviation of the direction-dependent charge mobility. The best (worst) values are highlighted in green (orange), assuming the best values correspond to high mobility and low anisotropy.

| Aza-$x$ isomer | HOLE | | | | ELECTRON | | | | | |
|----------------|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|-----|
|                | Min $\mu$ (cm$^2$/Vs) | Max $\mu$ (cm$^2$/Vs) | Average $\mu$ (cm$^2$/Vs) | Anisotropy (cm$^2$/Vs) | $\lambda_\in$ (meV) | Min $\mu$ (cm$^2$/Vs) | Max $\mu$ (cm$^2$/Vs) | Average $\mu$ (cm$^2$/Vs) | Anisotropy (cm$^2$/Vs) | $\lambda_\in$ (meV) |
| C              | 0.040 | 0.180 | 0.092 | 0.276 | 159 | 0.042 | 0.297 | 0.149 | 0.294 | 160 |
| 1              | 0.004 | 0.017 | 0.010 | 0.257 | 199 | 0.087 | 0.220 | 0.151 | 0.182 | 171 |
| 2              | 0.013 | 0.033 | 0.022 | 0.202 | 180 | 0.029 | 0.085 | 0.058 | 0.213 | 217 |
| 3              | 0.002 | 0.025 | 0.011 | 0.337 | 170 | 0.039 | 0.206 | 0.109 | 0.278 | 189 |
| 4              | 0.010 | 0.016 | 0.012 | 0.119 | 210 | 0.026 | 0.26  | 0.100 | 0.301 | 167 |
| 5              | 0.013 | 0.020 | 0.016 | 0.119 | 216 | 0.018 | 0.046 | 0.035 | 0.203 | 224 |
| 6              | 0.018 | 0.066 | 0.040 | 0.241 | 182 | 0.034 | 0.081 | 0.063 | 0.198 | 198 |
| 7              | 0.038 | 0.203 | 0.099 | 0.285 | 206 | 0.007 | 0.054 | 0.030 | 0.281 | 245 |
| 8              | 0.013 | 0.046 | 0.035 | 0.261 | 159 | 0.019 | 0.254 | 0.112 | 0.326 | 187 |
| 9              | 0.012 | 0.052 | 0.032 | 0.250 | 159 | 0.017 | 0.193 | 0.091 | 0.313 | 187 |
| 10             | 0.015 | 0.022 | 0.018 | 0.110 | 206 | 0.020 | 0.031 | 0.026 | 0.112 | 245 |
| 11             | 0.046 | 0.209 | 0.104 | 0.280 | 182 | 0.020 | 0.128 | 0.070 | 0.279 | 198 |
| 12             | 0.032 | 0.159 | 0.078 | 0.285 | 216 | 0.009 | 0.080 | 0.037 | 0.315 | 224 |
| 13             | 0.033 | 0.160 | 0.078 | 0.286 | 210 | 0.031 | 0.248 | 0.120 | 0.302 | 167 |
| 14             | 0.047 | 0.256 | 0.126 | 0.285 | 170 | 0.031 | 0.204 | 0.108 | 0.284 | 189 |
| 15             | 0.050 | 0.241 | 0.117 | 0.286 | 180 | 0.013 | 0.137 | 0.063 | 0.314 | 217 |
| 16             | 0.035 | 0.230 | 0.110 | 0.294 | 199 | 0.024 | 0.185 | 0.086 | 0.310 | 171 |

1,16 | 0.005 | 0.111 | 0.043 | **0.356** | **147** | 0.077 | 0.228 | **0.158** | **0.211** | **147** |
Single motif transfer integrals $J$ for the whole series

**HOLE**

**ELECTRON**
Mobility angular distribution plots

Figures S10. Angular distribution of the mobility in the three orthogonal planes for hole (blue) and electron (red) transport. Please note that the scale is set at the maximum mobility value, which is different for every isomer.

Carbo[6]helicene

\(ab\) plane

\(ac\) plane

\(bc\) plane
1-aza[6]helicene

$ab$ plane

$ac$ plane

$bc$ plane
2-aza[6]helicene

ab plane

ac plane

bc plane
3-aza[6]helicene

ab plane

ac plane

bc plane
4-aza[6]helicene

\textit{ab} plane

\textit{ac} plane

\textit{bc} plane
5-aza[6]helicene

**ab plane**

**ac plane**

**bc plane**
6-aza[6]helicene

**ab plane**

**ac plane**

**bc plane**
7-aza[6]helicene

*ab* plane

*ac* plane

*bc* plane
8-aza[6]helicene

*ab* plane

*ac* plane

*bc* plane
9-aza[6]helicene

ab plane

ac plane

bc plane
10-aza[6]helicene

**ab plane**

**ac plane**

**bc plane**
11-aza[6]helicene

*ab* plane

*ac* plane

*bc* plane
12-aza[6]helicene

$ab$ plane

$ac$ plane

$bc$ plane
13-aza[6]helicene

$ab$ plane

$ac$ plane

$bc$ plane
14-aza[6]helicene

\(ab\) plane

\(ac\) plane

\(bc\) plane
15-aza[6]helicene

*ab* plane

*ac* plane

*bc* plane
16-aza[6]helicene

*ab* plane

*ac* plane

*bc* plane
1,16-diaza[6]helicene

$ab$ plane

$ac$ plane

$bc$ plane
References