Modification of the order of the magnetic phase transition in cobaltites without changing their crystal space group

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It has been found that GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6-δ}$ can exhibit consecutive magnetic transitions: antiferromagnetic-ferromagnetic (AFM-FM) transition followed by ferromagnetic-paramagnetic transition (FM-PM), which give rise to a coexistence of inverse and conventional magnetocaloric effect (MCE), respectively. In the pristine compound (x=0), its AFM-FM transition is shown to belong to a first-order phase transition and the FM-PM to a second-order type. Despite it is widely known that the properties of cobaltites are highly influenced by their oxygen content and type of doping carriers, in this work, further evaluation using magnetocaloric analysis (universal curve method and a quantitative criterion using magnetic field dependence of the magnetic entropy change) reveals that the first-order AFM-FM phase transition converts into a second-order character with just Sr doping of x=0.1 (despite of having the same space group at room temperature and type of dopant carrier as x=0), severely affecting its thermomagnetic properties. Moreover, the peaks of these two MCE span over a temperature range that is larger than those reported for cobaltite-type materials, making it closer to room temperature applications.
1 Introduction

Ln$_{1-x}$A$_x$CoO$_{3-\delta}$ perovskite cobaltites (Ln: lanthanides, A: alkaline-earth metals) are known for their applications in magnetodielectric materials, solid oxide fuel cells, electrocatalytic activity as well as giant magnetoresistance effects etc.\textsuperscript{1-6}. Their performance is related to details of their phase transitions, which can also be highly compositional dependent.\textsuperscript{7} The oxygen content (3-\delta) is mainly dictated by the dopant level x (Ln$^{3+}$ + $\frac{1}{2}$ O$^{2-}$ $\rightarrow$ A$^{2+}$ + $\frac{1}{2}$ $\square$) and partitioning of Co$^{2+}$/Co$^{3+}$/Co$^{4+}$, leading to the possibility of electron or hole doping into the systems.\textsuperscript{8} Among Ln$_{1-x}$A$_x$CoO$_3$ cobaltites, the ordered oxygen vacancy double perovskite, GdBaCo$_2$O$_{6-\delta}$ (Fig. 1) exhibits thermomagnetic transitions and properties that are dependent on their \( \delta \) values: for \( \delta > 0.5 \), it corresponded to electron doping while \( \delta < 0.5 \) to hole doping.\textsuperscript{9} Recently, it has been reported that Sr doping in GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6-\delta}$ led to an improvement in conductivity due to the effects of hole doping from lowered oxygen deficiency with increasing Sr content.\textsuperscript{10}

Fig. 1: Crystal structure representation of (a) a single perovskite ABO$_3$, where A (green) is located in the centre of corner-connected BO$_6$ octahedra (blue); (b) an ordered perovskite AA’B$_2$O$_6$, where A (green) and A’ (purple) stack in an alternate sequence along z-crystallographic axis with corner-connected BO$_6$ octahedra shown in brown, for example GdBaCo$_2$O$_6$; (c) defective ordered perovskite AA’B$_2$O$_{6-\delta}$, where the vacancy of oxygen (\( \delta \), red) is preferentially created in the xy-plane in the A’ layer.
Similar compounds, like manganites, have been reported as potential magnetocaloric material candidates. Their doping dependencies on their phase transitions, transition temperatures as well as the temperature range of magnetic refrigeration have been widely reported\textsuperscript{11}, similar to perovskite cobaltites. There are only very few magnetocaloric effect (MCE) studies in cobaltites, which are usually focused on La\textsubscript{1-x}Sr\textsubscript{x}CoO\textsubscript{3}, Pr\textsubscript{1-x}Sr\textsubscript{x}CoO\textsubscript{3} and Nd\textsubscript{1-x}Sr\textsubscript{x}CoO\textsubscript{3} systems\textsuperscript{12-14}. However, reports on cobaltites with Ln=Gd are scarce, whereby only one study reports theoretical simulations of Gd\textsubscript{1-x}Ca\textsubscript{x}BaCo\textsubscript{2}O\textsubscript{5.5}\textsuperscript{15} while experimental results were shown only for Gd\textsubscript{0.7}Sr\textsubscript{0.3}CoO\textsubscript{3} (both with Ln=Gd), and none in particular about GdBa\textsubscript{1-x}Sr\textsubscript{x}Co\textsubscript{2}O\textsubscript{6-δ}. In addition, the latter’s thermomagnetic behavior and the magnetic field dependence of any magnetocaloric response have not been reported.

In this work, we aim to use magnetocaloric studies to further evaluate these materials, which reveal that Sr substitutions can drastically alter the magnetic behavior and its phase transitions. In particular, we have found that the pristine sample exhibits an inverse MCE then closely accompanied by a conventional MCE, whereby the former arises from the first-order antiferromagnetic-ferromagnetic (AFM-FM) phase transition and the latter from a ferromagnetic-paramagnetic (FM-PM) transition. The inverse MCE of this material has not been reported as the only related work, theoretical simulations on Gd\textsubscript{1-x}Ca\textsubscript{x}BaCo\textsubscript{2}O\textsubscript{5.5}\textsuperscript{15}, report solely on the conventional MCE. The relatively similar cobaltite (which is not a double pervoskite), Gd\textsubscript{0.7}Sr\textsubscript{0.3}CoO\textsubscript{3}, showed a conventional MCE at 10 K (magnetic entropy change of ∆S\textsubscript{M}~ -12 J kg\textsuperscript{-1} K\textsuperscript{-1} for 5 T)\textsuperscript{16}, which is at much lower temperatures than our results. In the current paper, two types of MCE are observed, with both inverse and conventional MCE responses occurring at higher temperatures (175 – 277 K) that could be useful for paving the ground to discover new materials with potentially more alternative applications than room temperature magnetic refrigeration. Collectively, our findings show that magnetocaloric studies are useful to offer insight into the magnetic behavior of doped perovskites, as they reveal an alteration of the order of phase transition with just minor Sr doping of x=0.1 despite the sample exhibiting same room temperature crystal symmetry and electron doping carrier as the pristine or undoped sample. Therefore, with apparently the same typical influences on the properties of cobaltites, their behavior can be severely affected.
2 Experimental

The GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6.5}$ powders were synthesized via a solid-state reaction whereby stoichiometric amounts of Gd$_2$O$_3$ (Alfa Aesar, 99.99%), BaCO$_3$ (Alfa Aesar, 99.8%), SrCO$_3$ (Alfa Aesar, 99.99%) and Co$_3$O$_4$ (Alfa Aesar, 99.7%) starting powders were mixed and ground without pre-calcination. They were sintered at 1100 °C for 60 h in static air with intermediate grinding for intervals of 12 h. Their measured compositions, quantified using electron probe microanalysis (JEOL JXA-8530F equipped with five wavelength dispersive spectrometers), were within the standard deviation of the nominal values. In this work, the samples are denoted by their Sr content (i.e. $x = 0 – 0.5$) as: Sr0, Sr1, Sr2, Sr3, Sr4 and Sr5 respectively. The Rietveld analyses of powder X-ray diffraction results showed that high Sr content led to crystallization in higher symmetry in the crystal structures: (i) the starting orthorhombic symmetry with $Pmnm$ space group with doubling in $b$- and $c$-axes for Sr0 and Sr1 samples (Rietveld refinement of Sr1 is shown in Fig. 2 as an example, wherein $2\theta_{001} = 11.73^\circ$ indicates the doubling in $c$, and $2\theta_{010} = 11.33^\circ$, $2\theta_{130} = 41.79^\circ$ and $2\theta_{131} = 43.56^\circ$ indicate the doubling in $b$) was transformed into (ii) $Pmmn$ with only doubling in $c$-axis (Sr2 and Sr3), then into (iii) tetragonal $P4/mmm$ (Sr4 and Sr5)\(^{10}\). The oxygen content calculated from the Co valence ($V_{Co}$) from iodometric titration reveals that the oxygen deficiency decreases as Sr replaces Ba, with $\delta=0.45(1)$ found for Sr5 (for all compositions, $V_{Co}$ values are summarized in Table 1). In addition, the calculations from the bond valence sum (BVS) analysis of cobalt-oxygen bonds (which indicates the bond strength in ionic compounds) were in agreement with the results from iodometric titration. Further details of the structural characterization and analysis, for both bulk and surface, are published elsewhere\(^ {10}\).
Fig. 2: Rietveld refinement of the XRD data of Sr1 sample performed at room temperature using Cu $K_{\alpha}$ radiation ($R_{wp} = 0.029, R_{Bragg} = 0.009$). The doubling in its $c$-axis is indicated by $2\theta_{001} = 11.73^\circ$ and its doubling in $b$ by $2\theta_{010} = 11.33^\circ, 2\theta_{130} = 41.79^\circ$ and $2\theta_{131} = 43.56^\circ$.

Table 1. Oxygen content and cobalt valence states in GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6-\delta}$

<table>
<thead>
<tr>
<th>Sr content (x)</th>
<th>Sample</th>
<th>Oxygen content (6-\delta)</th>
<th>Cobalt Valence (V$_{Co}$)</th>
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</thead>
<tbody>
<tr>
<td>x = 0</td>
<td>Sr0</td>
<td>5.21 (1)</td>
<td>2.71 (1)</td>
</tr>
<tr>
<td>x = 0.1</td>
<td>Sr1</td>
<td>5.28 (1)</td>
<td>2.78 (1)</td>
</tr>
<tr>
<td>x = 0.2</td>
<td>Sr2</td>
<td>5.38 (1)</td>
<td>2.88 (1)</td>
</tr>
<tr>
<td>x = 0.3</td>
<td>Sr3</td>
<td>5.51 (1)</td>
<td>3.01 (1)</td>
</tr>
<tr>
<td>x = 0.4</td>
<td>Sr4</td>
<td>5.54 (1)</td>
<td>3.04 (1)</td>
</tr>
<tr>
<td>x = 0.5</td>
<td>Sr5</td>
<td>5.55 (1)</td>
<td>3.05 (1)</td>
</tr>
</tbody>
</table>

The magnetic field dependence of magnetization $M(H)$ was characterized using a Lakeshore 7407 vibrating sample magnetometer using a maximum applied field of 15 kOe. For magnetocaloric studies, each sample was first heated in zero field to temperatures up to 350 K, cooled in zero field to the measurement temperature and the subsequent $M(H)$ isotherms were measured with increasing
field using a discontinuous protocol. Isothermal magnetization curves for samples Sr0 and Sr1 are shown in Figure 3.

![Isothermal magnetization curves for samples Sr0 and Sr1.](image-url)

Fig. 3: Field dependence of magnetization measured at different temperatures for samples Sr0 and Sr1.

The magnetic entropy change ($\Delta S_M$) due to the application of a magnetic field was calculated by:

$$\Delta S_M = \mu_0 \int_0^H \left( \frac{\partial M}{\partial T} \right)_H dH$$  \hspace{1cm} (1)

from the processing of the experimental temperature and field dependent magnetization data using the magnetocaloric effect analysis program from LakeShore Cryotronics. The calculation of $\Delta S_M$ from this discontinuous measurement protocol avoids spurious results irrespective of the order of the phase transition.

The magnetic field dependence of $\Delta S_M$ follows a power law expression:

...
\[ \Delta S_M \propto H^n, \]  
where its exponent \( n \) (field and temperature dependent) can be locally calculated using:

\[ n = \frac{d \ln |\Delta S_M|}{d \ln H}. \]  

3 Results and discussion
The \( M(T) \) zero field cooling and field cooling curves in Fig. 4 show that the GdBa\(_{1-x}\)Sr\(_x\)Co\(_2\)O\(_{6.5}\) samples exhibit more than one magnetic phase transition. The pristine sample, Sr0, (which crystallized in \( Pmmm \) orthorhombic symmetry with doubling in \( b- \) and \( c- \) axes) exhibits an AFM-FM transition around 240 K and a FM-PM transition around 275 K. This leads to a narrow FM region observed for all the measured fields (up to \( \sim 37 \) K for up to 500 Oe), which is analogous to results found in the literature \(^{20,21}\). With minor Sr doping, Sr1 (maintaining the identical space group as undoped Sr0 at room temperature) shows a lowered transition temperature of AFM-FM (\( T_{AFM-FM} \)) while retaining \( T_{FM-PM} \). In this case, its FM window is expanded, as can be seen from the broader magnetization maximum in Fig. 4(a). Furthermore, the abrupt slope at \( T_{AFM-FM} \) observed in Sr0 converts into a gradual one (for Sr1) and was smeared out with higher Sr doping (\( x \geq 0.2 \)). Although Sr2 crystallizes in \( Pmmm \) symmetry (similar to Sr0 and Sr1), it retains only the doubling in \( c- \) axis (losing the doubling in \( b \)) and shows a lower \( T_{FM-PM} \) as well as two smeared maxima at \( \sim 240 \) and \( \sim 210 \) K when magnified (Fig. 4(b)). This could suggest another magnetic phase detected, which agrees with the structural analysis, wherein a 0.9(2) wt.% a single perovskite GdCoO\(_3\) was found by the Rietveld refinement of its XRD data and also observed by EPMA characterization \(^9\). For higher Sr content, a gradual decreasing magnetization with increasing temperature is observed, without AFM-FM this time, indicating a suppression of the latter with Sr\(^{2+}\) doping, similar to literature \(^9,20,22\). It is worth highlighting that the suppression was reported for higher oxygen content above O\(_{5.50}\) \(^9\), wherein the authors considered it as a limiting composition corresponding to the type of doping carriers in GdBaCo\(_2\)O\(_{5+y}\) compounds: electron doping for \( y < 0.5 \) and hole doping for \( y > 0.5 \). Depending on the type of doping or, in other words, oxygen deficiency from O\(_{5.50}\), the \( V_{Co} \) changes from 3+ (for O\(_{5.50}\)) to
a mixture of 2+/3+ and 2+/3+/4+ for y<0.5 and y>0.5, respectively. This led to a noticeable alteration in the magnetic behavior as well as in conductivity in both regions. From Table 1, it is observed that the oxygen content exceeds this limiting composition (i.e. >O_{5.50}) for Sr concentration of x≥0.3, wherein the AFM-FM phase transition was no longer observed in their M(T) data unlike for lower Sr-containing samples (Fig. 4). In addition, an enhanced conductivity previously reported for our higher Sr-doped GdBa_{1-x}Sr_xCo_2O_{6-δ} samples (Sr4) \(^{10}\) exhibited an oxygen content above the O_{5.50} limiting composition, thus lays in the hole-doped region. This is in agreement with literature \(^9\), wherein hole doping was attributed to the observed lowering of resistivity with increasing oxygen content above O_{5.50} (resistivity was lowered by ~3 orders of magnitude with Sr\(^{2+}\) mole fraction of z=0.07 in Gd_{1-z}Sr_zBaCo_2O_{5+δ} \(^{20}\)). Furthermore, the authors suggested that an oxygen composition above O_{5.50} equates to the presence of Co\(^{4+}\) and proportional to hole doping. This is also observed for our higher Sr-containing samples, for e.g. Sr4 sample, which exhibits an average V_{Co} of +3.04, could exhibit some contributions of Co\(^{4+}\) to balance the Co\(^{2+}\) detected in XPS characterization \(^{10}\).
Fig. 4: Zero field cooling and field cooling curves of GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6.5}$: (a) whole sample series, and magnified views for (b) Sr2 and Sr3.

Fig. 5 shows the field and temperature dependence of the magnetic entropy change for Sr0 and Sr1 samples. For higher amount of Sr$^{2+}$ doping, the magnetocaloric response becomes negligible. Both of them feature inverse (positive $\Delta S_M$) MCE at low temperatures and closely accompanied by conventional MCE (negative $\Delta S_M$) at higher temperatures. To date, the MCE of Gd$_{1-x}$Ca$_x$BaCo$_2$O$_{5.5}$ is theoretically reported and models only considered its conventional MCE without the presence of its AFM-FM phase transition$^{15}$. Their predictions of $\Delta S_M$ of an undoped sample (GdBaCo$_2$O$_{5.5}$) coincide with the experimental values obtained in the present paper. For Sr1, the peak of the inverse MCE ($\Delta S_M^{\text{peak}}$) and its corresponding temperature ($T_{pk}^{\text{inverse}}$) reduce as compared to those of Sr0. Furthermore, the conventional MCE is observed to be more evident in Sr1 than in Sr0 sample, suggesting the stabilization of FM phase with Sr$^{2+}$ doping and/or oxygen stoichiometry, consistent with their $M(T)$ results and also literature$^{20,22}$.

Fig. 5: Magnetic entropy change curves of Sr0 and Sr1 samples as a function of temperatures for all applied fields. The color map is also projected as bottom contour as a guide to the eye.

Fig. 6 shows a closer examination of $\Delta S_M^{\text{peak}}$ shifting to lower temperatures with magnetic fields ranging from 0.02 to 1.5 T as indicated with the arrows. Moreover, it can be observed that the flipping of the $\Delta S_M$ signs occurs earlier (i.e. at lower temperatures) with increasing magnetic fields,
which indicates that the inverse MCE is compensated by the conventional MCE with increasing fields. Hence, on top of compositional effects, the competition of magnetic phases and the alteration of the order of the magnetic phase transition contributes to the magnitude of $\Delta S_M$ effected from its AFM-FM phase transition.

Very recently, a quantitative criterion based on the magnetocaloric effect to determine the order of magnetic phase transition has been successfully applied to several magnetocaloric materials, namely La-Fe-Si-, Heusler-type alloys and composites, as well as numerical simulations23. As magnetocaloric materials are usually classified according to the order of their phase transitions (first- or second-order type), many have regarded that the ideal magnetocaloric material with a large effect with minimal or without hysteresis would be in-between the two classifications (at the region termed as the critical point of second-order phase transition)11. Hence, it is interesting to apply this recently proposed quantitative criterion to our work for evaluation, whereby the technique could even distinguish the classifications even for compositions near the critical point of second-order phase transition without being confined to a particular model but based on the magnetic field dependence of $\Delta S_M$ (equations 2 and 3). Fig. 7(a) shows the 2D plots of $\Delta S_M(T)$ for Sr0 with applied fields up to 1.5 T. The dashed green line corresponds to $\Delta S_M = 0$ and inverse and conventional MCE are indicated by the blue and pink regions, respectively. The darker shades of the blue and pink regions illustrate increasing

Fig. 6: Low temperature region of $\Delta S_{M(inverse)}(T)$ of Sr0 and Sr1 samples for 0.02-1.5 T. Arrows indicate the effect of increasing magnetic field.
magnetic fields. The $T_{pk}^{\text{inverse}}$ shifts to lower temperatures with increasing fields while $T_{pk}^{\text{direct}}$ remains at approximately the same position as a function of field. For Fig. 7(b), the exponent $n$ from the field dependence of $\Delta S_M$ for the Sr0 sample is presented as a function of temperature. At low temperatures, an overshoot of $n>2$ (illustrated by the blue regions) is observed near the onset of $T_{AFM-FM}$ (within the region of 212-222 K as they are field dependent), indicating a first-order phase transition (FOPT), which is in agreement with the order of the phase transition indicated in literature $^{24-26}$. These overshoots shift to lower temperatures with increasing field, in agreement with the field dependent $T_{pk}^{\text{inverse}}$ observed earlier. The characteristic spikes observed near 242 – 248 K (yellow region) indicate the switching of signs of $\Delta S_M$ from inverse to conventional MCE (indicated by the green dotted line which correspond to $\Delta S_M = 0$), analogous with the $n(T)$ behavior of a Heusler alloy reported in ref.$^{23}$. The exponent $n$ then goes to a minimum (corresponding to the Curie temperature of the FM-PM phase transition) prior to approaching a value of up to 2 (paramagnetic region), which agrees with the $n(T)$ behavior of a SOPT (shown in shades of pink in Fig. 7) $^{19}$. 
Fig. 7: Temperature and field dependence of: (a) $\Delta S_M$ and (b) exponent $n$ for Sr0 sample at different applied fields. Dash green line corresponds to $\Delta S_M = 0$ in (a) while the orange indicates $n = 2$ in (b). Inverse and conventional MCE are indicated by the blue and pink regions in (a), respectively. The yellow region corresponds to a change in the sign of $\Delta S_M$, producing a spike in $n$.

The field dependence of $\Delta S_M$ and exponent $n$ as a function of temperature for Sr1 at $\mu_0 H = 1.5$ T are presented in Fig. 8. Fig. 8(a) shows that the sample exhibits an inverse MCE (blue region) at low temperatures and a conventional MCE (pink region) at higher temperatures. On the other hand, its $n(T)$ plot in Fig. 7(b) shows only the characteristic spikes of switching MCE signs but without any overshoot of $n>2$. Its exponent $n$ was observed to first begin at $\sim 1.6$ (no blue shaded region this time unlike for Sr0 in Fig. 6(b)) at low temperatures then display characteristic spikes (yellow region) of switching MCE signs at approximately $207 - 213$ K. With increasing temperatures thereafter, $n$ tends to a minimum at the Curie temperature of FM-PM before approaching a value of up to 2 ($T>300$ K) as
illustrated in the pink region in Fig. 8(b). These observations reveal that though the minor doping of Sr$^{2+}$ in GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6.5}$ does not suppress the AFM-FM phase transition at low temperatures, it considerably transformed FOPT-character into a SOPT-type, which is not obvious from the $\Delta S_m(T)$ data.

The change in the order of the phase transition from FOPT to SOPT decreases considerably the magnetic entropy change of the perovskite. However, this change is produced without altering the crystalline structure at room temperature or the type of doping carrier for cobaltites (both Sr0 and Sr1 samples lay in the electron-doped category based on their oxygen content).
Fig. 8: Temperature dependence of: (a) $\Delta S_M$ and (b) exponent $n$ for Sr1 sample at a single field of 1.5 T. Inverse and conventional MCE are indicated by the blue and pink regions in (a), respectively. The yellow region corresponds to a change in the sign of $\Delta S_M$, producing a spike in $n$.

Furthermore, the universal curve method is another way to distinguish FOPT or SOPT based on the presence or absence of a qualitative feature, and has been widely used and applicable to identify the type of magnetocaloric materials\textsuperscript{19,27}. Its construction procedure details can be found in ref.\textsuperscript{19}. In short, the magnetic entropy change curves of the samples were normalized and their temperature axes were phenomenologically rescaled, which are presented in Fig. 9 for Sr0 and Sr1. For Sr0 at low temperatures (i.e. AFM-FM) in Fig. 9(a), data do not collapse onto a universal curve, indicating a FOPT in the AFM-FM transition, which is in agreement with Fig. 7. However, a good collapse onto a single universal curve observed at higher temperatures in Fig. 9(b) indicates that Sr0 undergoes a SOPT in the FM-PM region. On the other hand, Sr1 shows a good collapse of data at both AFM-FM and FM-PM temperature regions (Figs. 9(c) and (d)), suggesting that both have undergone SOPT. These observations reinforce with the analyses from Figs. 7 and 8, affirming that the FOPT-character of the AFM-FM of Sr1 sample was lost, and they prove the applicability of the quantitative criterion to cobaltites.
It is worth mentioning that the presence of very minor hysteresis in the temperature dependent magnetic entropy change curves can be misleading when using it to identify the order of the phase transition\textsuperscript{28}, inasmuch as thermal lag of the experimental setup might lead to erroneous conclusions. Therefore, that criterion is avoided in the current paper.

4 Conclusions

The properties of cobaltites are known to be highly dependent on their oxygen content deviating from the critical limit of $O_{5.50}$ leading to different type of doping carriers: electron-doped for $\delta<0.5$ while hole-doped for $\delta>0.5$. The electron-doped GdBa$_{1-x}$Sr$_x$Co$_2$O$_{6.5}$ double perovskite samples correspond to Sr additions of up to $x=0.2$ while higher Sr concentration led to hole doping by oxygen additions ($\delta>0.5$). Their thermomagnetic behavior were observed to fall into two systems: for electron-doped samples, the pristine (Sr0), Sr1 and Sr2 samples present a AFM-FM phase transition at low temperatures and a FM-PM transition at higher temperatures, though the former phase transition is very much smeared out for Sr2 sample. Conversely, only a gradual FM-PM transition is observed for...
hole-doped samples (Sr3 – Sr5) while the AFM-FM is suppressed. In addition, Sr2 and Sr3 samples lost the doubling in the \( b \)-axis though retaining the doubling in \( c \)- and crystallographic symmetry (\( Pmmm \)) while Sr4 and Sr5 completely adopt a different space group (\( P4/mmm \)).

The pristine sample was shown to present an inverse and a conventional magnetocaloric effect arising from its AFM-FM transition and FM-PM transition respectively. The exponent \( n \) of its magnetic field dependence of \( \Delta S_M \) shows an overshoot of \( n>2 \), which shifts to lower temperatures with field, consistent with the field dependence of transition temperature of its AFM-FM (which decreases with field). By using the recently proposed quantitative criterion for identifying the order of phase transitions based on the magnetocaloric effect, the fingerprint of the overshoot of \( n>2 \) clearly indicates that its AFM-FM is a first-order phase transition. On the other hand for Sr1 sample, though with minor doping of \( x=0.1 \) and retaining the same room temperature crystallographic symmetry as that of Sr0 sample (\( Pmmm \) with doubling in \( b \) and \( c \) axes), its \( n \) behavior uncovers that the first-order nature of AFM-FM was transformed into a second-order-type despite that it still exhibits a similar-looking thermomagnetic behavior and inverse magnetocaloric effect as that of the pristine sample. This was only clearly demonstrated upon further evaluation of its magnetocaloric behavior using the universal curve and magnetic field dependence methods. Therefore, it is evident that doped samples that retain the same crystalline structures and electron-doped carrier as the undoped composition might exhibit remarkably different magnetic properties due to the change of the order of phase transition.

5 Acknowledgments
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6 References
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Table Captions

Table 1. Oxygen content and cobalt valencies in GdBa\(_{1-x}\)Sr\(_x\)Co\(_2\)O\(_6\)\(_{\delta}\)

<table>
<thead>
<tr>
<th>Sr content (x)</th>
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<th>Oxygen content (6-(\delta))</th>
<th>Cobalt Valency (V(_{Co}))</th>
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Figure Captions

Fig. 1: Crystal structure representation of (a) a single perovskite ABO\(_3\), where A (green) is located in the centre of corner-connected BO\(_6\) octahedra (blue); (b) an ordered perovskite AA’B\(_2\)O\(_6\), where A (green) and A’ (purple) stack in an alternate sequence along z-crystallographic axis with corner-connected BO\(_6\) octahedra shown in brown, for example GdBaCo\(_2\)O\(_6\); (c) defective ordered perovskite AA’B\(_2\)O\(_6\)\(_{\delta}\), where the vacancy of oxygen (\(\delta\), red) is preferentially created in the xy-plane in the A’ layer.

Fig. 2: Rietveld refinement of the XRD data of Sr1 sample performed at room temperature using Cu K\(_{\alpha}\) radiation (R\(_{wp}\) = 0.029, R\(_{Bragg}\) = 0.009). The doubling in its c-axis is indicated by 2\(\theta\)\(_{001}\) = 11.73 ° and its doubling in b by 2\(\theta\)\(_{010}\) = 11.33 °, 2\(\theta\)\(_{130}\) = 41.79 ° and 2\(\theta\)\(_{131}\) = 43.56 °.

Fig. 3: Field dependence of magnetization measured at different temperatures for samples Sr0 and Sr1.

Fig. 4: Field cooling curves of GdBa\(_{1-x}\)Sr\(_x\)Co\(_2\)O\(_6\)\(_{\delta}\): (a) whole sample series, and magnified views for (b) Sr2 and Sr3.

Fig. 5: Magnetic entropy change curves of Sr0 and Sr1 samples as a function of temperatures for all applied fields. The colormap is also projected as bottom contour as a guide to the eye.

Fig. 6: Low temperature region of \(\Delta S_M\)\(_{(\text{inverse})}\) (\(T\)) of Sr0 and Sr1 samples for 0.02-1.5 T.

Fig. 7: Temperature and field dependence of: (a) \(\Delta S_M\) and (b) exponent \(n\) for Sr0 sample at different applied fields. Dash line correspond to \(\Delta S_M = 0\). Inverse and conventional MCE are indicated by the blue and pink regions in (a), respectively. The yellow region corresponds to a change in the sign of \(\Delta S_M\), producing a spike in \(n\).

Fig. 8: Temperature dependence of: (a) \(\Delta S_M\) and (b) exponent \(n\) for Sr1 sample at single field of 1.5 T. Inverse and conventional MCE are indicated by the blue and pink regions in (a), respectively. The yellow region corresponds to a change in the sign of \(\Delta S_M\), producing a spike in \(n\).

Fig. 9: Rescaling of the magnetic entropy change curves of Sr0 and Sr1 for different applied magnetic fields: (a, b) and (c, d) respectively.
Fig. 1: Crystal structure representation of (a) a single perovskite ABO$_3$, where A (green) is located in the centre of corner-connected BO$_6$ octahedra (blue); (b) an ordered perovskite AA’B$_2$O$_6$, where A (green) and A’ (purple) stack in an alternate sequence along z-crystallographic axis with corner-connected BO$_6$ octahedra shown in brown, for example GdBaCo$_2$O$_6$; (c) defective ordered perovskite AA’B$_2$O$_{6-\delta}$, where the vacancy of oxygen ($\delta$, red) is preferentially created in the xy-plane in the A’ layer.
Fig. 2: Rietveld refinement of the XRD data of Sr1 sample performed at room temperature using Cu $K_\alpha$ radiation ($R_{wp} = 0.029, R_{Bragg} = 0.009$). The doubling in its $c$-axis is indicated by $2\theta_{001} = 11.73^\circ$ and its doubling in $b$ by $2\theta_{010} = 11.33^\circ, 2\theta_{130} = 41.79^\circ$ and $2\theta_{131} = 43.56^\circ$. 
Fig. 3: Field dependence of magnetization measured at different temperatures for samples Sr0 and Sr1.
Fig. 4: Field cooling curves of GdBa$_{1.4}$Sr$_x$Co$_2$O$_{6.5}$: (a) whole sample series, and magnified views for (b) Sr2 and Sr3.
Fig. 5: Magnetic entropy change curves of Sr0 and Sr1 samples as a function of temperatures for all applied fields. The colormap is also projected as bottom contour as a guide to the eye.
Fig. 6: Low temperature region of $\Delta S_M(T)$ of Sr0 and Sr1 samples for 0.02-1.5 T. Arrows indicate the effect of increasing magnetic field.
Fig. 7: Temperature and field dependence of: (a) $\Delta S_M$ and (b) exponent $n$ for Sr0 sample at different applied fields. Dash green line corresponds to $\Delta S_M = 0$ in (a) while the orange indicates $n = 2$ in (b). Inverse and conventional MCE are indicated by the blue and pink regions in (a), respectively. The yellow region corresponds to a change in the sign of $\Delta S_M$, producing a spike in $n$. 
Fig. 8: Temperature dependence of: (a) $\Delta S_M$ and (b) exponent $n$ for Sr1 sample at single field of 1.5 T. Inverse and conventional MCE are indicated by the blue and pink regions in (a), respectively. The yellow region corresponds to a change in the sign of $\Delta S_M$, producing a spike in $n$. 
Fig. 9: Rescaling of the magnetic entropy change curves of Sr0 and Sr1 for different applied magnetic fields: (a, b) and (c, d) respectively.
Highlights:

- Perovskite cobaltites exhibit consecutive antiferro-ferro-paramagnetic transitions
- The order of the phase transition can be determined with a new quantitative method
- The antiferro-ferro transition changes from first to second order with Sr doping
- Despite the change of order of phase transition, crystal structure at room temperature is unchanged
Figure 3
Figure 5
Figure 7

\(\Delta S_M (\text{J kg}^{-1} \text{K}^{-1})\) vs. \(T (\text{K})\)

(a) \(\Delta S_M = 0\)

(b) \(n = 2\)

\(\mu_0 H (\text{T})\)
- 0.7
- 1.0
- 1.2
- 1.5

Legend:
Figure 8
Figure 9