GEOTECHNICAL CHARACTERISATION OF THE MIOCENE

FORMATIONS AT THE LOCATION OF IVENS SHAFT, LISBON

António Pedro1*, Lidija Zdravković2, David Potts2 & Jorge Almeida e Sousa1

1Department of Civil Engineering, University of Coimbra, Coimbra, Portugal
2Department of Civil and Environmental Engineering, Imperial College, London, UK

*Corresponding author (e-mail: amgpedro@dec.uc.pt)

ABSTRACT

The design of complex underground structures in an urban environment requires in the first instance an appropriate characterisation and interpretation of the ground conditions and of the mechanical behaviour of soil formations in the ground profile. With such information it is then possible to select and calibrate appropriate soil constitutive models for application in advanced numerical analysis, with the objective of predicting the induced ground movements and the potential damage to existing structures and services. This paper provides an interpretation of the site investigation data collected for the numerical analysis and design of the Ivens shaft excavation in Lisbon, Portugal. For the first time a comprehensive set of interpreted data is obtained for two of the main formations in the Lisbon area, Argilas e Calcários dos Prazeres (AP) and Areolas da Estefânia (AE), improving the understanding of their mechanical behaviour and making the data available for application in most soil constitutive frameworks. It is evident from the results that even with careful testing procedures the data may appear to be inconsistent, requiring further assumptions when deriving soil parameters. Such assumptions are discussed and an emphasis is placed on the need to combine data from laboratory and field investigations.

1 INTRODUCTION
The Baixa-Chiado metro station is one of the most important interface stations of the Lisbon Metro network, as it enables the interchange between the busy Green and Blue lines and is located near downtown Lisbon (Figure 1). Apart from the two galleries that accommodate the platforms, the Baixa-Chiado station also has two exit tunnels, Chiado and Crucifixo (Postiglione et al., 1997). A third exit via a 40m deep shaft is also included in the original project but its construction has been successively delayed to date (late 2017). Due to space constraints the shaft was positioned in the backyard of the Quintão building, with access via the Ivens street, and is surrounded by old buildings and services (hatched areas in Figure 1). The shaft, named Ivens, is of a complex shape, varying from an elliptical cross section at the ground surface to a circular cross section at its base.

Several previous ground investigation reports were available for the design of the Ivens shaft, relating to various locations in Lisbon (Moitinho de Almeida, 1991; Marques, 1998; Cenorgeo, 2008; Guedes de Melo, 2008). These have established the ground profile and enabled some characterisation, mainly through field testing, of the two main formations, geologically referred to as Miocene: the predominantly silty-clayey “Argilas e Calcários dos Prazeres” or the AP formation; and the predominantly granular “Areolas da Estefânia” or the AE formation. Limited laboratory testing existed, in particular the assessment of the soils’ nonlinear small strain stiffness behaviour.

A ground investigation conducted in 2010 reported by Pedro (2013) was aimed at providing more reliable geotechnical data for the numerical analysis of ground movements caused by shaft excavation. A particular effort was directed to the interpretation of the small strain stiffness, as this aspect of soil behaviour is most influential in predicting ground movements (e.g. Addenbrooke et al., 1997; Franzius et al., 2005; Zdravkovic et al., 2005). The paper brings together the existing and new site investigation data and interprets the main mechanical parameters of strength, stiffness and compressibility of both formations.

INSERT FIGURE 1 HERE

2 GEOLOGICAL PROFILE AT THE IVENS SHAFT SITE
The geology of Lisbon has been influenced by several extreme geological processes (Antunes, 1979; Alves et al., 1980). The oldest superficial soils date from the Cretaceous period, 95 million years ago (Ma), although the majority of the city centre is founded upon Miocene formations, formed around 24 Ma ago (Moitinho de Almeida, 1991). During this epoch several transgressive-regressive cycles, each corresponding to a depositional sequence, occurred due to tectonic events and due to variations in sea level (Dias & Pais, 2009). This epoch was followed by the last glacial period, when a substantial climate change in the region caused intense erosion and a deflection in the course of the river Tagus (Dias et al., 1997). Only at the beginning of the current Holocene epoch did the water level start to rise again and new sediments began to deposit in the basin.

The lithological profile at the Ivens shaft site is shown in Figure 2. The top 6 m is a loose sandy fill. Underneath are the two main formations, AE down to 35 m, followed by the AP formation. The AP formation was deposited in a marine environment which changed progressively to a sub-tidal zone in shallower waters. The material between 35 and 37 m depth can be considered a different unit (Top AP), as it is lighter in colour (more oxygen) and is more compatible with the latter type of environment. The analysis of the AE formation is more complicated since it contains layers of different degrees of cementation, as a result of significant differences in the depositional environment (Cotter, 1956; Antunes et al., 2000). At depths between 12 and 17 m within the AE formation there is a 5 m thick layer of fossiliferous limestone, which is usually formed in shallow, quiet and warm waters, the conditions often associated with tidal flats or reef environments. Despite significant variations within the AE formation, it is usually considered in the literature as a single unit, with the exception of the limestone layer which is considered independently. The water table was measured at approximately 27 m depth.

The particle size distribution (PSD) determined by Pedro (2013) at each metre depth, with the exception of the limestone layer, is presented in Figure 3. The PSDs for the AP formation (below 35 m depth) are almost identical, with around 23 % of clay, 62 % of silt and only 15 % of mostly fine sand. In contrast, the results of the AE formation indicate differences which can be related to depth and to past geological events. The layer above the limestone, between 5 and 12 m, is a finer soil since it
comprises nearly 44% of silt and 14% of clay on average, while the lower layer (18 to 34 m) consists of an average of 80% of sand (mostly fine) and 16% of silt. According to the ASTM (2006) standard the AP formation is classified as a lean clay (CL), while the AE formation, despite its variability throughout the profile, can be classified as a silty sand (SM). The fill is fairly homogeneous with 93% of fine sand and is classified as a poorly graded sand (SP).

3 NEW GEOTECHNICAL INVESTIGATION

The new ground investigation involved drilling of two new boreholes (B1 and B2) in the backyard of the Quintão building (Figure 1) to about 40 m depth. Figure 2 shows positions in the ground profile from which 76 mm diameter samples were taken. The boreholes were primarily drilled using rotary techniques to provide cores of 76mm diameter to enable almost continuous sampling of the soil. However, at specific depths, where good quality samples were required, instead of coring a thin-walled sampler with a PVC liner of also 76mm diameter was used. After the extraction, the coring resumed until another specific extraction depth was reached. High recovery rates were obtained in the finer materials while in the coarser materials, particularly those located below the water table (27m depth), only partial recovery was achieved. Apart from retrieving samples, disturbed for identification of the lithology and determination of the physical properties, and intact for advanced laboratory testing, the investigation also included seismic tests for characterising the initial stiffness of the soils. Unfortunately, due to obstructions met in both boreholes it was only possible to perform down-hole tests to a depth of 28 m.

Due to the granular nature of the AE formation the sampling of intact samples was not straightforward, which is why prior investigations of the strength and stiffness of this material mainly relied on indirect correlations with in-situ tests, such as the Ménard Pressuremeter Test, MPT (Guedes de Melo, 2008) or Self-Boring Pressuremeter Test, SBPT (Ludovico Marques & Sousa Coutinho, 2004). However, in the new investigation it was possible to retrieve intact samples from this formation using the methodology mentioned (Pedro, 2013). As soon as the samples were retrieved, and while laterally confined by the PVC tube, they were fully wrapped in wax in order to preserve their natural properties.
and minimise any disturbance. All samples were then placed into a moisture controlled chamber until preparation and testing in a temperature controlled laboratory.

A total of 34 tests were conducted by Pedro (2013) in the Geotechnical laboratory of Coimbra University in Portugal. A summary of all tests and their initial conditions are presented in Table 1 in the Appendix. The experimental programme comprised three oedometer and four isotropic triaxial compression tests, for assessing the behaviour in compression, six isotropic triaxial compression tests with bender element measurements for analysing the initial stiffness, and 21 triaxial tests for evaluating the strength and deformation of the soils in the two formations. The oedometer samples were 50 mm in diameter and 19 mm thick. The triaxial samples were 38 mm in diameter and 76 mm high. All samples were initially saturated to a minimum B-value of 0.95 (up to 0.98 in the case of the AE samples).

In the AE formation a total of 14 samples were isotropically consolidated in a triaxial apparatus to different levels of the mean total stress, $p_t$, 9 of which then followed compression and 5 extension stress paths. These tests were divided into 3 main groups, each with a purpose of investigating a specific aspect of soil behaviour. In order to evaluate the small strain stiffness behaviour independently of the $p'$-effect, 6 tests, 3 in compression (PC) and 3 in extension (PE), were performed with constant $p'$. A second group of tests were sheared following total stress paths expected to apply to the shortest and longest axes of the elliptical shaft during excavation, as sketched in Figure 4 for the shaft’s horizontal cross-section. With the vertical total stress being approximately constant in the soil around the shaft at any horizontal section, a triaxial compression path with decreasing $p$ (CD), due to a decreasing total horizontal stress, is expected in the short axis of the shaft. Conversely, a triaxial extension path with increasing $p$ (EI) is expected in the long axis, due to an increase in the horizontal total stress. An additional test in extension with a decreasing $p$ (ED) was also performed in order to simulate the total stress path followed by a soil element located above the enlargement of the shaft section, as shown in Figure 4 for the shaft’s vertical cross-section. In this case the vertical stress reduces due to the shaft excavation beneath. Finally, a third group of compression tests follows a conventional compression stress path with an increasing $p$ (CI), in order to facilitate the understanding
and interpretation of all results and enable a comparison with other soils. Since the majority of the
samples were collected at 3 different depths (8, 18 and 21 m), the tests were performed at
approximately those three in-situ stress conditions, represented by p’ of 130, 300 and 400 kPa,
respectively. The 7 samples tested in the AP formation (2 from the Top AP unit) were all collected from
between 36.3 and 40.4 m depth and consequently the estimated vertical field stress varied from 585
to 630 kPa. Due to limitations of the maximum working pressure of the triaxial cell all tests were
performed with an initial p’ of 480 kPa. However, in order to compare the effects of the initial stress
state 2 samples had an initial isotropic stress state while the remainder were consolidated under
anisotropic conditions (K₀=0.7). A similar strategy was adopted for this formation regarding the
shearing stress paths. However, in this case and given the limited number of samples available, not all
the different stress paths could be tested as for the AE formation.

4 IN SITU STRESSES

The new ground investigation at the Ivens shaft site did not include tests to estimate the in-situ stress
profile. However, results from several SBPTs conducted by the National Laboratory for Civil
Engineering (LNEC, 1996a, b, c, d) were available from previous investigations and were recalculated
by the authors taking into consideration the water table position measured at the Ivens site by Pedro
(2013). This enabled a more accurate estimation of the coefficient of earth pressure at rest, K₀ (Figure
5), albeit with some scatter. Despite this it is possible to establish that the K₀ value in the AE formation
appears to decrease with increasing vertical effective stress from a maximum of about 1.5 at 200 kPa
to approximately 0.7 at 500 kPa. The results obtained for the AP formation show a smaller variation
of $K_0$, with average of 0.7. The high $K_0$ values in the top part of the AE formation are thought to be consistent with the geological history discussed earlier, and in particular glaciation and erosion of the deposits.

5 PHYSICAL PROPERTIES

X-Ray diffraction tests on samples collected in the new ground investigation revealed that quartz is the predominant mineral in both formations (60%), followed by feldspar (15%). The AP formation also contains reasonable amounts of mica-illite (11%) and smectite (9%) which may affect the compressibility characteristics of the soil if variations in the water content occur (Skempton, 1953). The intact samples collected at different depths enabled the definition of profiles of plasticity index, activity, unit weight, moisture content, void ratio and degree of saturation, as presented in Figure 3. Despite some scatter, typical of natural soils that exhibit variability due to different depositional environments, it is interesting that these properties seem broadly constant with depth, independent of the lithology. Both formations have a unit weight of approximately 20 kN/m$^3$, a water content of around 20 %, and a void ratio below 0.7. Apart from the coarser zones below the Limestone layer, the soil appears to be saturated. The Atterberg limits of the AP formation suggest that the formation should have low compressibility, since the water content of soil is at or slightly below the plastic limit (about 25 %) and the liquid limit increases with depth from 40 % at 36m depth to about 50% at 40m depth. Despite the low plasticity index in Figure 3, the activity can be considered medium to high according to Skempton (1953). These values support the conclusions of the mineralogical analysis that the clay fraction is sensitive to variations in the water content.

6 BEHAVIOUR IN COMPRESSION

Figure 6 shows the results of 4 isotropic compression tests (denoted ‘I’) on intact samples collected from two boreholes at the Ivens shaft site (Pedro, 2013). Two of the samples, I-AE-08.5 and I-AE-21.5, taken from 8.5 and 21.5 m depth respectively, show almost identical behaviour in compression, with
the interpreted gradient of the normal compression line (NCL) being $\lambda=0.134$. The volumetric strain measured in test I-AE-18.0, for a similar change in $p'$, is significantly lower, with interpreted $\lambda=0.089$. This sample was collected from 18 m depth, immediately below the limestone, and is therefore likely to have some cementation which contributes to its low compressibility. Consequently, a representative NCL for the AE formation is taken as that with $\lambda=0.134$. In contrast, the swelling paths, both from the unload-reload loops and from the final unloading, are similar for all AE tests, and a representative gradient is $\kappa=0.033$.

A single isotropic compression test on the AP formation indicates a compression gradient $\lambda=0.178$, and a swelling gradient $\kappa=0.066$. The gradients for both formations are within the expected range of values found in the literature for materials with similar gradings (Atkinson, 1993). To assess the existence of structure in the AP soil, additional oedometer tests were performed on intact samples of ‘fair’ quality, according to the approach proposed by Lunne et al. (1997). The results are compared in Figure 7 with the intrinsic compression line (ICL) determined using Equations 1 and 2 proposed by Burland (1990).

\begin{align}
C_C^* &= 0.256 \cdot e_L - 0.04 \quad (1) \\
e_{100}^* &= 0.109 + 0.679 \cdot e_L - 0.089 \cdot e_L^2 + 0.016 \cdot e_L^3 \quad (2)
\end{align}

Where $C_C^*$ represents the intrinsic compression index, $e_{100}^*$ the void ratio at a vertical effective stress of 100 kPa and $e_L$ the void ratio at liquid limit (taken as 1.096). The responses of the two deeper samples (O-AP-37.5 and 40.0) plot above the ICL and yield at higher stresses, confirming the existence of structure. The degradation of structure with further compression is not rapid and an average sensitivity of the clay (Cotecchia & Chandler, 2000), of about 3 was determined. In contrast, the shallower sample O-AP-36.5 appears to follow the intrinsic compression line, behaving more like a reconstituted material. These results are in agreement with the proposed geological framework in Figure 2, in that the top of the AP formation is a separate less-structured layer, while the rest of the formation is clearly structured. The results from the 3 tests show that the AP formation is over-consolidated, with the OCR, determined using Taylor (1948) method, varying from 3.4 to 5.6.
Furthermore, oedometer results show no significant creep displacements and enable an estimation of a coefficient of permeability of about $2 \cdot 10^{-10}$ m/s to be made for the in-situ stress level.

**7 DRAINED STRENGTH PARAMETERS**

**7.1 AE FORMATION**

Figures 8 to 11 show the shearing behaviour of all AE samples under both drained and undrained conditions. The applied shearing rate was 5% of axial strain per day, which was sufficient to ensure no excess pore pressures in the former and uniform excess pore pressures in the samples in the latter type of shearing (both checked with a mid-height pore pressure probe). Generally, the soil displays dilatant behaviour in both compression and extension, with most samples showing post-peak strain-softening in Figure 8, with the peak strength occurring at axial strains between 2 and 6%. Shearing to about 20% axial strain, $\varepsilon_a$, has not established clear critical state stress ratios, $q/p'$, in either of the two shearing modes. In terms of the volumetric response, the samples tested under drained conditions exhibited an initial contraction followed by dilation (Figure 9). Tests in extension with a constant $p'$ ($T$-AE-DPE-I) show a consistent effect of the mean effective stress level $p'_i$, with a sample sheared from 400 kPa exhibiting the smallest dilation, while that at 130 kPa the largest. Similarly, the tests in compression at constant $p'$ ($T$-AE-DPC-I) also reveal higher dilation at lower stress levels, although the test at $p' = 130$ kPa has stopped prematurely. In general samples sheared in compression show higher volumetric dilation than those sheared in extension. However, despite the measured final volumetric strains differing significantly, the initial gradients of dilation $|\Delta \varepsilon_a|/\Delta \varepsilon_v$ appear to be similar for these samples, as shown in the figure. The two additional standard drained tests in compression ($T$-AE-DCI-I) presented higher contractive volumetric strains followed by dilation, with this behaviour being more evident in the case of the smaller $p'$. The excess pore water pressures
in the undrained tests (Figure 10) varied from sample to sample, in conjunction with the applied
modes of shearing explained earlier in Figure 4, but their overall trend was again negative at high
strains. These interpretations confirm the behaviour of the AE formation to be characteristic of dense
granular soils with most of the observed differences being a result of the natural variability of the
formation, as ascertained from Figure 3, and particularly of the stress conditions and paths imposed
during shearing.

As noted above, no clear ultimate strength conditions could be identified from all samples, particularly
those tested in extension. However, the analysis of the effective stress paths from all 14 tests is helpful
in interpreting the likely peak strength envelopes in compression and extension (Figure 11). Marked
on the figure are also the points of the maximum stress ratio ($q/p'$) for all stress paths. Despite the
scatter observed in the results and the variability in this formation (Figure 3) the strength envelopes
determined present a very good fit, indicating an angle of shearing resistance of 42°, in both
compression and extension, with no apparent cohesion. Furthermore, despite failing to reach
convincing critical state conditions, an angle of shearing resistance of about 35° was determined from
the stress ratio $q/p'$ achieved at highest strain levels.

Seven triaxial compression tests were performed on intact samples from the AP formation, the results
from which are presented in Figures 12 to 15. The same shearing rate of 5%/day was applied, but in
this case both from isotropic and $K_o$ initial stresses. Although all samples are taken from practically
the same depth of the deposit, the striking feature from the figures is a large variation in the observed
responses. However, the response from all samples is consistent with the behaviour of
overconsolidated clays. Some of the differences in the results are also related to the different stress
and shearing conditions imposed in the tests and to the inherent variability of the deposit. The
shearing behaviour presented in Figure 12 exhibits varying degrees of strain-softening, consistent with
a break-down of structure. The evolution of the volumetric strains in Figure 13 from the 4 drained
tests is highly variable, but all samples show dilation towards final states. The effect of the initial stress
state for the same initial $p'$ is evident from samples T-AP-DPC-K and T-AP-DPC-I, with the latter
showing higher contractive volumetric strains as it starts shearing further from the strength envelope.
A similar level of variability is observed in the pore pressure response measured in the 3 undrained
tests, but the overall tendency is one of generating negative excess pore pressures towards failure
(Figure 14). Also the tests performed with an increase in $p'$ (UCI) generated initially positive excess
pore pressure while that with a decrease in $p'$ (UCD) generated negative excess pore pressure from
the start of shearing.

The behaviour exhibited by the two samples retrieved from 36.3 and 37.7 m depth in the TAP layer,
T-TAP-DPC-I-480 and T-TAP-UCI-K-480, differs from that observed in other samples, despite having
similar mineralogical and PSD curves. Both samples show a mild strain-softening (Figure 12), absence
of bonding, a more pronounced contraction (Figure 13) and a high positive excess pore water pressure
(Figure 14) generated at the beginning of shearing, typical of reconstituted samples. When plotting
the effective stress paths of these tests in Figure 15 the points of their maximum stress ratio are not
aligned with the remaining points, making it difficult to establish a unique peak strength envelope for
the AP formation. When considering all tests, a $\phi'$ and an apparent $c'$ of 31° and 162 kPa can be
estimated, respectively, although with low confidence (low $R^2$). Much better agreement is obtained
when the two TAP samples are not considered, with values of $\phi'$ and $c'$ being estimated to be 45° and
103 kPa, respectively. These discrepancies are again in agreement with the proposed geological
framework presented in Figure 2, with samples deeper than 38 m indicating considerable bonding and
high $c'$ (the samples would not disintegrate if submerged in water), while others, between 35 and 38 m depth, exhibiting minimal or even non-existent structure. Similar difficulties were observed for the evaluation of the critical state angle of shearing resistance in this formation. A value of 28° was estimated when neglecting the results of the TAP samples. These shearing results further confirm that the top of the AP layer (TAP) should be considered as a different unit in the ground profile.

8 STIFFNESS PROPERTIES

8.1 INITIAL STIFFNESS

Measurements of shear wave velocities in the new field investigations were taken through a down-hole (DH) test in borehole B1, to a depth of 28 m (Pedro, 2013). The results of the shear wave velocity, $V_s$, and of the interpreted maximum shear modulus, $G_0$, profile are shown in Figure 16, together with the results of similar tests compiled by Guedes de Melo (2011) from various sites in Lisbon. Unfortunately, the latter does not distinguish different formations and the data are only used here for reference. However, the new (DH) profile of both $V_s$ and $G_0$ present a trend similar to that from previous data, generally increasing with depth, and with a concentration of higher values around the depth of the Limestone layer (grey area in Figure 16).

Shear wave velocities measured in the laboratory using bender elements (BE) on triaxial samples (3 tests in the AE formation, 2 in the AP formation and 1 in the limestone layer) are also presented on Figure 16. In order to define the arrival time of the vertically propagating and horizontally oscillating
shear wave between the top and the bottom BE, the ‘first arrival’ method from the time-domain framework was applied (Viggiani & Atkinson, 1995). The BE profile of $G_0$ in Figure 16 has a trend similar to that from the in-situ DH test, but is significantly smaller in magnitude, although the values are consistent with results published in the literature for similar materials (Hight et al., 2007; Clayton, 2011). Discrepancies like this, between in-situ and laboratory results, have been reported by several authors for other soils (Kokusho, 1987; Ishihara, 1996; Ng & Wang, 2001) and are usually attributed to a combination of factors that were also observed in this study. Despite careful preparation, the set-up and data interpretation of both BE and DH tests involve some uncertainties, which are amplified by scale effect (field vs sample) and greater heterogeneity within the soil mass. However, the most significant factor contributing to this discrepancy is a loss of cementation during sampling of the AE formation. Despite this, the ratio between measured laboratory and field shear moduli is still within the experimentally derived upper and lower boundaries for sands, as proposed by Kokusho (1987), with the average ratio being approximately 25%.

8.2 STIFFNESS DEGRADATION CURVE

From laboratory experiments

The small-strain stiffness behaviour of the AE soil was assessed from the results of 6 isotropically consolidated drained triaxial tests sheared in compression and in extension with a constant $p'$, at three different mean effective stress levels. The results are shown in Figure 17 as tangent shear stiffness, $G_{tan} (= \Delta(\sigma'_a - \sigma'_r)/(3\Delta\varepsilon_s))$, versus deviatoric strain, $\varepsilon_d (= (2/3)(\varepsilon_a - \varepsilon_r))$. Although the local axial strain instrumentation, comprising two LVDTs on the opposite sides of the sample, could resolve only to about 0.005% strain, the results show the usual trend of modulus decay with increasing deviatoric strains and the $G_{tan}$ values being higher at higher $p'$. However, for the same stress level (i.e. $p'$) the differences between the shear degradation curves in compression and in extension are small. The $G_0$ values from bender element tests, which correspond to very small strains, are
superimposed in the figure, where plateaus for the initial part of the stiffness degradation curves would be expected for the three stress levels.

For the AP soil 3 drained triaxial compression tests were performed on samples collected at 36.3 m (T-AP-DPC-I-480) and at 39 m (T-AP-DPC-K-480 and T-AP-DPC-I-480*) depth. Two samples, one at each depth, were consolidated isotropically and the third sample anisotropically, with a K₀ equal to 0.7. In all cases a mean effective stress of 480 kPa was applied at the beginning of shearing as explained earlier. The interpreted stiffness curves in Figure 18 show some scatter and, as for the AE samples, the smallest recorded deviatoric strains were, on average, above 0.005 %. The initial shear modulus from the BE test indicates a possible plateau of stiffness degradation curves.

Figure 21 displays a summary of normalised (by the current p’) stiffness degradation envelopes from all triaxial tests, including the results of the unload-reload loops from five tests on both soils. Although the AE soil has generally higher stiffness (AE – Triax) compared to the AP soil (AP – Triax), the two ranges overlap. The ranges of normalised $G₀$ measurements from BE tests on samples from both soils (AE – BE and AP – BE) are marked at very small strains and also show very similar magnitudes of maximum stiffness.

From in-situ experiments

The stiffness degradation curves are further interpreted from the unload-reload cycles of the SBPTs and this was done using the idealised theory of expanding cavities (Palmer, 1972). A closed-form solution was proposed by Bolton & Whittle (1999) and Whittle (1999), assuming that the non-linear elastic response of soils can be described by a power law (Equation 3), where $\alpha$ and $\beta$ are fitting parameters that can be obtained by applying the least squares method to the horizontal stress ($\sigma_h$) –
cavity strain \((\varepsilon_c)\) curves measured during the SBPT. The tangent shear modulus is then calculated using Equation 4.

\[
\sigma_h = \alpha \cdot \varepsilon_c^\beta \tag{3}
\]

\[
G_{\text{tan}} = \alpha \cdot \beta \cdot \varepsilon_c^{\beta - 1} \tag{4}
\]

The procedure can be applied both to unload and reload paths of the SBPT cycle, but is often applied only to the latter, as it is thought that the unloading path presents initially some creep, probably related to strain rate effects, making it difficult to select the correct origin of the cycle (Whittle et al., 1993). Figure 19 shows an example of an unload-reload SBPT loop and a fitted power law curve to the reload path of the loop. The authors applied this procedure to 34 reload cycles of the SBPTs carried out by LNEC (1996a, b, c, d) in both soils (11 in the \(\text{AP}\) and 23 in the \(\text{AE}\)). The fitting of all data resulted in the power law parameters \(\alpha = 18.367\) and \(\beta = 0.643\) (Figure 19). Using Equation 4, the resulting tangent shear modulus normalised by the mean effective stress (estimated assuming that the vertical stress did not change and that the horizontal stress was given by the SBPT) is plotted against the deviatoric strain \((\varepsilon_s = 2/\sqrt{3} \varepsilon_c)\) in Figure 20 for the \(\text{AE}\) formation. This range of stiffness degradation curves (\(\text{AE-SBPT}\)) is added to the overall stiffness plot in Figure 21. A similar procedure was applied to SBPTs performed in the \(\text{AP}\) soil, with the results (\(\text{AP-SBPT}\)) in Figure 21 indicating a similar range of shear modulus decay to that of the \(\text{AE-SBPT}\) interpretation. Finally, the normalised \(G_0\) data from the DH test are also added in Figure 21.

Analysis of Figure 21 indicates two important aspects of shear stiffness interpretation for both soils: (i) significant difference, up to 40\%, between the in-situ- and laboratory-derived shear modulus, in particular in the nonlinear range (shear strains less than 0.01\%); and (ii) overlaps of stiffness envelopes between the two soils at all strain levels and for both experimental sources. The reasons for the former may be attributed to various levels of disturbance of intact samples related to loss of cementation during their extraction, although it was not possible to quantify this with any precision. From the latter observation (ii), considering that this interpretation of shear stiffness is in terms of an overall isotropic stiffness, it is difficult to make a meaningful distinction between the two formations. As a
consequence, it seems reasonable to assume the same normalised shear stiffness for both soils and
the solid and dashed lines in Figure 21 represent average curves derived from the in-situ and
laboratory data respectively. The implication of this interpretation is that any modelling of small-strain
stiffness would need to combine the field and laboratory data (e.g. Tatsuoka & Shibuya (1991)). The
former is likely to apply for the elastic plateau and in the small-strain range to 0.01% strain, and the
latter in the medium to large strain range beyond 0.01% strain where the loss of cementation becomes
evident. However, the adopted stiffness degradation curve would need to be validated on a boundary
value problem with measured ground movements.

INSERT FIGURE 19 HERE

INSERT FIGURE 20 HERE

INSERT FIGURE 21 HERE

8.3 BULK STIFFNESS

Data relating to the decay of tangent bulk modulus with volumetric strain have been obtained from
the isotropic compression tests performed on both soils (Figure 6). In order to determine the tangent
bulk modulus, $K_{tan} = \Delta p' / \Delta \varepsilon_v$, data from the first loading (L), final unloading (F) and from the
unload (U) – reload (R) loops was analysed separately. The bulk modulus curves, normalised by the
mean effective stress, $p'$, are plotted against volumetric strain in Figure 22. The results show that for
both soils the highest stiffness is mobilised along loading paths, followed by a steep decay. In contrast,
along the unloading paths an almost constant bulk modulus was obtained. This path-dependence is
more clearly evident in the AP formation. For volumetric strains higher than 0.5 %, the majority of the
curves have reached a minimum plateau and consequently no major variation of the normalised bulk
modulus is expected beyond this strain. If an elastic relationship between $G_{tan}$ and $K_{tan}$ is assumed
at small strains ($\varepsilon_s = 0.0001\%$ and $\varepsilon_v = 0.001\%$ ) a Poisson’s ratio of about 0.17 is estimated.
9 CONCLUSIONS

The objective of this paper is to contribute new knowledge on the mechanical behaviour of two of the main soil formations in the Lisbon ground stratigraphy, known as the AE and AP formations, based on the results from a new site investigation for the enhanced analysis of the proposed Ivens shaft excavation in Lisbon, Portugal. The investigation comprised both field and laboratory experiments with particular emphasis on the latter. Despite the scatter in experimental evidence observed in both formations caused by the inherent variability of these materials, the interpretation of compressibility and drained strength, has provided a better definition of the layers in the ground profile and a better understanding of their behaviour. It is demonstrated that the more granular AE formation, despite differing degrees of cementation, can be considered as a single unit, apart from the Limestone layer. However, the clayey-silty AP formation needs to be split in two layers, with the top 2 m being of lower strength.

In interpreting stiffness, both of the two formations exhibit similar behaviour with a tangent shear modulus degradation at all strain levels and from both the field and laboratory data. However, significant differences, of up to 40% for very small strains (less than 0.0001%), were observed between the field and laboratory-interpreted shear stiffness. Similar differences, have been observed with the behaviour of other stiff clays and are mainly attributed to loss of cementation during sampling, variability and scale effects and require critical judgement when deriving parameters for numerical modelling. A possible methodology would be to establish a stiffness degradation curve based on the combination of the two sets of results, with the field data used to define the small strain range (less than 0.01% strain) and the data from the laboratory used in the range of medium to large strains.

The results from this investigation, complemented with information from other sites in the Lisbon area, provide a valuable set of data for the selection of an appropriate numerical framework for modelling the general behaviour of these Miocene formations of Lisbon. The data enable calibrations to be made of advanced constitutive models that combine both failure and small-strain soil behaviour.
However, as the results of the current investigation have shown, there is significant variability across the area from the various geological processes, and so consistency of local site conditions with those presented here should be checked.

ACKNOWLEDGEMENTS

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\( \alpha, \beta \)  
Fitting parameters

\( \Delta u \)  
Excess pore water pressure

\( \varepsilon_a \)  
Axial strain

\( \varepsilon_c \)  
Cavity strain

\( \varepsilon_r \)  
Radial strain

\( \varepsilon_s \)  
Shear strain

\( \varepsilon_v \)  
Volumetric strain

\( \kappa \)  
Isotropic swelling index

\( \lambda \)  
Isotropic compression index

\( \sigma^\prime_a \)  
Axial effective stress

\( \sigma_h \)  
Horizontal stress

\( \sigma^\prime_r \)  
Radial effective stress

\( \sigma^\prime_{r0} \)  
Initial radial effective stress

\( \sigma^\prime_v \)  
Vertical effective stress

\( \sigma^\prime_{v0} \)  
Initial vertical effective stress

\( \phi' \)  
Angle of shear resistance

\( c' \)  
Cohesion

\( C_C^* \)  
Intrinsic compression index

\( e^*_{100} \)  
Void ratio in the ICL for a vertical effective stress of 100 kPa

\( e_L \)  
Void ratio at liquid limit

\( G_0 \)  
Initial shear modulus

\( G_{tan} \)  
Tangent shear modulus

\( K_0 \)  
Earth pressure coefficient at rest

\( K_{tan} \)  
Tangent bulk modulus

\( LL \)  
Liquid limit

\( p' \)  
Mean effective stress

\( PL \)  
Plastic limit

\( q \)  
Deviatoric stress

\( u_0 \)  
Initial pore water pressure

\( V_S \)  
Shear wave velocity
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Figure 21 – Comparison of the normalised tangent shear modulus curves from field and laboratory tests on AE and AP soils

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Table 1– Tests performed on intact samples retrieved from the boreholes drilled in the backyard of the Quintão building (Pedro, 2013)

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<th>Type of test</th>
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</table>

Test designation code (Example):

- **Lithology**: AE - "Areolas da Estefânia"; AP - "Argilas e Calcários dos Prazeres"; TAP – Top of “Argilas e Calcários dos Prazeres”; LI – Limestones
- **Shearing path**: DPC - drained compression with constant p'; DPE - drained extension with constant p'; DCD - drained compression with decrease p'; DCI - drained compression with increase p'; UED - undrained extension with decrease p'; UEI - undrained extension with increase p'; UCI - undrained compression with increase p';
- **Consolidation**: I - isotropic consolidation; K - anisotropic consolidation ($K_0=0.7$)
- **Oedometer**: Type of test – Lithology – Sample Depth (O-AP-36.5)
- **Isotropic compression**: Type of test – Lithology – Sample Depth (I-AE-18.0)
- **Bender elements**: Type of test – Lithology – Sample Depth (BE-AE-07.7)
- **Triaxial**: Type of test – Lithology – Shearing path – Consolidation - initial mean stress (T-AE-DPC-I-130)
Figure 1 – Location of the Baixa-Chiado station and Ivens shaft in Lisbon downtown

Figure 2 – Ivens shaft soil profile
Figure 3 – Particle size distribution and index properties of the Ivens shaft site ground profile (Pedro, 2013)

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Figure 9 – Volumetric strains from drained triaxial tests on the AE soil

Figure 10 – Excess pore pressures from undrained triaxial tests on the AE soil
Figure 11 – Effective stress-paths from all triaxial tests on the AE soil

Strength envelope:
\[ \phi' = 42^\circ \]
\[ c' = 0 \text{ kPa} \]

\( R^2 = 0.99 \)

\( R^2 = 0.92 \)
Figure 12 – Stress ratio – axial strain curves from all triaxial tests on the AP soil

Figure 13 – Volumetric strains from drained triaxial tests on the AP soil
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Figure 19 – An example of an unload-reload SBPT loop employed in the derivation of shear stiffness degradation curves

\[ G_{\text{tan}} (\text{MPa}) \]

\[ \varepsilon_s (\%) \]

\[ \sigma_h (\text{kPa}) \]

\[ \varepsilon_c (\%) \]

\[ \text{SBPT} \]

Fitted power law
\[ \alpha = 18.367 \]
\[ \beta = 0.643 \]
Figure 20 – Normalised shear stiffness degradation curves for the AE soil derived from the reload paths of SBPT loops.

Figure 21 – Comparison of the normalised tangent shear modulus curves from field and laboratory tests on AE and AP soils.
Figure 22 – Normalised bulk modulus degradation curves for AE and AP soils