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# A Molecular Model For HNBR With Tunable Cross-Link Density

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S1: Force-field parameters and force-field analytical formulation

S2: Volume-temperature plot for  $T_g$

# S1: Force-field

CT =  $sp^3$  carbon, CM =  $sp^2$  carbon, CZ =  $sp$  carbon  
 HC = hydrogen, NZ = nitrogen

## Masses, charges and Lennard-Jones parameters

Type ID	Atom	Mass [g mol <sup>-1</sup> ]	$\sigma$ [Å]	$\epsilon$ [kcal mol <sup>-1</sup> ]	charge [ $e$ ]
1	CT	12.011	3.5	0.066	-0.12
2	CT	12.011	3.5	0.066	-0.18
3	HC	1.008	2.5	0.015	0.06
4	HC	1.008	2.42	0.03	0.115
5	CM	12.011	3.55	0.076	-0.115
6	HC	1.008	2.5	0.03	0.06
7	NZ	14.007	3.2	0.17	-0.56
8	CT	12.011	3.3	0.066	0.04
9	CZ	12.011	3.3	0.066	0.046

## Bond coefficients

Type ID	Atoms	$r_0$ [Å]	$k_b$ [kcal(Åmol) <sup>-1</sup> ]
1	CT-HC	1.09	340.0
2	CT-CT	1.529	268.0
3	CT-CM	1.51	317.0
4	CM-HC	1.08	340.0
5	CM-CM	1.34	549.0
6	CT-CZ	1.47	390.0
7	CZ-NZ	1.157	650.0

## Angle coefficients

Type ID	Atoms	$\theta_0$	$k_\theta$ [kcal mol <sup>-1</sup> ]
1	CT-CM-CM	70.0	124.0
2	CT-CM-HC	35.0	117.0
3	CT-CT-HC	37.5	110.7
4	CT-CT-CT	58.3	112.7
5	CM-CT-HC	35.0	109.5
6	CM-CM-HC	35.0	120.0
7	CM-CT-CT	63.0	111.1
8	HC-CT-HC	33.0	107.8
9	CT-CT-CZ	58.3	112.7
10	CT-CZ-NZ	150.0	180.0
11	HC-CT-CZ	35.0	108.5

## Dihedral coefficients - all $K_i$ are [kcal mol<sup>-1</sup>]

Type ID	Atoms	$K_1$	$K_2$	$K_3$	$K_4$
1	CT-CM-CM-CT	0.0	14.0	0.0	0.0
2	CT-CM-CM-HC	0.0	14.0	0.0	0.0
3	CT-CT-CT-HC	-0.9	0.0	0.3	0.0
4	CT-CT-CT-CZ	0.0	0.0	0.0	0.0
5	CT-CT-CT-CT	0.7	-0.05	0.2	0.0
6	CM-CM-CT-HC	1.116	0.0	-0.372	0.0
7	CM-CT-CT-HC	-1.098	0.0	0.366	0.0
8	CM-CT-CT-CT	0.7	-0.05	0.2	0.0
9	CM-CM-CT-CT	3.058	0.405	-0.904	0.0
10	HC-CT-CM-HC	-0.954	0.0	0.318	0.0
11	HC-CM-CM-HC	0.0	14.0	0.0	0.0
12	HC-CM-CT-CT	0.0	0.0	0.0	0.0
13	HC-CT-CT-HC	-0.9	0.0	0.3	0.0
14	CT-CT-CZ-NZ	0.0	0.0	0.0	0.0
15	HC-CT-CT-CZ	-1.098	0.0	0.366	0.0
16	HC-CT-CZ-NZ	0.0	0.0	0.0	0.0
17	CZ-CT-CT-CM	0.0	0.0	0.0	0.0
18	CM-CT-CT-CM	0.0	0.0	0.0	0.0

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$$U = \left\{ \begin{array}{l}
\overbrace{\frac{1}{2} \sum_{\text{bonds}} k_b (r - r_0)^2}^{\text{bond terms}} + \overbrace{\frac{1}{2} \sum_{\text{angles}} k_\theta (\theta - \theta_0)^2}^{\text{angle terms}} + \\
\overbrace{\frac{1}{2} \sum_{\text{dihedrals}} \{K_1 [1 + \cos \phi] + K_2 [1 - \cos 2\phi] + K_3 [1 + \cos 3\phi] + K_4 [1 - \cos 4\phi]\}}^{\text{dihedral terms}} + \\
\overbrace{\sum_{i,j} \left\{ 4\epsilon_{ij} \left[ \underbrace{\left(\frac{\sigma_{ij}}{r_{ij}}\right)^{12}}_{\text{repulsive}} - \underbrace{\left(\frac{\sigma_{ij}}{r_{ij}}\right)^6}_{\text{VdW}} \right] + \underbrace{\frac{q_i q_j e^2}{r_{ij}}}_{\text{Coulomb}} \right\}}^{\text{repulsive + VdW + Coulomb terms}}}_{f_{ij}}
\end{array} \right.$$

## S2: Volume-temperature plot for $T_g$

Figure S1 shows the typical volume/temperature curves used to determine the glass transition temperature. For the same HNBR structure with 39% ACN content, two different cross-link fractions are shown, i.e., 0 and 50 %. Figure S1 highlights how cross-links alter the density as well as the glass transition temperature for a given system. At the same temperature, the structure with higher cross-link fraction has a lower volume compared to the same structure with zero cross-links. On the other hand, the intersection point between the rubbery and glassy fit is shifted towards higher temperature, i.e., higher glass transition for more cross-linked systems.

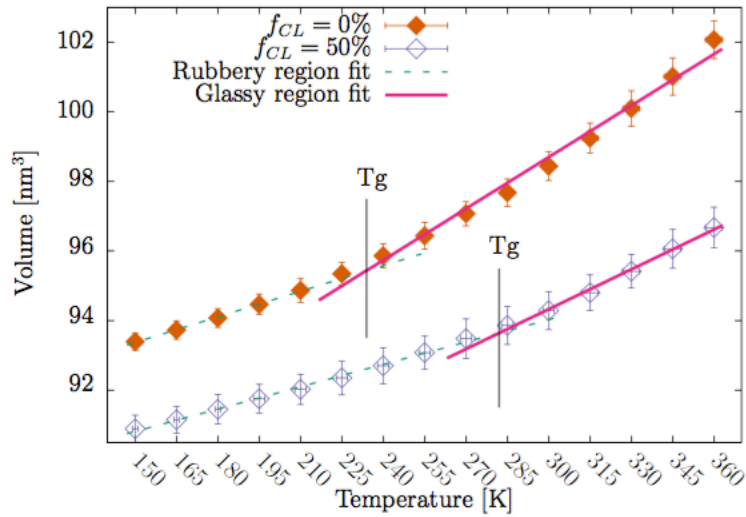


Figure S1: Example of typical volume/temperature curves for HNBR at different cross-link fractions.