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28 **A three-dimensional study of vegetation management on cut slopes**

29 **Tsiampousi, A.**

30 **Abstract**

31 Infrastructure slopes often become covered in dense vegetation due to poor vegetation
32 management. Despite increasing cohesion and enhancing slope stability, high water demand
33 vegetation leads to serviceability problems, primarily towards the end of the summer. Drastic
34 approaches, however, such as vegetation clearance, have caused instabilities during wet
35 seasons. Therefore, appropriate, effective, and continuous vegetation management is of essence
36 and should consider both biodiversity and the engineering asset, while accounting for the
37 contribution of vegetation in battling climate change. Developing numerical methodologies and
38 models can be particularly useful in acquiring insight into the complex mechanism and processes
39 taking place during slope-plant-atmosphere interactions. The work presented here focused for the
40 first time on combining three-dimensional stability and serviceability issues through the
41 development of a 3D numerical model to investigate different vegetation management strategies
42 for a slope covered in high evapotranspiration demand vegetation and suffering serviceability
43 problems. Different 3D patterns of vegetation removal and of replacement with lower water
44 demand vegetation were considered and the effect of each of these on the serviceability and
45 stability of the slope during the subsequent year was examined. The results demonstrated that
46 replacement was preferable to removal, as stability and serviceability should be considered
47 concurrently, and that, occasionally, clearance may have detrimental effects not only on stability
48 but also on serviceability. The importance of considering out-of-plane displacements, which have
49 traditionally been ignored, was revealed, thus providing numerical evidence that a shift in field
50 monitoring is required, to capture the three-dimensionality of the problem.

51 **Key words:** slope stability, serviceability, vegetation, precipitation, soil-atmosphere interaction,
52 3-dimensional effects

53 Introduction

54 Vegetation affects the geotechnical infrastructure on which it grows in multiple ways: from altering
55 the hydraulic (e.g. Leung et al., 2015; Ni et al., 2019a; Dias et al., 2021) and mechanical properties
56 (e.g. Yildiz et al., 2018; Fraccica et al., 2020) of the rooted zone and altering the pore water
57 pressures and the coefficient of earth pressure at rest at depths far exceeding the depth of the
58 rooted zone (Tsiampousi et al., 2014), to contributing with its weight to the stability or instability
59 of sloping ground (Greenwood et al., 2004). Desiccation cracks may form under prevailing
60 evapotranspiration during dry periods (Li & Zhang, 2011), increasing mass soil permeability and
61 promoting water ingress during subsequent wet periods, inducing instabilities (Ng et al., 2001).
62 Ng et al. (2022) provided a thorough review of the state of the art in relation to the hydraulic and
63 mechanical reinforcement of the soil due to the presence of roots, highlighting among other key
64 points, the influence of root architecture.

65 Significant work has been carried out in developing appropriate constitutive models which capture
66 the mechanical and hydraulic reinforcement. Switala et al. (2019) presented a critical state type
67 model which accounted for the root strength and its progressive activation through the increase
68 of preconsolidation pressure (root hardening). Ng et al. (2022) introduced a constitutive model
69 that coupled root effects with the cyclic thermo-mechanical unsaturated soil behaviour. Both
70 models present significant advances over the customary approach of increasing cohesion and
71 present a practical and realistic alternative to analytical models reviewed by Wu (2012). In terms
72 of hydraulic modelling, the work of Ni et al. (2019b) highlighted the differences between bare,
73 single- and mixed-species vegetated soil, and underlined the effect of root decay in the value of
74 saturated permeability. Importantly, it provided means for modelling these effects on soil
75 permeability and soil-water retention curve. Despite the significant advances in the constitutive
76 modelling of rooted zones, a methodology has not yet been developed on how to incorporate
77 them in numerical analyses where vegetation is either cleared or replaced by a different type, and
78 specifically how to deal with the imposed decrease in strength. This becomes a prohibitive issue

79 in numerical analyses where soil states lie on or very close to a certain yield surface
80 corresponding to a certain vegetation type, and the size of the new yield surface, for the new
81 vegetation type, leaves these soil states outside, i.e., representing an impossible stress state.

82 In addition to slope stability, serviceability problems have been related to the presence of
83 vegetation, primarily when evapotranspiration is high (O'Brien, 2013). Tsiampousi et al. (2017)
84 studied numerically the whole life cycle of a slope cut in London clay, demonstrating that high
85 water demand vegetation enhances slope stability but at the expense of serviceability. Vegetation
86 clearance on the other hand, may lead to a rapid loss of stability. These findings are supported
87 by field measurements in similar cut and embankment slopes (Smethurst et al., 2012; Smethurst
88 et al., 2015) and highlight the importance of vegetation management in preserving engineering
89 assets.

90 Owing to the complexity of the coupled hydro-mechanical processes taking place, numerical
91 analysis has proved to be a useful tool in studying soil-atmosphere interaction (Elias et al., 2017),
92 with multiple breakthroughs, from the early attempts of incorporating winter and summer pore
93 water pressure profiles (e.g. Russell et al., 2000; Kovacevic et al., 2001; Nyambayo et al., 2004;
94 O'Brien et al., 2004; Lees et al., 2013), to performing non-coupled (e.g. Tsaparas et al., 2002;
95 Rouainia et al., 2009) and fully-coupled (e.g. Tsiampousi et al., 2017; Pedone et al., 2022;
96 Sitarenios et al., 2021) 2D hydro-mechanical numerical analyses. Switala et al. (2018) considered
97 the effect of vegetation on resisting rainfall induced slope failure in a fully-coupled 3D analysis,
98 demonstrating the beneficial effect of accounting for the additional strength of the vegetated soil.
99 Mao et al. (2014) considered different vegetation scenarios in 3D and studied their effect on slope
100 stability, employing a linear elastic perfectly plastic Mohr-Coulomb model and modifying the soil
101 parameters to account for the effect of roots. They demonstrated that depending on the presence
102 and density of roots beneath the superficial rooted zone, the Factor of Safety may increase by
103 15% and in certain cases over 25%. More recently, Ng et al. (2021) presented a comprehensive
104 theoretical 3D model to capture hydro-mechanical effects of root systems on slope stability.

105 Notably, they differentiated between primary and secondary roots, introducing a pull-out force for
106 the former and an increased cohesion term for the latter. Tsiampousi (2023a) studied the effect
107 of vegetation removal on the stability of a cut slope in a series of fully-coupled 3D analyses,
108 providing useful albeit preliminary insights into 3D effects. Similar to the previous works, the work
109 by Tsiampousi (2023a) focused on slope stability with no consideration for serviceability. It should
110 be noted that the selection of soil model – a linear elastic perfectly plastic Mohr-Coulomb model,
111 where stiffness is independent of stress and strain level – was a major limitation that prevented
112 the combined study of stability and serviceability.

113 This work builds on the work of Tsiampousi et al. (2017), which was loosely based on the case
114 study by Smethurst et al. (2012) from a cut slope in Newbury, SE England. Rather than focusing
115 on the whole-life cycle of the slope in 2D, as Tsiampousi et al. (2017), the current study expands
116 on the subject of vegetation management, considering a plethora of different scenarios where
117 high water demand vegetation is either removed entirely or replaced by vegetation of lower water
118 demand, following various 3D geometrical patterns, in order to establish good practice with
119 reference to both stability and serviceability. Although Lobmann et al. (2020) and Ng et al. (2021)
120 also studied the effect of different vegetation types and/or vegetation spacing on slope stability,
121 there are two major points of differentiation between this and previous works: (a) this work extends
122 to serviceability, whereas previous works focused only on stability and (b) change of vegetation
123 type and/or vegetation clearance is modelled as part of the on-going analysis, whereas in previous
124 work different vegetation types or topology were considered in separate analyses. The second
125 point necessitated some modelling simplifications, in that the hydro-mechanical reinforcement
126 that the roots provide to the soil could not be easily and robustly incorporated in the analysis, as
127 explained above. Nonetheless, ignoring the direct effect of roots facilitates significant
128 computational savings, and provides a safe estimate of the factor of safety, as the beneficial effect
129 of roots on enhancing slope stability is well recognised (e.g., Lobmann et al., 2020, Ng et al.,
130 2021; 2022).

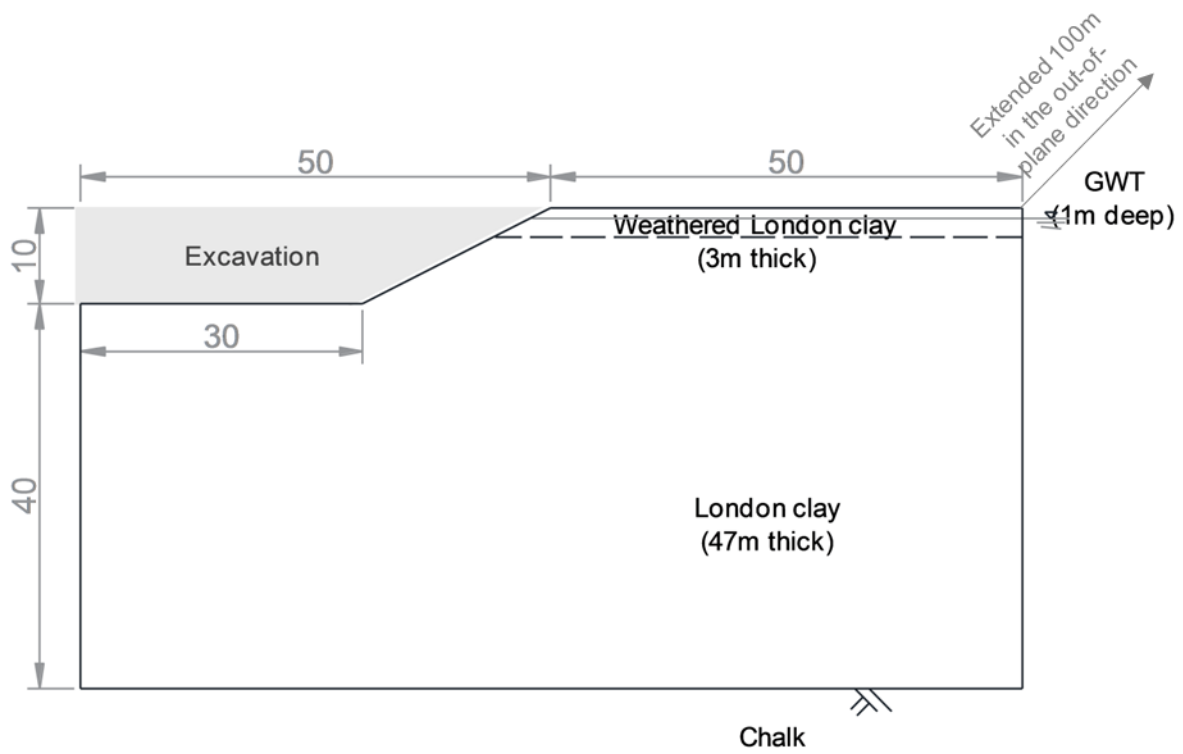
131 The fully-coupled 3D analyses presented here were performed with PLAXIS 3D (Bentley
132 Systems, 2022), employing a user-defined soil model (Taborda et al., 2023a, 2023b), placing
133 emphasis on both the strength and stiffness of London clay, where the Newbury cut was
134 excavated. As explained, the model disregards the effect of roots on the mechanical and hydraulic
135 soil properties and the presence of vegetation is accounted for through an appropriate hydraulic
136 boundary condition. The numerical results provide insight into the mechanisms and interactions
137 taking place during vegetation management and provide guidance as to which approaches to
138 vegetation management may be beneficial and which should be avoided.

139 **Problem description**

140 **Geometry, soil stratigraphy and FE discretisation**

141 The in-plane geometry of the cut slope was typical of cut slopes in London clay, with a depth of
142 10m and a slope of 2:1 (horizontal:vertical) and can be seen in Figure 1. The top 3m of the 50m
143 deep layer of London clay were considered to have been naturally weathered (Smethurst et al.
144 2012) and the chalk bedrock underlying the London clay layer was not considered in the numerical
145 model and was replaced by appropriate boundary conditions, as explained later.

146 The 3D FE mesh used in the analysis extended 100m in the out-of-plane direction and is shown
147 in Figure 2 (a). Figure 2 (b) illustrates an in-plane view zoomed-in around the excavation. Although
148 the elements that were excavated at the beginning of the analysis were also included in the FE
149 mesh, they are not shown in Figure 2 for reasons of visual clarity. The mesh consisted of 10-
150 noded tetrahedral 3D solid elements, each node being assigned three displacement degrees of
151 freedom in the three orthogonal directions and a pore water pressure degree of freedom. The
152 mesh was refined behind the cut slope where a failure mechanism may develop, to accommodate
153 the large changes in displacements and stresses expected in such an event.

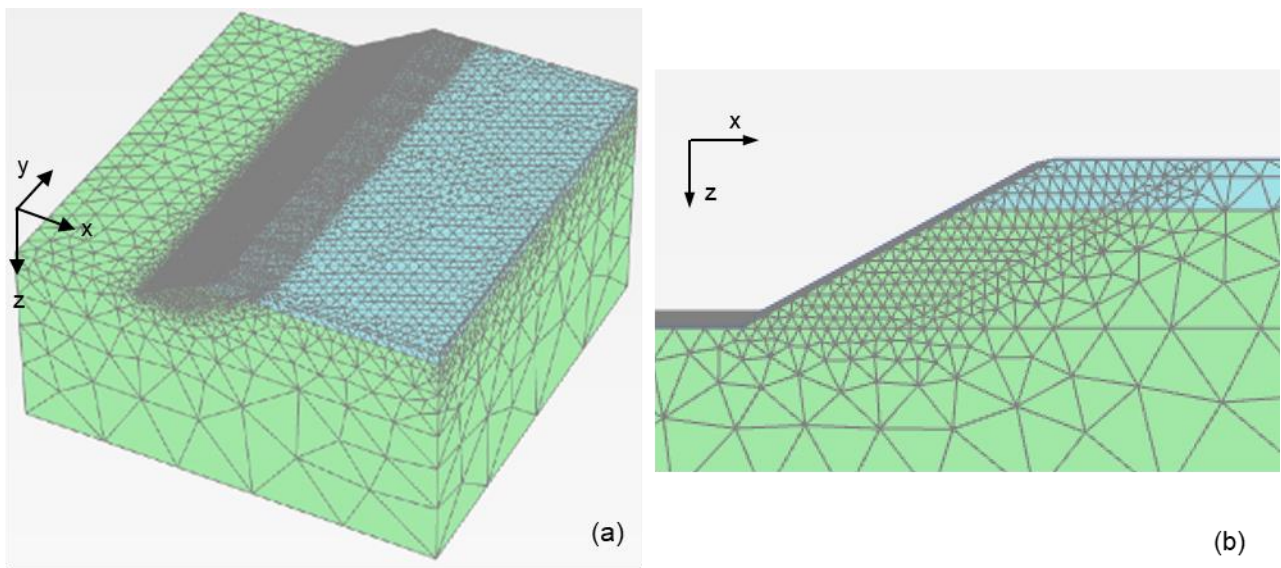


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Figure 1: In-plane problem geometry and soil stratigraphy

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Figure 2: (a) 3D view of the adopted FE mesh; (b) zoomed-in (nearly) in-plane view of the area behind the slope

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163 Soil properties and initial stresses

164 The modelling of the unweathered and weathered layers of London clay differs in relation to their
165 hydraulic behaviour. The unweathered layer was considered to remain fully saturated under the
166 range of suctions expected in the analysis, as London clay can withstand suctions as high as
167 1000 kPa before desaturating (e.g., Dias et al., 2023). To reduce the computational cost, a
168 constant value of permeability equal to 3.47E-9 m/sec was adopted. This value reflects the
169 average operational value of permeability adopted by Tsiampousi et al. (2017) at a depth of 10m,
170 i.e. equal to the excavation depth. As a failure mechanism would potentially initiate from the toe
171 of the slope (Potts et al., 2009) and as serviceability was examined in relation to an engineering
172 asset (e.g., railway, highway) at the bottom of the excavation, this choice was deemed
173 appropriate.

174 The weathered layer was allowed to desaturate with suction and follow the soil-water retention
175 curve shown in Figure 4, which was based on interpreting field measurements of suction and
176 water content by Smethurst et al. (2012). A version of the monotonic van Genuchten (1980)
177 retention curve, which is readily available in PLAXIS 3D and which does not account for the effect
178 of void ratio, was employed and its equation is given here for clarity:

$$S(\psi) = S_{res} + (S_{sat} - S_{res}) \cdot [1 + (g_a \cdot |\psi|)^{g_n}]^{\left(\frac{1-g_n}{g_n}\right)} \quad (1)$$

179 $S(\psi)$ is the current degree of saturation, corresponding to the current value of $\psi = -\frac{p_w}{\gamma_w}$, p_w being
180 the suction and γ_w being the unit weight of the pore fluid. S_{sat} and S_{res} are the saturated and
181 residual degrees of saturation, respectively, and g_a and g_n are fitting parameters similar (but not
182 equal) to parameters α and n in the original paper by van Genuchten (1980). The values adopted
183 to reproduce the curve in Figure 4 are summarised in Table 2.

184 A variable permeability model, also readily available in PLAXIS 3D, was employed to model the
185 variation of relative permeability, $k_{rel}(S)$, with the effective degree of saturation, S_{eff} :

$$S_{eff} = \frac{S(\psi) - S_{res}}{S_{sat} - S_{res}} \quad (2)$$

$$k_{rel}(S) = (S_{eff})^{g_l} \cdot \left\{ 1 - \left[1 - (S_{eff})^{\frac{g_n}{g_n-1}} \right]^{\frac{g_{n-1}}{g_n}} \right\}^2 \quad (3)$$

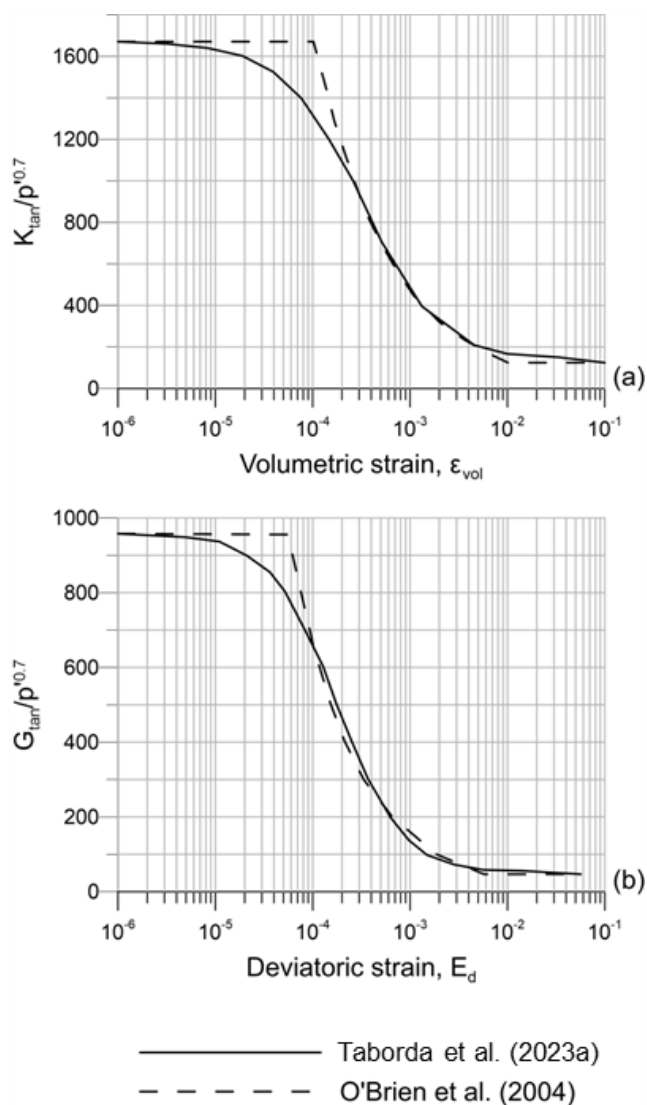
186 where g_l is a fitting parameter. The actual permeability can be calculated by multiplying the
 187 saturated value of permeability by $k_{rel}(S)$. Equation 3 is similar to the Mualem (1976) expression,
 188 if $g_l = 1/2$. The value adopted in the analyses is also shown in Table 2. $k_{rel}(S)$ varies between
 189 1 and a minimum value of 10^{-4} set by the program in order to stop the actual permeability from
 190 obtaining near zero values, which could cause numerical non-convergence.

191 The constitutive model by Taborda et al. (2023a), which combines the Mohr-Coulomb failure
 192 criterion with the Taborda et al. (2016) small-strain stiffness model, was used to simulate the
 193 mechanical behaviour of the clay. This is not a standard feature of PLAXIS 3D and was
 194 implemented into the software as a user-defined soil model (see Taborda et al. (2023a, 2023b)
 195 for details). The same model parameters (Table 1) were adopted for the unweathered and
 196 weathered London clay and were calibrated on London clay data from O'Brien et al. (2004) (bulk
 197 and shear stiffness moduli and their strain-level dependency, Figure 3) and Kovacevic et al.
 198 (2007) (drained shear strength)¹. The beneficiary effect of suction is taken into account through
 199 the change in mean effective stress. The fully saturated model by Taborda et al. (2023a) was
 200 deemed appropriate to simulate the mechanical constitutive behaviour of London clay, primarily
 201 because of its nonlinear elastic stiffness, which depends on both the stress and the strain level.
 202 Not only its air-entry value of suction exceeds the suction levels obtained in the analysis, London
 203 clay is a highly overconsolidated clay, with values of overconsolidation ratio exceeding 6-7,
 204 meaning that features of unsaturated behaviour such as wetting-induced collapse would anyway
 205 be irrelevant (note also that there is further unloading because of the simulated excavation).

¹ Explanation of model parameters can be found in the supplementary file.

206 Furthermore, since strength is of importance in factor of safety calculations, it was necessary to
 207 avoid employing critical state type models which highly overpredict the soil strength on the dry
 208 side of critical state (Tsiampousi et al., 2013a).

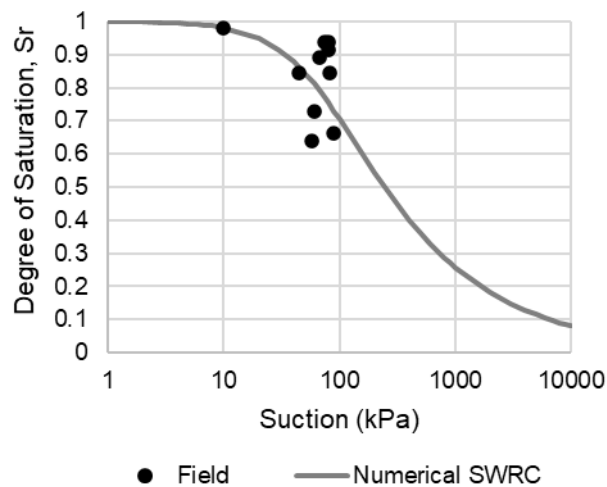
209 The unit weight of the two layers was 19.1 kN/m^3 both above and below the groundwater table,
 210 which was assumed to be at a depth of 1m. The initial pore water pressure distribution with depth
 211 was hydrostatic and the coefficient of earth pressure at rest K_0 was 2.1, consistent with the high
 212 values of overconsolidation ratio (e.g., Hight et al., 2007).



213
 214 Figure 3: Degradation of (a) Bulk stiffness with volumetric strain and (b) of Shear Stiffnesses
 215 with deviatoric strain (adapted from Tsiampousi et al., 2017)

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219 Figure 4: Soil-water retention curve for the weathered layer; field data interpreted from
220 Smethurst et al. (2012)

221

222 Analysis sequence and boundary conditions

223 The excavation was performed in an undrained manner at the beginning of the analysis, in five
224 phases in each of which a 2m deep soil layer was excavated. The subsequent phases of the
225 analysis modelled soil-atmosphere interaction for five years and were fully coupled: the slope and
226 the horizontal ground behind the crest of the slope were covered in high water demand (HWD)
227 vegetation, whereas the newly formed boundary at the bottom of the excavation, hosting the
228 engineering asset, remained bare. This five-year period aimed to reproduce repeatable year-on-
229 year pore pressure regimes for each of the twelve months of the final two years², and therefore,
230 representative conditions at the initiation of vegetation management, which was studied in detail
231 in Year 6.

232 Conditions during Years 1 to 5 were equivalent to plane strain. 3D effects were introduced in the
233 6th year of the analysis, when different vegetation management scenarios were considered,

² See supplementary file for pore water pressures

234 ranging from vegetation clearance to replacing HWD vegetation with lower water demand (LWD)
235 vegetation at different areas and patterns on the slope. The way different types of vegetation were
236 simulated in the analysis is a of great importance, as they affect the pore water pressures in the
237 slope and by extension its stability and serviceability.

238 The infiltration boundary condition in PLAXIS 3D was used to simulate soil-atmosphere
239 interaction. This is a dual boundary condition, changing automatically from applied inflow/outflow
240 with a user-prescribed rate to a user-prescribed head condition and vice versa. This requires that
241 rainfall and evapotranspiration rates are manually combined prior to inserting a single net value
242 to be applied in the analysis. Average long-term monthly climate data, extracted from Smethurst
243 et al. (2012) and shown in Figure 5, were used to calculate the net rates that were applied on the
244 flat ground covered by HWD vegetation. Note that rainfall and evapotranspiration rates in Figure
245 5 are both plotted as positive to facilitate visual comparison, whereas net rates are shown as
246 positive when referring to inflow and as negative when referring to outflow. The climatic year
247 applied started in April (beginning of the “dry” season) and finished in March (end of the “wet”
248 season).

249 Following the assumption made by Tsiamposi et al. (2017), a drainage system capable of
250 capturing and removing 50% of the rainfall was present in the slope. For simplicity, and for directly
251 comparing the effect of lowering water demand, no further changes in rainfall rates were applied
252 (e.g., due to leaf intercept). Smethurst et al. (2012) estimated the potential evapotranspiration to
253 be 25% less on the Newbury slope than what they calculated for a flat open site. The same
254 reduction as a percentage was assumed here. The adjusted rates corresponding to sloping
255 ground are also shown in Figure 5.

256 At the flat ground behind the crest of the excavation, the maximum possible head was set to -
257 1m (or ~10 kPa of suction) to maintain the position of the initial water table, as field data have
258 shown that total loss of suction is unlikely (e.g., Smethurst et al., 2012; Smethurst et al., 2015).
259 On the sloping ground, however, the maximum possible head was set to 0m (or 0kPa of pore

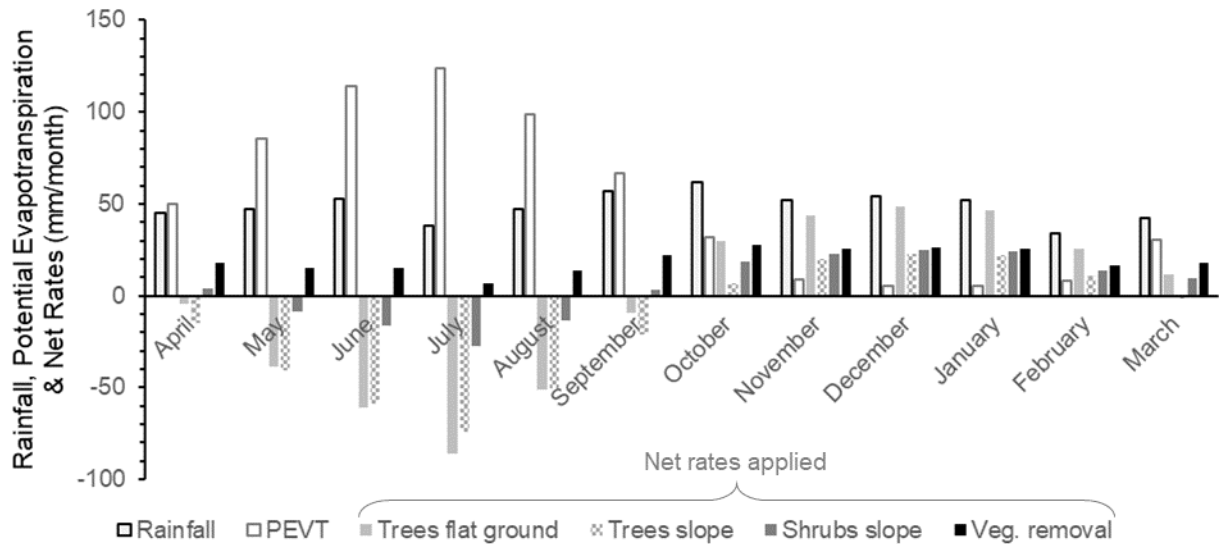
260 water pressure), so that no suctions were maintained artificially at areas where stability may be
261 critical. The minimum possible head was set equal to -150m (or ~1500 kPa of suction) for the
262 whole vegetated area (flat or sloping ground) and agrees with previous values reported in the
263 literature (e.g., Nyambayo & Potts, 2010).

264 As explained in the next section, different vegetation management scenarios were considered
265 where HWD vegetation was either removed or replaced by LWD vegetation. To simulate
266 vegetation removal from the slope, the potential evapotranspiration rates were reduced to 10% of
267 those applied on the slope when it was covered in HWD vegetation, while the slope rainfall rates
268 remained unchanged. This would qualitatively reflect evaporation conditions on a north-facing
269 slope (which would be the critical one). A similar process was followed when calculating the net
270 rates corresponding to LWD vegetation, with the difference that the evapotranspiration rates were
271 reduced to 50% rather than to 10%. The same rates had been assumed by Tsiampousi et al.
272 (2017).

273 Throughout the fully coupled phases of the analysis, seepage was allowed at the bottom of the
274 excavation, where the engineering asset is located. Suctions generated during the undrained
275 excavation could dissipate through this boundary, but water could not pond on it. All vertical
276 boundaries were impermeable (planes of symmetry), with the exception of the right-hand-side
277 out-of-plane vertical boundary, where seepage was allowed and pore water pressures changed
278 in response to the applied inflow/outflow rate at the top boundary of the FE mesh. Pore water
279 pressures were left unchanged at the interface with the permeable chalk at the bottom boundary.
280 The horizontal displacements at the four vertical boundaries and the horizontal and vertical
281 displacements at the bottom boundary were fixed throughout the analysis.

282 As explained above, the analysis is loosely based on the case study of the Newbury cut slope
283 (Smethurst et al., 2012), which had previously been used to validate the numerical methodology
284 adopted here (e.g., Tsiampousi et al., 2017; Tsiampousi et al., 2023b). This methodology is

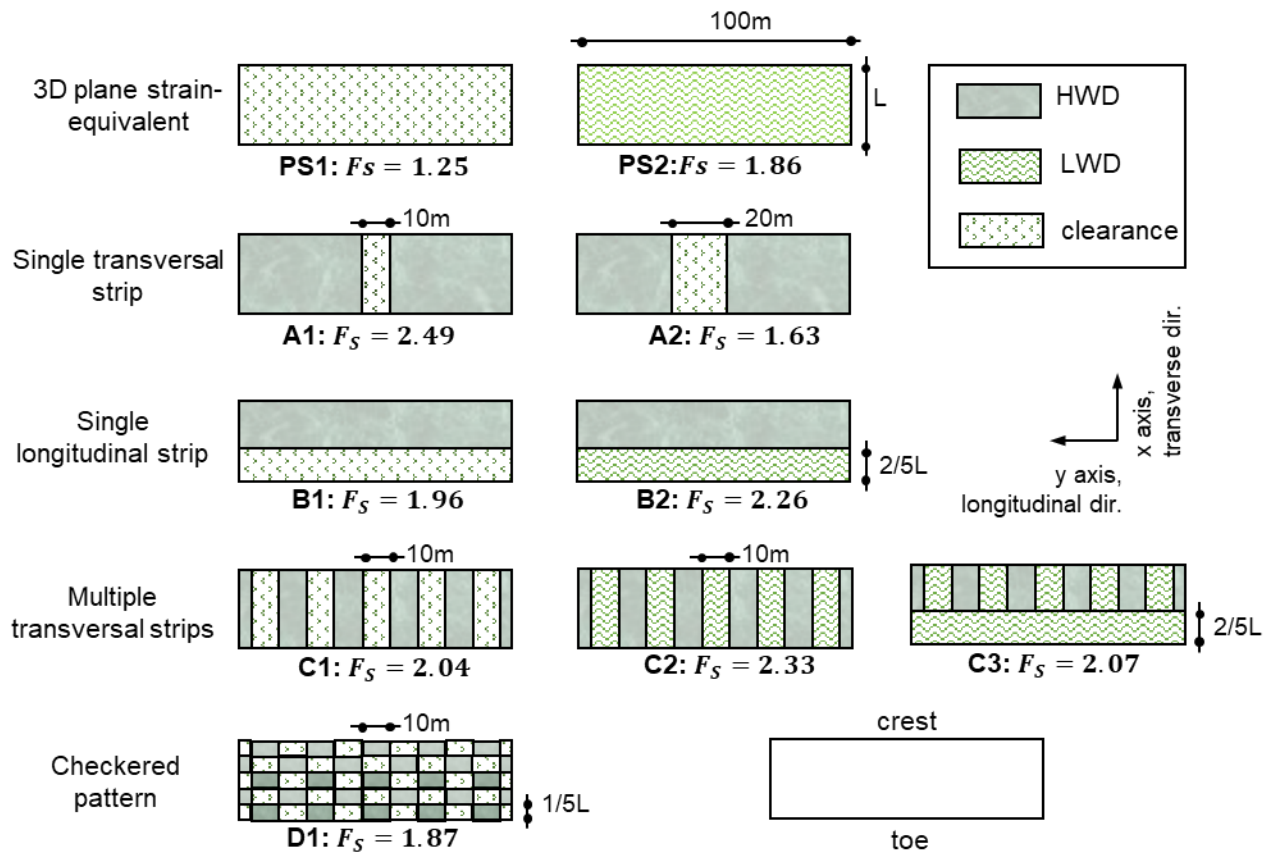
285 expanded here to a generic 3D hypothetical case, as vegetation management scenarios such as
 286 the ones adopted in the analyses have not yet been trialled in the field.



287
 288 Figure 5: Precipitation, potential evapotranspiration and net rates for a typical year (negative
 289 values of net rates indicate that potential evapotranspiration exceeds precipitation rates)

290 **Cases considered**

291 Ten different scenarios of vegetation removal, where HWD vegetation was removed leaving only
 292 low and sparse vegetation behind, and vegetation replacement, where HWD was replaced by
 293 LWD vegetation, were considered during the 6th Year of the analysis, which was dedicated to
 294 vegetation management. They are shown schematically in Figure 6, which illustrates a plan view
 295 of the slope, where vegetation management was applied. The boundary conditions on the
 296 remaining of the FE mesh, including on the flat ground behind the crest of the slope, were left
 297 unchanged.



298

299 Figure 6: Schematic reproduction of the vegetation management scenarios PS1-2, A1-2, B1-2,
 300 C1-3 and D1; plan view of the slope (see sketch at bottom right for orientation).

301 **Factor of safety**

302 The factor of safety (FoS) against failure was calculated at the end of Year 6 in each of the
 303 analyses in order to capture the FoS and the corresponding failure mechanism at the end of the
 304 wet period, after one year of vegetation management. The FoS phases of the analyses were
 305 drained meaning that pore water pressures were not allowed to change as per previous analyses
 306 (e.g., Tsiampousi et al., 2013b; Tsiampousi et al., 2016; Tsiampousi et al., 2017). A c'/φ' reduction
 307 technique, which applies partial factors of safety on cohesion and the tangent of the angle of
 308 shearing resistance until failure is achieved, was implemented within the user-defined constitutive
 309 model and its integrator for the purposes of this study. Failure was manually verified in each case
 310 by examining whether a failure mechanism was fully developed by assessing vectors of

311 incremental displacements. FoS are reported to an accuracy of 2 decimal places. This bears little
312 engineering significance, a fact which should be accounted for when evaluating the analysis
313 results, and was done for theoretical consistency between the reported FoS and the
314 corresponding failure mechanism: e.g., a number of analysis steps were carried out between FoS
315 of 1.6 and 1.63 in A2 (see Figure 6) in which the failure mechanism evolved towards its final shape
316 and location.

317 **Effect of HWD vegetation on slope serviceability**

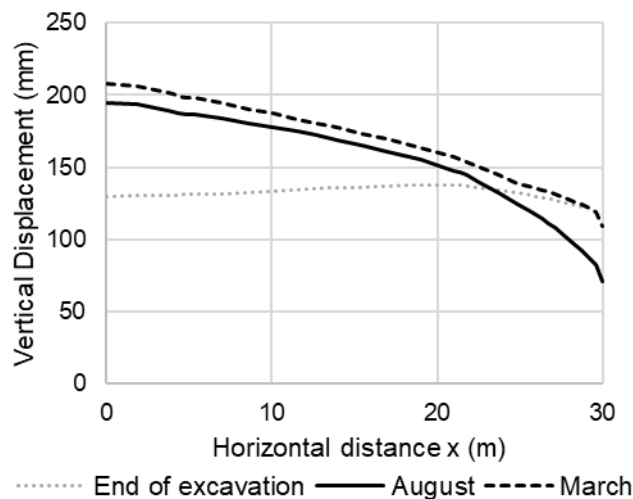
318 Before exploring vegetation management, the impact of current vegetation on the serviceability
319 of the slope was established through careful examination of the displacements computed in the
320 first 5 years of the analysis, simulating the presence of HWD vegetation on the slope. This phase
321 of the analysis was common for all ten vegetation management scenarios considered, meaning
322 that all subsequent results could be benchmarked against the results of this phase.

323 Figure 7 shows the total vertical displacements at the bottom of the excavation along a line
324 perpendicular to the slope toe in August and March of Year 5 in comparison to the vertical
325 displacements at the end of the undrained excavation. This monitored line would be perpendicular
326 to the axis of the engineering asset. Until Year 5 the analysis is essentially equivalent to plane
327 strain and therefore the exact location of this line along the y-axis (longitudinal direction) is
328 irrelevant. In the present case, for simplicity, a line in the middle of the model (at $y = 50\text{m}$) was
329 selected.

330 It can be observed that the vertical displacements at the end of the excavation showed little
331 variation along the monitored line. Their magnitude is associated to the short-term unloading
332 taking place. Note that in this undrained part of the analysis, the overall soil volume remained
333 unchanged, and the local displacements seen here were compensated for elsewhere in the FE
334 mesh to produce a net zero volume change.

335 By the end of August of Year 5, heaving had occurred at the centre of the excavation ($x = 0\text{m}$)
336 and shrinkage at the toe ($x = 30\text{m}$). The former was due to the dissipation of tensile excess pore
337 water pressures that developed during the excavation (swelling), whereas the latter was
338 associated with the action of vegetation on the slope during the dry period, when
339 evapotranspiration exceeds rainfall, and a net outflow is obtained. A large differential
340 displacement, in excess of 120 mm, is obtained as a result. This would be a significant differential
341 displacement for an engineering asset, in particular for a railway. By the following March, swelling
342 had occurred in relation to August, which was larger around the toe than at the centre, hence
343 reducing the magnitude of the differential displacements to about 100 mm, which was still
344 significant.

345 The analysis results clearly underline the need for vegetation management in slopes covered in
346 HWD vegetation. When the entire slope was cleared of its vegetation in PS1 (see Figure 6), the
347 FoS one year later had reduced to 1.25 from 2.6 at the end of Year 5. In agreement with what has
348 already been observed in the literature (Smethurst et al., 2015; Tsiampousi et al., 2017), simply
349 clearing vegetation has the potential to alter a serviceability problem into a stability problem.
350 Therefore, both stability and serviceability need to be considered while managing vegetation.



351

352 Figure 7: Vertical displacements at the bottom of the excavation along a line perpendicular to
353 the toe at $y = 50\text{m}$ for Year 5; $x = 0\text{m}$ corresponds to the centre of the excavation, $x = 30\text{m}$
354 corresponds to the toe of the slope

355 **Width of vegetation removal**

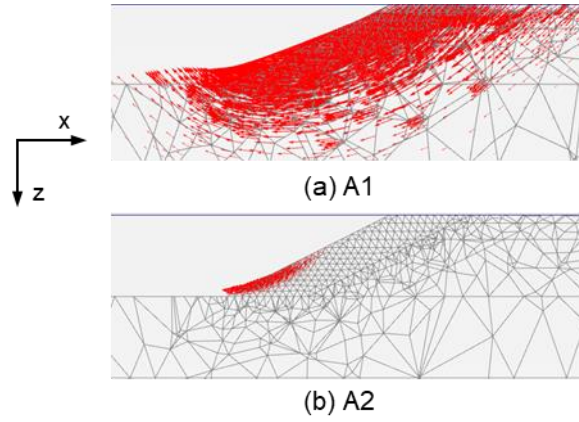
356 The aim of analyses A1 and A2 was to establish what effect the width of vegetation removal has
357 on the stability of the slope in order to adopt a reasonable value in the subsequent analyses which
358 were devoted in studying vegetation management under 3D conditions.

359 The FoS prior to vegetation removal, i.e., at the end of the wet period (March) of Year 5, was
360 calculated to be 2.6. The FoS at end of March of Year 6, i.e., following vegetation clearance,
361 reduced to 2.49 for scenario A1 and 1.63 for scenario A2 (see also Figure 6). The corresponding
362 failure mechanisms are shown in Figure 8. It should be noted that it is the relative and not the
363 actual magnitude of the vectors of incremental displacements that is of interest, as this is what
364 demonstrates the existence of a failure mechanism. It is evident that the failure mechanism for a
365 10m wide clearance strip (A1) was significantly deeper than the mechanism for a 20m wide
366 clearance strip (A2). In the latter case, the mechanism was limited to the toe of the slope, whereas
367 in the former this was not the case, and a much deeper area of the FE mesh was mobilised.

368 To investigate the longitudinal extent of the failure mechanism in the y -direction, the transverse
369 incremental displacements (i.e., the displacements in the x -direction) were examined for the
370 failure step. Figure 9 illustrates the incremental transverse displacements along the toe of the
371 slope for the two scenarios, normalised by the maximum absolute value. For scenario A2, the
372 failure mechanism was centred about the centre of the clearance strip ($y = 55\text{m}$) and was
373 contained within its 20m width, in that the transverse displacements were zero outside the 45 –
374 65m y co-ordinate. For scenario A1, the soil along the whole longitudinal extent of the mesh in y -
375 direction was mobilised, with displacements being the largest within the 10m wide clearance strip
376 (centred at $y = 50\text{m}$) but not limited to within the width of this strip.

377 Figure 10 shows contours of suctions at the end of March of Year 6 on the slope (top views in (a)
378 and (b)) and at cross sections at the centre of the respective clearance strips and 10m away ((c)
379 to (f)), for scenarios A1 and A2. From the top views ((a) and (b)), it is evident that vegetation
380 clearance affected primarily the suctions at the clearance strip, and, to a much lesser extent,
381 outside it, with the biggest affect outside the strips concentrated at the bottom half of the slope
382 and in the vicinity of the strips. Although there were some small differences in the values and
383 shapes of contours at the central cross-sections for A1 and A2 ((c) and (d)), the differences were
384 more significant in the cross-sections located 10m away from the centre of the strip ((e) and (f)),
385 with A1 having resulted, unsurprisingly, to higher suctions. These higher suctions 10m away from
386 the centre of the clearance strip in A1 aided the soil to resist the full development of a failure
387 mechanism, mobilising the shear strength of areas further away. Nonetheless, the suctions further
388 away are equally large and become progressively, albeit slightly, larger, impeding the formation
389 of a fully developed failure mechanism. This explains why transverse displacements at the last
390 step of the FoS analysis were non-zero even at $y = 0$ and 100m (Figure 9) and why the calculated
391 value of F_s (2.49) was only slightly smaller than the value of F_s (2.6) at the same month (March)
392 prior to vegetation clearance.

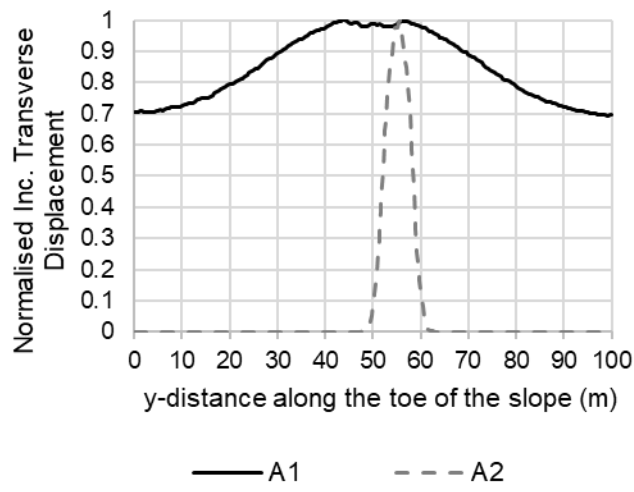
393 The results of analyses A1 and A2 indicated that although a single 20m wide clearance strip was
394 wide enough for a fully developed failure mechanism to develop within it, with a significant
395 reduction in FoS, a single 10m wide clearance strip was narrow enough to avoid a failure
396 mechanism developing within it, mobilising the strength of soil in areas still covered in HWD
397 vegetation. This observation supports the choice of 10m wide strips when studying vegetation
398 clearance in scenarios C1 and D1, but also when considering vegetation replacement in scenarios
399 C2 and C3, to allow for direct comparison between cases.



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401

Figure 8: Vectors of incremental displacement at failure for scenarios A1 and A2



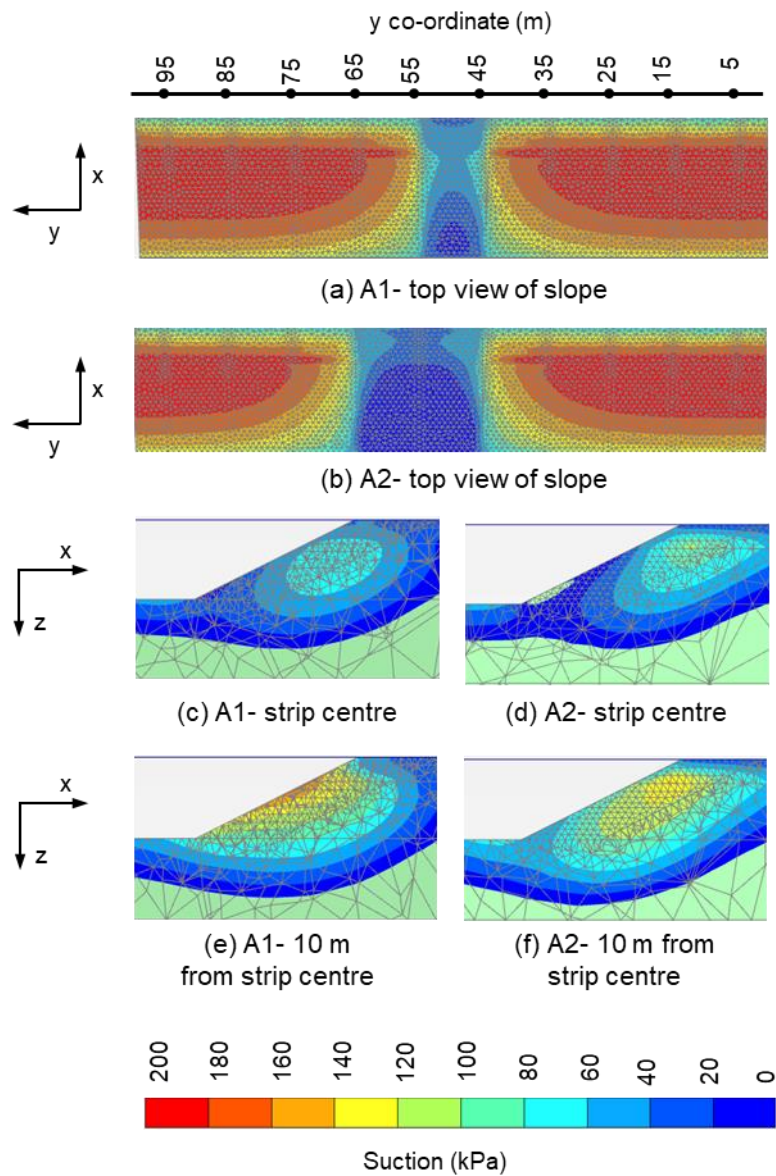
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Figure 9: Normalised incremental transverse displacement (i.e., in the x-direction) along the toe of the slope for scenarios A1 and A2



406

407

Figure 10: Contours of suction (kPa)

408 **Stability**

409 **Vegetation removal**

410 The FoS for scenarios B1, C1 and D1 simulating vegetation removal have been included in Figure
 411 6. The respective failure mechanisms at the last converged step of the FoS analyses are shown
 412 in Figure 11 (a) to (c). The failure mechanisms extended longitudinally to the whole width of the

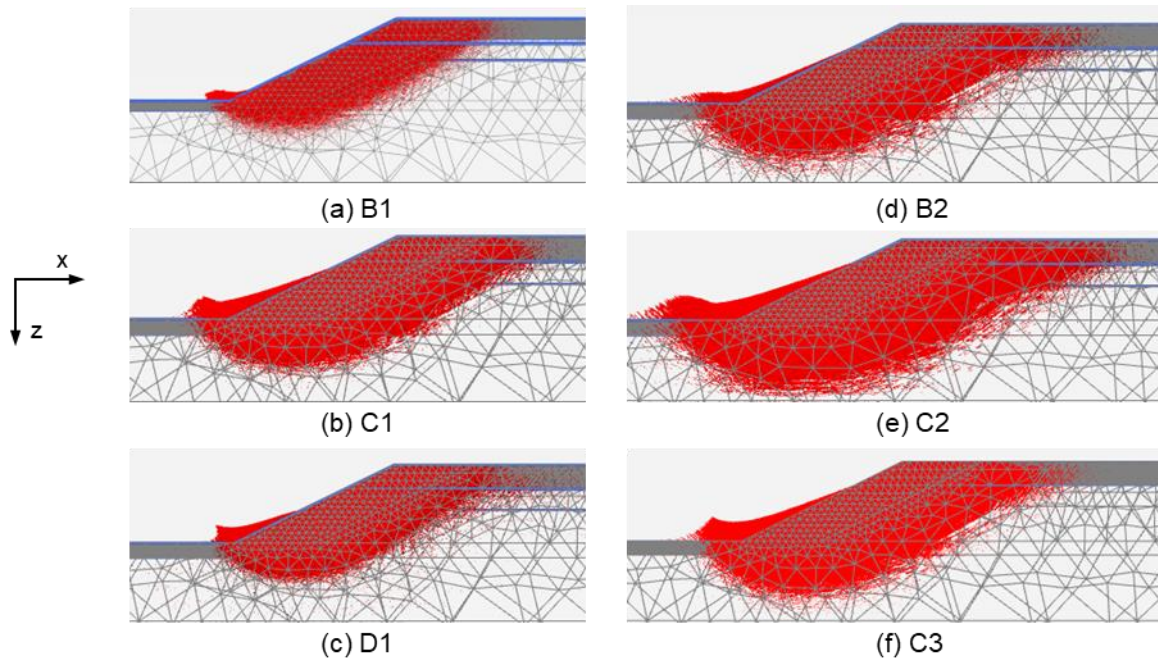
413 FE mesh, owing either to conditions being equivalent to plane strain (B1) or to the closely repeated
414 pattern of vegetation (C1 and D1).

415 With particular reference to C1 in relation to A1, the FoS reduced visibly when multiple 10m wide
416 strips were considered. It was seen that the single strip in A1 was not of adequate width for a
417 failure mechanism to fully develop within it, mobilising the shear strength of the soil in areas
418 outside it. The longitudinal extent of these areas on either side of the single strip in A1 exceeded
419 by far the 10m width of the vegetated strips in C1 which remained intact between the cleared
420 strips (Figure 9), which explains the reduction in FoS.

421 All three cases, B1, C1 and D1, yielded a FoS which was larger than PS1 (also summarised in
422 Figure 6), indicating that maintaining some HWD vegetation on the slope is beneficial for its
423 stability. C1, which resulted in the deepest failure mechanism, also resulted in the largest FoS.
424 This is perhaps not surprising when comparing C1 to B1, as in C1 HWD vegetation is still present
425 intermittently at the toe, where failure initiated in the analysis, increasing overall the pore water
426 pressures, whereas in B1 HWD vegetation was cleared entirely from the toe. Interestingly, this
427 pattern was not observed in D1, which produced the smallest FoS and where HWD vegetation
428 was also present intermittently at the toe, albeit at a different pattern than in C1. Considering an
429 in-plane (i.e., transversal to the slope) cross-section, the failure mechanism initiated at the toe
430 and propagated upwards with increasing partial factors of safety. Continuous presence of HWD
431 vegetation (i.e., increased pore water pressure) in regularly repeated in-plane cross-sections in
432 C1 provided extra in-plane stability at these cross-sections. This was not the case in in-plane
433 cross-sections in D1, where there was no continuity of HWD vegetation. Continuous presence of
434 HWD vegetation at the upper part of the slope in B1 also assisted in-plane stability in comparison
435 to D1, albeit to a lesser extent than in C1.

436 Following vegetation clearance, slope stability was enhanced by the presence of HWD vegetation
437 at the toe, even when this was intermittent in the out-of-plane (longitudinal) direction, as long as
438 there was continuity of HWD vegetation in in-plane cross sections, which were equally spaced in

439 this particular case. Further checkered patterns were not considered (e.g., for vegetation
440 replacement), as they would be mechanically, as well as economically (e.g., increased cost of
441 maintenance of this elaborate pattern), of low interest.



443 Figure 11: Vectors of incremental displacement at failure

444 **Vegetation replacement**

445 The FoS for scenarios B2, C2 and C3 simulating vegetation replacement can be found in Figure
446 6 and the respective failure mechanisms in Figure 11 (d) to (f). All three cases yielded a FoS
447 which was larger than PS2, indicating again that maintaining some HWD vegetation on the slope
448 is beneficial for its stability. A similar relationship between B2 and C2 in terms of calculated FoS
449 was obtained as for B1 and C1, indicating that conclusions drawn from the vegetation clearance
450 exercise can be extrapolated to vegetation replacement, with particular reference to the presence
451 of HWD vegetation at the toe. This is further supported by the lower FoS computed for C3, which
452 combined absence of HWD vegetation at the toe and intermittent present of HWD vegetation at
453 the upper part of the slope and produced the lowest FoS out of the three vegetation replacement
454 analyses. When compared directly to their respective vegetation clearance scenarios, the

455 vegetation replacement scenarios B2 and C2 yielded higher FoS and deeper failure mechanisms.
456 This is of course expected, as LWD vegetation potentially maintains higher suctions through
457 evapotranspiration than in the case of vegetation clearance, which is reflected in the net rates
458 that have been applied in the analyses (Figure 5). The FoS for C3, although smaller than for other
459 vegetation replacement analyses, was comparable to the highest FoS for vegetation clearance
460 (C1), indicating that replacing rather than clearing vegetation may generally be a better option,
461 not only for enhancing biodiversity, but also for the stability of the slope irrespective of the actual
462 pattern followed, as long as some continuity of HWD vegetation in in-plane cross-sections is
463 maintained. Nonetheless, replacing vegetation would be a more expensive approach to
464 vegetation management than clearing vegetation, and one requiring further resources (e.g.,
465 frequent but careful irrigation during plant growth season, until the new vegetation gets
466 established). Furthermore, its impact on serviceability in comparison to vegetation clearance also
467 needs to be taken into account.

468 **Serviceability**

469 **Vegetation removal**

470 The vertical displacements computed for the vegetation removal scenarios at the bottom of the
471 excavation perpendicular to the slope toe are shown in Figure 12 (a) for August and in Figure 12
472 (b) for March of Year 6 and are compared with the corresponding displacements from Year 5. For
473 B1 and D1, the monitoring line was at $y = 50\text{m}$, and for C1 at $y = 60\text{m}$, coinciding with the centre
474 of a HWD vegetated strip, where, as discussed subsequently, the differential displacements were
475 the largest.

476 Starting with August, further swelling occurred between Years 5 and 6. The removal of HWD
477 vegetation reduced the shrinkage at the toe in all three vegetation management analyses, with
478 the vertical distance of the respective curves from the curve for Year 5 being larger at the toe of
479 the slope ($x = 30\text{m}$) than at the centre of the excavation ($x = 0\text{m}$). As a result, the differential

480 displacements between the toe and the excavation centre reduced from 120mm to roughly 75,
481 110 and 100 mm, in B1, C1 and D1, respectively.

482 Although B1 seemed to lessen the serviceability problems by 37.5% in August (by 45mm out of
483 the initial 120), in March upward vertical displacements accumulated at the toe as a result of the
484 increased rainfall infiltration following HWD vegetation removal from the entire longitudinal strip
485 along the toe. If the width of the asset is significantly smaller than the width of the excavation and
486 it is centred around the centreline of the excavation, serviceability will have improved. If, however,
487 the whole width of the excavation is made use of to host the asset, then serviceability at the edge
488 of the excavation has markedly deteriorated. A similar upward displacement close to the toe in
489 relation to March of Year 5 can also be observed for D1, albeit significantly smaller in magnitude.
490 This can be explained by the partial, rather than total, removal of HWD vegetation from the toe,
491 which contributed to the overall pore water pressures around the slope remaining higher than in
492 B1. Despite the swelling that occurred around the toe for C1 between August and March, this was
493 not as significant as in B1 and D1. It would be difficult to differentiate the effect of swelling at the
494 toe because of decreasing suctions during the wet period following vegetation clearance, from
495 the effect of reducing stiffness due to reducing effective stresses and due to shearing (note the
496 difference in FoS in the three analyses, which signifies that the FoS calculation phase started
497 from significantly different stress states). It is likely that the displacements at the toe are a
498 combination of all these interacting mechanisms in these coupled consolidation analyses, where
499 stiffness was a function of both stress and strain.

500 The vertical displacements in Figure 12 are presented normalised in Figure 13 for further
501 comparison. The normalisation presented refers to the maximum value of $\Delta\text{displacement}/\Delta x$ for
502 each curve, i.e., is a worst-case scenario sort of slope. A reduction in the normalised vertical
503 differential displacement signifies an overall improvement in serviceability. With reference to the
504 August results, B1 produced the largest improvement between the three vegetation clearance
505 scenarios (B1, C1 and D1). However, the same analysis yielded the worst results for March. The

506 improvement for C1 was less significant in August (when the serviceability issues are more
507 critical) than in March. For D1 there was hardly any improvement in March, and the improvement
508 was more significant in August.

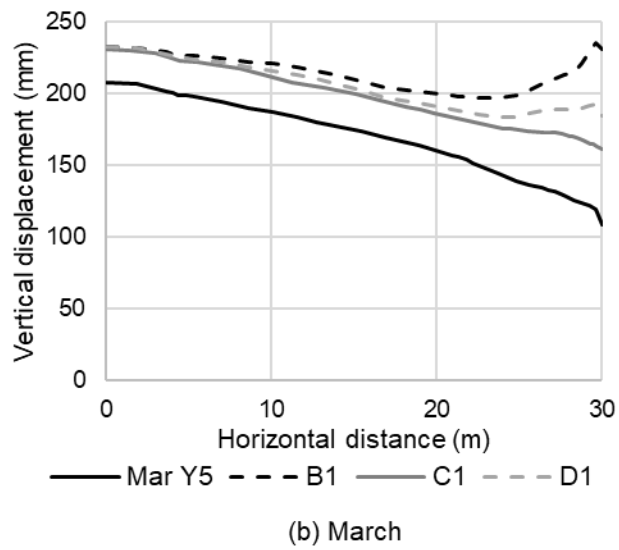
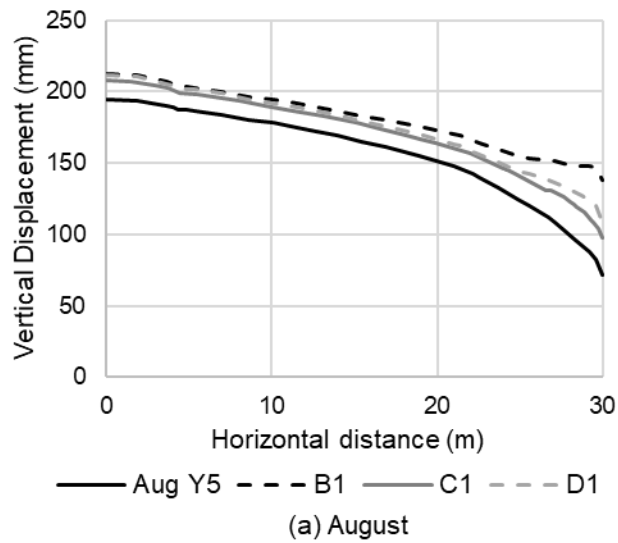
509 To put these displacements into perspective, the cross-level maintenance tolerance in high cant
510 deficiency curves is set by Network Rail (2022) in the UK to 10 mm (cross-level refers to the
511 difference in elevation between tracks). Considering that track gauge is typically 1,435 mm, this
512 gives a normalised ratio equivalent to that plotted in Figure 13 of just 6.97. It should be highlighted
513 that there is no direct relationship between ground movements and track geometry, the track
514 geometry being used in Network Rail standards for both design and maintenance, and therefore
515 comparison between this value and the values in Figure 13 is only indicative of the potential
516 significance of the computed displacements.

517 Figure 14 plots the transversal, longitudinal and vertical displacements (in the x- and y- and z-
518 directions) displacements in August for C1 and D1 along the toe of the slope (note that B1 is an
519 equivalent plane-strain analysis, therefore, yielding uniform displacements in the out-of-plane).
520 Perhaps unsurprisingly considering the extent of the HWD vegetated zone up the slope in the two
521 cases, the differential displacements were larger for C1 than D1. The magnitudes of the
522 differential displacements (marked in Figure 14) may not seem very large. However, the
523 longitudinal and transversal differential displacement, in combination with the prevalence of
524 evapotranspiration during August, may contribute to desiccation cracking and increased inflow of
525 rainfall water during the next wet period, exacerbating the seasonal changes of pore water
526 pressures year-on-year, and therefore, further contribute to poor serviceability. The vertical
527 differential displacements occur within a distance of 10m, so in normalised terms they are
528 comparable to the differential displacements in Figure 12. This may or may not be acceptable,
529 depending on the nature and geometry of the engineering asset, but it should be noted that
530 differential displacements tend to become progressively worse with time, and therefore, while
531 attempting to solve serviceability issues perpendicular to the asset axis, the approach in C1 and

532 D1 may inadvertently induce new serviceability issues along its axis, with C1 presenting a worse
533 outcome than D1.

534 An indication of the significance of the calculated vertical displacements can be obtained by
535 considering the Network Rail (2022) maintenance limits for cyclic top, i.e., for series of regularly
536 spaced drops in the vertical alignment of the tracks, a fault which can potentially cause derailment.
537 For example, cyclic tops of 20 to 23 mm on one rail, or 43 to 46 mm on both rails need to be
538 corrected within 60 days. Very importantly, it is required that the trigger is also rectified to ensure
539 that the fault does not re-occur. The wavelength for cyclic top depends on the train speed and is
540 typically recorded at 4.5, 6, 9, 13 and 18 m, i.e., at distances relevant to the wavelength of 10 m
541 encountered in the analysis. Similarly, to put the transversal displacements into perspective, the
542 35 m horizontal alignment of the track can be considered: Network Rail (2022) identifies a 30 mm
543 intervention limit and a 25 mm maintenance tolerance. As highlighted earlier, a direct relationship
544 between ground movements and track geometry has not been established, so these comparisons
545 should only be seen as an indication of the relative significance of the computed ground
546 movements.

547 The observed differential vertical displacements along the toe have yet another implication in the
548 interpretation of the results. Although the minimum vertical displacement for C1 was obtained at
549 $y = 60\text{m}$, the minimum vertical displacement for D1 was obtained at $y = 50\text{m}$, coinciding in both
550 cases with where the HWD vegetation remained untouched at the toe of the slope and contributed
551 to local shrinkage. The transversal (in-plane) sections where the minimum vertical displacements
552 are obtained at the toe suffer the worse serviceability issues (largest difference with centre-line
553 vertical displacements). This has practical implications for the interpretation of the numerical
554 results, as well as for field monitoring of differential displacements across the route of the asset,
555 which should ideally be centred about the HWD vegetated areas.

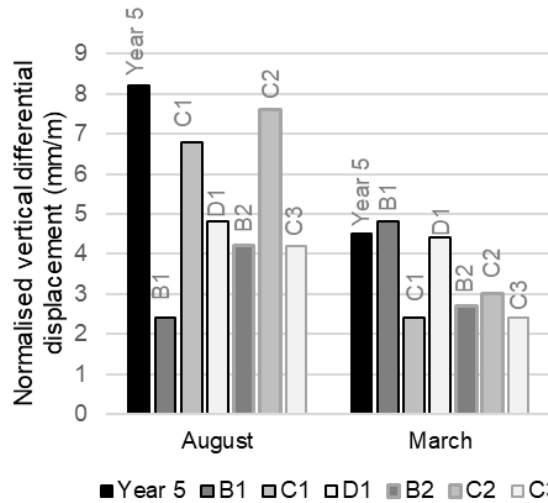


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557 Figure 12: Vertical displacements at the bottom of the excavation along a line perpendicular to
 558 the toe for Year 6 (at $y = 50\text{m}$ for B1, D1 and at $y = 60\text{m}$ for C1) in comparison with Year 5 (a) in

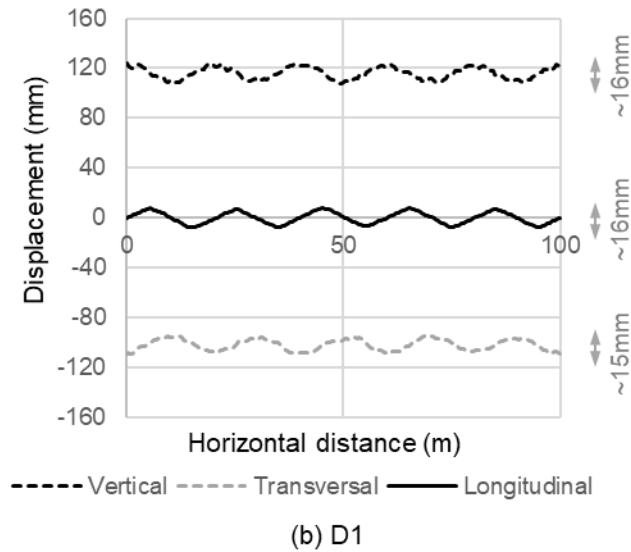
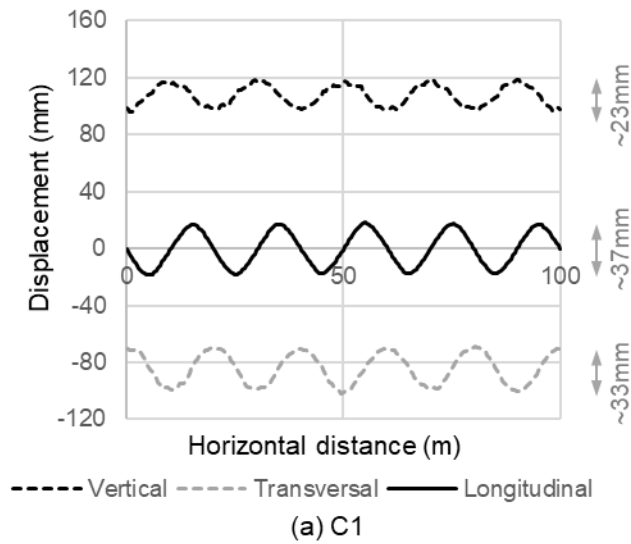
559

August and (b) in March



560
561

Figure 13: Normalised vertical differential displacements in August and March



562
563

Figure 14: Transversal (x), longitudinal (y) and vertical (z) displacements along the toe for scenarios (a) C1 and (b) D1

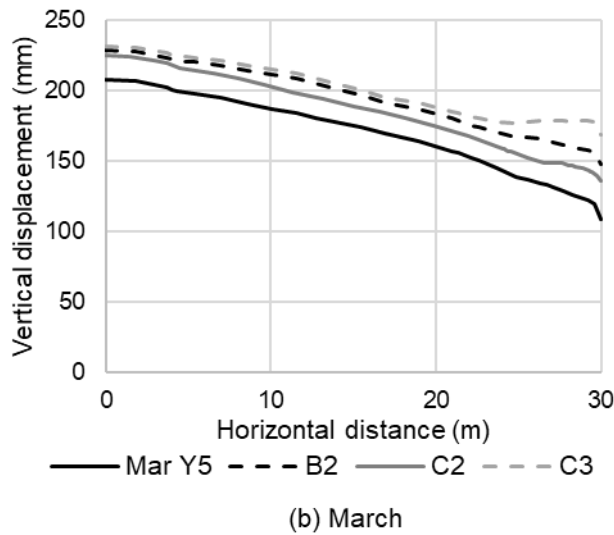
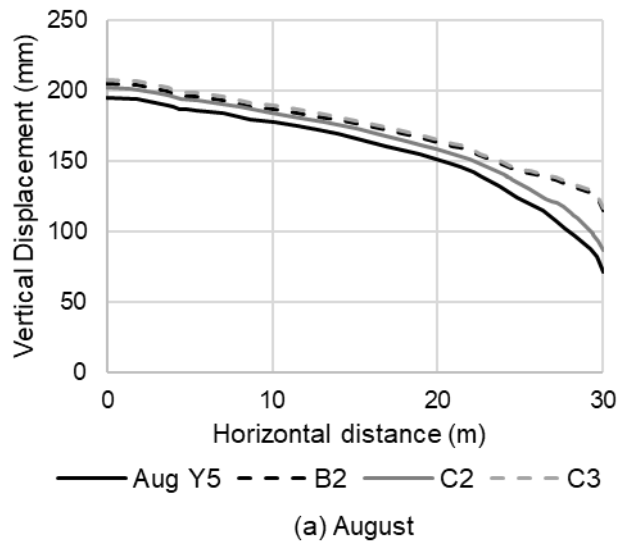
564

565 **Vegetation replacement**

566 Figure 15 illustrates the vertical displacements perpendicular to the asset axis at $y = 50\text{m}$ for B2
567 and C3, and at $y = 60\text{m}$ for C2. The August differential displacements have improved by similar
568 measures in B2 and C3, as also shown in Figure 13, with the displacement curves for the two
569 analyses showing little difference. The improvement was visibly smaller for C2. By the following
570 March, differences in the displacements for B2 and C3 became obvious close to the toe, with C3
571 demonstrating the highest swelling (and smallest differential displacement), owing to more HWD
572 vegetation overall having been replaced than in B2. The benefit, however, was small and
573 counterweighted by the reduced FoS and the increased associated cost of maintaining more
574 complex patterns of vegetation. Overall, the March serviceability was improved by comparable
575 measures in all three analyses.

576 In contrary to what was observed in B1, where in March serviceability was critical close to the toe,
577 in B2, which was the equivalent scenario to B1 but with vegetation replacement rather than
578 clearance, this was no longer the case. As a result, in March, serviceability was improved for B2
579 in relation to Year 5 (Figure 13). The serviceability of the slope improved more in C1 than in C2,
580 i.e., for the clearance rather than the replacement scenario, both in August and in March, although
581 scenario C1 in itself did not present an attractive solution anyway, as already discussed.

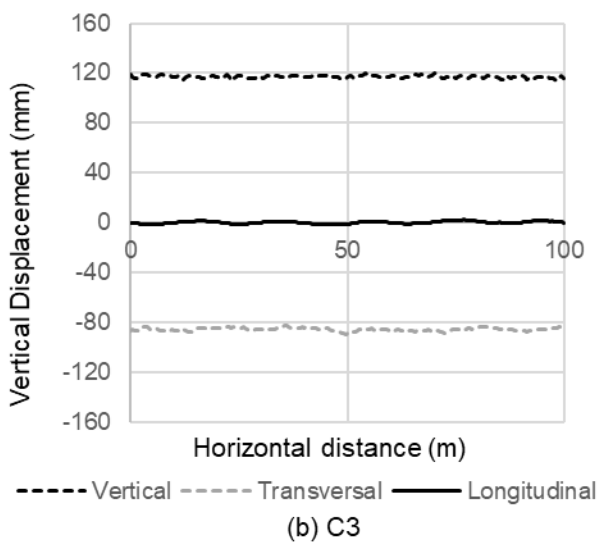
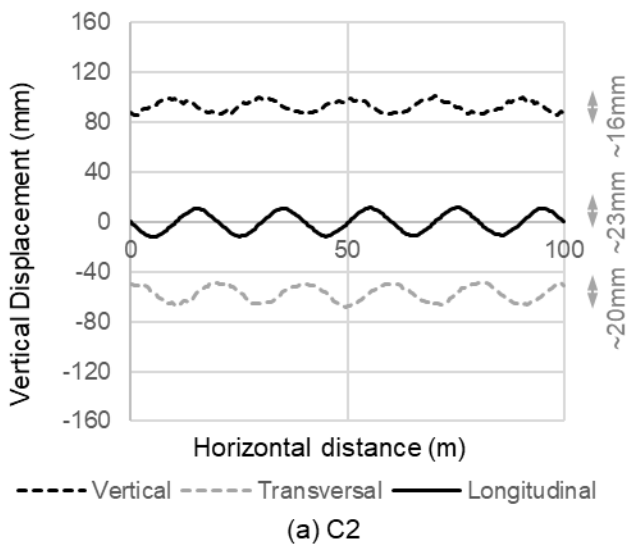
582 The transversal, longitudinal and vertical displacements along the toe are shown in Figure 16.
583 Differential displacements of magnitudes comparable to, but smaller than, C1 were obtained for
584 C2. Vegetation replacement seemed to cause smaller serviceability problems along the toe, as
585 the difference between net inflow/outflow, and therefore, pore water pressures, for HWD and LWD
586 vegetation, which alternate along the toe in C2, is smaller than for HWD vegetation and vegetation
587 clearance, which alternate along the toe in C1. Removing the HWD vegetation from the bottom
588 part of the slope in C3 prevented any differential displacements from developing, signifying that
589 conditions along the toe were not affected by the irregular vegetation pattern higher up the slope.



590
 591 Figure 15: Vertical displacements at the bottom of the excavation along a line perpendicular to
 592 the toe at $y = 50\text{m}$ for scenarios B2 and C2 and at $y = 60\text{m}$ for D2, for Year 6 in comparison with
 593 Year 5 (a) in August and (b) in March

594 As highlighted earlier, the displacements around the toe would be an outcome of suction reduction
 595 in combination with coupled mechanical effects, rendering it impossible to predict whether
 596 serviceability would improve or deteriorate with different vegetation management scenarios a-
 597 priori, based solely on intuition. From the analyses results presented here, it is evident that
 598 scenarios B2 and C3, that involve vegetation replacement at the toe, would yield the best all-
 599 around outcome for the slope, with serviceability improving both in August and in March and with

600 values of F_s of above or around 2 maintained. Perhaps scenario B2 is the most attractive,
 601 considering the lower maintenance it would require and the better outcome for slope stability.



602
 603 Figure 16: Vertical (z) and horizontal (x and y) displacements along the slope toe for scenarios
 604 (a) C2 and (b) D2
 605

606 **Conclusions**

607 The paper studied and compared the effects of vegetation clearance and vegetation replacement
608 on the stability and serviceability of a typical slope cut in London clay, considering various
609 vegetation management scenarios in 3D. Although focused on a geometry and climate
610 representative of SE England, the conclusions drawn from the study are universal, in that they
611 account for the changing balance of pore water pressures, strength and stiffness, which
612 qualitatively would be similar to many other cases and climates.

613 When considering vegetation management, the continuous presence of HWD vegetation in in-
614 plane cross-sections may prevent to a certain extent a dramatic loss of stability, even if continuity
615 is limited to the upper part of the slope. Maintaining some HWD vegetation on the slope is
616 generally beneficial for its stability, and with appropriate vegetation management serviceability
617 can be improved. Care should be taken that, while attempting to solve serviceability issues
618 perpendicular to the asset axis, vegetation management does not inadvertently induce new
619 serviceability issues along its axis.

620 Serviceability is not generally and universally improved by vegetation clearance. In certain cases,
621 clearance may lead to a worsening serviceability, as well as to worsening stability. In fact,
622 vegetation replacement, although potentially more expensive, may be preferable for both
623 reasons of stability and serviceability, as well as for enhancing bio-diversity.

624 From the scenarios considered here, it would seem that the preferred option may be to replace
625 HWD vegetation along the toe of the slope with LWD vegetation. The optimal extent of vegetation
626 replacement up the slope remains to be studied and this could be done in 2D.

627 It needs to be highlighted that it would not have been straightforward, and perhaps not possible,
628 to predict based solely on intuition which scenario would provide the best combined outcome for
629 the stability and the serviceability of the slope, post vegetation management. This is because
630 reduced shrinkage at the toe associated with a change of inflow/outflow rates, needs to be

631 considered concurrently with a potential reduction of stiffness and strength due to reducing
632 suctions and, therefore, effective stresses. The complex mechanisms taking place, render
633 numerical analysis a very useful and cost-effective tool which can be used to guide and inform
634 field and large-scale laboratory investigations, which are of course irreplaceable but also require
635 a lot more resources.

636 Further to the conclusions drawn directly from the study, the paper's contribution extends to
637 presenting a numerical methodology and a numerical model for 3D conditions which can form the
638 basis for further studies, such as the effect of irregular in the out-of-plane vegetation on
639 progressive failure, the progression of serviceability with time post-vegetation management,
640 modelling of isolated trees or group of trees on the slope and their management, to name a few.
641 Similar methodologies can be extended to study 3D vegetation effects on natural slopes,
642 embankment slopes, flood embankments and any other geotechnical structure that interacts with
643 the atmosphere.

644 Further analyses should ideally take into account the mechanical reinforcement of the soil due to
645 the presence of roots. This requires that a consistent and robust methodology is developed on
646 how to incorporate vegetation replacement and clearance in constitutive models.

647 Numerical analysis can provide preliminary, cost-effective information and guide large-scale
648 laboratory and field investigations, which require a lot more resources but are irreplaceable and
649 necessary. The paper provides clear numerical evidence for the first time of the importance of
650 considering vegetation management as a three-dimensional problem for stability as well as for
651 serviceability and can underpin a paradigm shift in laboratory and field investigations of vegetation
652 management on infrastructure slopes.

653

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- 789

790 **Tables**

791 Table 1: Model parameters for weathered and unweathered London clay

Strength parameters											
Angle of shearing resistance, φ'				Cohesion, c'				Angle of dilation, ν			
(degrees)				(kPa)				(degrees)			
23°				7.0				0.0			
Small strain stiffness parameters											
G_0	K_0	G_{min}	K_{min}	m_G	m_k	a_0	b	$R_{G,min}$	$R_{k,min}$	r_0	s
(kPa)	(kPa)	(kPa)	(kPa)	()	()	()	()	()	()	()	()
955	1665	2000	3000	0.7	0.7	1.81E-4	1.3	5E-2	7.9E-2	3E-4	1.1

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Table 2: Hydraulic parameters for weathered London clay

k_{sat}	S_{sat}	S_{res}	g_n	g_a	g_l
(m/s)	()	(kPa)	()	(1/m)	()
4.3E-8	1	0	1.5	0.15	0

797