Guiding the folding pathway of DNA origami.

Katherine E. Dunn^{*1,†}, Frits Dannenberg^{*1,2}, Thomas E. Ouldridge³, Marta Kwiatkowska²,
Andrew J. Turberfield¹ and Jonathan Bath¹

¹University of Oxford, Department of Physics, Clarendon Laboratory, Parks Road,
Oxford OX1 3PU, U.K.

²University of Oxford, Department of Computer Science, Wolfson Building, Parks Road,
Oxford OX1 3QD, U.K.

³University of Oxford, Department of Physics, Rudolf Peierls Centre for Theoretical Physics,
1 Keble Road, Oxford OX1 3NP, U.K.

[†]current address: Department of Electronics, University of York, York YO10 5DD, U. K.

*authors contributed equally to this work

DNA origami is a robust molecular assembly technique by which a single-stranded DNA template is folded by annealing it with hundreds of short ‘staple’ strands.¹⁻⁴ The guiding design principle of nanofabrication by DNA self-assembly is that the target structure is the single most stable configuration;⁵ however, the pathway and kinetics of origami assembly are poorly understood. The folding transition is cooperative^{4,6,7}, and there is a strong analogy with protein folding: both are governed by information encoded in polymer sequence.⁸⁻¹¹ Misfolded structures are kinetic traps. The yield of well-folded DNA origami can be low;² yield is improved by titration of cations^{2,12} or by following empirical design rules,^{12,13} but it is frequently necessary to separate well-folded origami from misfolded objects.^{2, 3, 14-16} Here, we present an origami structure that is designed to reveal the assembly process. Our system has the unusual property of having a small set of distinguishable, well-folded shapes that represent discrete and approximately degenerate energy minima in a vast folding landscape. We obtain a high yield of well-folded origami structures, demonstrating the existence of efficient folding pathways. The distribution of shapes provides information about individual trajectories through the folding landscape. We show that the assembly pathway can be steered by rational design and identify similarities to protein folding: assembly is highly cooperative; reversible bond-formation is important in recovering from transient misfoldings; and the early formation of long-range connections can be very effective in forcing particular folds. Expanding the rational design process to include the assembly pathway is the key to reproducible synthesis, which is essential if nucleic acid self-assembly is to continue its rapid development^{1-3,17-19} and become a reliable manufacturing technology.²⁰

This study is based on a simplified version of the archetypal origami tile¹ and, in particular, on the distribution of observed folds of a ‘dimer’ variant which contains two copies of the template sequence in head-to-tail repeat. The ‘monomer’ tile (Fig. 1) is created by annealing a 2646-nucleotide (nt) circular template with 90 staples, each designed to hybridize to one or more 15- or 16-base domains of the template. 76 of the staples mediate interactions between pairs of non-contiguous template domains: 66 U-shaped ‘body’ staples form short-range contacts between domains that are relatively close in the primary sequence of the template; 5 pairs of ‘seam’ staples form long-range contacts, bridging between positions where the template folds back on itself to form a central seam.¹ Unlike the interactions between amino acid residues that stabilize a protein, staples mediate interactions between template domains that are highly specific: each staple can be considered to bind stably only to complementary domains of the template. The designed fold of the monomer tile corresponds to an absolute minimum in the free energy landscape. This origami folds with high yield to form discrete rectangular tiles of approximately 80 nm × 40 nm (Fig. 1c); approximately 80% of tiles appear to be well folded.

The ‘dimer’ template is also circular. It contains two identical copies of the monomer joined head-to-tail and can therefore bind two copies of each staple (Fig. 2). Each pair of body and seam staples can bind in one of two configurations (Fig. 2a) to form either an internal link within each copy of the monomer sequence or a pair of cross-links between the two copies. The total number of possible domain pairings is $2^{76} \approx 10^{23}$. Although many of these configurations are sterically inaccessible it is clear that the result of reducing the specificity of staple binding is that, as in the case of protein folding, the number of possible states of the system is overwhelmingly greater than the number of well-folded structures. However, in contrast to proteins (and to conventional origami structures) there is more than one ‘well-folded’ state (Fig. 2): not one but a handful of well-folded states occupy discrete energy

minima in a vast configurational landscape. Remarkably, when the dimer origami is annealed by cooling from 95°C, a small set of well-folded shapes are formed with good yield: each consists of a pair of rectangular tiles attached on one edge (Fig. 2b,c). The probability of finding well-folded structures by random search of configuration space is negligible,⁸ therefore efficient folding pathways must exist.^{21,22} As in protein folding, assembly is constrained such that the system is highly likely to discover free-energy minima that correspond to well-formed final states.

The dimer origami tile has 22 template routings that correspond to well-folded configurations in which all staple binding sites are occupied and in which the tile is expected to be planar and unstrained. These give 6 unique shapes, each with a characteristic offset between two linked rectangular components, each of which has essentially the same structure as the monomer tile (Fig. 3a-c, Extended Data Fig. 1). These shapes can be grouped into classes according to the contacts made by the seam staples: fold $m:n$ has m pairs of seam staples that connect domains *within* each half of the template and n pairs of seam staples that form connections between domains in opposite halves (Fig. 3a-c). Folds $m:n$ and $n:m$ have the same shape and are therefore not distinguished in our experiments (Extended Data Fig. 1b). A set of non-planar folds adds a seventh shape to the six defined above and a further 52 template routings (Fig. 3e and Extended Data Fig. 2). Fink and Ball²³ have estimated the maximum number of distinct, compact configurations that can be encoded into a single polymer sequence: for a polymer of 168 unique domain types on a square lattice^{23,24} the theoretical limit is 13. A major factor in allowing the large number of folds in our system is the extensive re-use of structural motifs within distinct folds, a possibility not considered by Fink and Ball.

Atomic force microscopy (AFM) enables us to distinguish different configurations of the template and this provides a unique opportunity to study folding pathways. Samples of annealed origami were imaged by AFM. Most observed shapes are consistent with the classification scheme shown in Fig. 3, and the outlines of 44% of objects identified as candidate dimer tiles were successfully fitted to measure the offset between the two component monomer tiles (Fig. 3d, Extended Data Fig. 3).

The distribution of tile shapes was compared to predictions made using a Markov chain model of folding in which each transition corresponds to binding or unbinding of a single staple domain (Methods). An unbound staple at concentration c binds to the template with a rate k_+c (where $k_+ = 10^6 \text{ M}^{-1}\text{s}^{-1}$, ref. 25). After one half of a staple has bound, the second half can bind with a rate (k_+c_{eff}) that depends on its effective concentration, c_{eff} , at the corresponding template domain. The effective concentration depends on the proximity of the template domain which, in turn, depends on the contacts between template domains already established by hybridization of other staples. We expect folding to be dominated by short-range interactions because staples are more likely to connect two template domains that are spatially close, either because they are closely spaced along the template or because the previous binding of other staples is holding them together. To determine the effective concentration, the shortest path through the part-assembled origami that connects the complementary template and staple domains is identified. This connection is modelled as a heterogeneous freely jointed chain with double-stranded (ds) and single-stranded (ss) DNA components. The effective concentration of the part-bound staple at the complementary template domain is related to the probability that the ends of the chain lie spontaneously within a (short) interaction range. Unbinding of a staple domain is treated as a two-state transition, with a configuration-independent rate: $k_- = k_+ \exp\{-\Delta G^{0,\text{duplex}}/RT\}(1 \text{ M})$ where $\Delta G^{0,\text{duplex}}$ is the change in standard free energy on dissociating the duplex. In order to

represent steric constraints on folding, the state space of the model is restricted to patterns of staple binding in which each segment of the partially folded origami occurs in one of a set of pre-defined, well-ordered folds.

The histograms in Fig. 4 show distributions of offset values, measured by fitting AFM data (Extended Data Figs 3, 4), and corresponding distributions predicted by the model between the discrete shapes shown in Fig. 3. Fig. 4a corresponds to the staple set described above (cf. Fig. 21): structures with each of the seam configurations 5:0, 4:1 and 3:2 are observed. The model suggests that the folding pathway depends on competition between body and seam staples. If local interactions mediated by body staples were to form first and dominate the outcome, the system would prefer the 5:0 fold in which all body staples are bound to two domains that are as close as possible along the template. In this fold, no staples link the two halves of the template. However, strong seams favour a more uniform distribution between all possible seam configurations: for example, once the part-folded structure 1:1 has formed, the 5:0 fold is inaccessible unless at least one seam connection is broken (Extended Data Fig. 5). With this staple set, each seam is bridged by two staples. The cooperative binding of seam staple pairs offsets the increased entropic cost of forming long-range contacts, with the result that seam staples are incorporated at a similar temperature to body staples in both model (Fig. 4a) and experiment (Extended Data Fig. 6). Consequently the model predicts that all seam configurations should be observed, consistent with experimental observations.

We predict that the folding pathway can be changed by altering the relative strengths of short- and long-range interactions. Breaking in half one of each pair of seam staples (Fig. 4b), so that the pairs no longer bind cooperatively, weakens these long-range bonds, causing them to form later in the folding pathway (Fig. 4b, central panel and Extended Data Fig. 6) and to break and reform in alternative configurations more frequently (Extended Data Fig. 7). With

weakened long-range interactions, we expect folding to be governed primarily by local interactions. The model predicts that the distribution of shapes is shifted strongly towards the 5:0i fold, in which all body staples span the smallest possible distances along the template (the same distances as in the monomer tile) and this is confirmed by experiment (Fig. 4b). Breaking every other seam staple has approximately the same effect on the stability of each well-folded states and therefore no effect on the equilibrium distribution: we have changed the distribution between folds not by changing the relative stability of the final states but by deliberately controlling the stabilities of crucial intermediate states, thus shaping the folding pathway.

The importance of stable, long-range interactions in determining the folding pathway is revealed by the evolving correlations between seam staples in the model. Characteristic patterns of correlation can be used to predict the final fold even before seam staple occupancy has reached 50% (Extended Data Fig. 8).

The influence of seam staples on folding is similar to that of disulphide bonds in Anfinsen's experiment on protein folding.⁹ If long-range bonds are allowed to form first and, effectively, irreversibly then folding is kinetically trapped. If they are weakened and permitted to rearrange then folding can be controlled by weaker short-range interactions.

Fig. 4c shows an alternative staple set incorporating extended staples that form particularly strong short-range connections and therefore bind stably to the template early in the folding process (Fig. 4c, central panel). Without interference from other staples, these contacts are most likely to form between the pairs of template domains with the smallest separation along the template. These preferred contacts occur in the 3:2 and 5:0 folds but not the 4:1 fold, in which one extended staple bridges forms a long-range contact between the two halves of the template. Experimental results confirm the model prediction that the 4:1 fold is strongly

Formatted: Not Highlight

suppressed (Fig. 4c). As with the broken seam staples, this modification guides the folding pathway without imposing an energetic penalty on alternative folds.

We can control the fold of the dimer very effectively by engineering *both* the folding pathway *and* the stability of the chosen target structure. The 3:2 configuration can be favoured by weakening the original seams (as in Fig. 4b) and adding new seam staples that can only bridge between the monomer tiles without distortion in the 3:2 configuration (Fig. 4d). This modification guides folding by increasing the stability of 3:2 relative to other folds. Similarly, a long staple in the bottom right corner of the monomer tile (Fig. 4e) biases folding towards the 5:0iv shape by decreasing the stability of other folds, which would require introduction of a sharp bend within the long staple. (The model does not include any penalty for bending and so fails to predict the engineered bias in this case.)

We have shown that an origami tile with a duplicated template can be annealed to produce a high yield of well-folded structures from among $\sim 10^{23}$ disordered alternative staple configurations: this demonstrates that, as in the case of proteins, efficient folding pathways exist and that folding is highly cooperative. Folding of our dimer template is more prone to kinetic traps than a conventional origami in which each staple has a unique location in the final folded structure: we infer that all origamis follow efficient folding pathways. Our dimer tile has multiple near-degenerate well-folded states, allowing us to discriminate between different folding pathways by inspection of the final folded forms. We show that by changing the relative strengths of local and long-range staple interactions the folding pathway can be steered by design. Manipulation of the folding pathway validates a simple folding model that successfully predicts the dominant folding pathways observed in experiments. We anticipate that our folding model could be used to improve the yield of origami structures that fold

poorly, and that these results will help to sustain the rapid development of DNA nanotechnology by expanding the design rules to include folding pathways.

References

1. Rothemund, P. K. W. Folding DNA to create nanoscale shapes and patterns. *Nature* **440**, 297-302 (2006)
2. Douglas, S. M. *et al.* Self-assembly of DNA into nanoscale three-dimensional shapes. *Nature* **459**, 414-418 (2009)
3. Dietz, H., Douglas, S. M. and Shih, W. M. Folding DNA into twisted and curved nanoscale shapes. *Science* **325**, 725-730 (2009)
4. Sobczak, J. P. J., Martin, T. G., Gerling, T. and Dietz, H. Rapid folding of DNA into nanoscale shapes at constant temperature. *Science* **338**, 1458-1461 (2012)
5. Seeman, N. C. DNA in a material world. *Nature* **421**, 427-431 (2003)
6. Arbona, J.-M., Aimé, J.-P. and Elezgaray, J. Cooperativity in the annealing of DNA origamis. *J. Chem. Phys.* **138**, 015105 (2013)
7. Song, J. *et al.* Direct visualization of transient thermal response of a DNA origami. *J. Am. Chem. Soc.* **134**, 9844-9847 (2012)
8. Levinthal, C. Mössbauer Spectroscopy in Biological Systems Proceedings, Univ. of Illinois Bulletin **67**, 22-24 (1969)
9. Anfinsen C. B. Principles that govern the folding of protein chains. *Science* **181**, 223-230 (1973)
10. Dobson, C. M. Protein folding and misfolding. *Nature* **426** 884-890 (2003)
11. Baker, D. A surprising simplicity to protein folding. *Nature* **405**, 39-42 (2000)

12. Martin, T. G. and Dietz, H. Magnesium-free self-assembly of multi-layer DNA objects. *Nature Communications* **3**, 1103 (2012)
13. Ke, Y., Bellot, G., Voigt, N. V., Fradkov, E. and Shih, W. M. Two design strategies for enhancement of multilayer-DNA-origami folding: underwinding for specific intercalator rescue and staple-break positioning. *Chem. Sci.* **3**, 2587-2597 (2012)
14. Castro C. E. *et al.* A primer to scaffolded DNA origami. *Nature Methods* **8**, 221-229 (2011)
15. Douglas, S. M., Bachalet, I. and Church, G. M. A logic-gated nanorobot for targeted transport of molecular payloads. *Science* **335**, 831-834 (2011)
16. Perault S. D. and Shih, W. M. Virus-inspired membrane encapsulation of DNA nanostructures to achieve *in vivo* stability. *ACS Nano* **8**, 5132-5140 (2014)
17. Han, D. *et al.* DNA gridiron nanostructures based on four-arm junctions. *Science* **339**, 1412-1415 (2013)
18. Ke, Y., Ong, L. L., Shih, W. M. and Yin, P. Three-dimensional structures self-assembled from DNA bricks. *Science* **338**, 1177-1183 (2012)
19. He, Y. *et al.* Hierarchical self-assembly of DNA into symmetric supramolecular polyhedra. *Nature* **452**, 198-201 (2008)
20. Kershner, R. J. *et al.* Placement and orientation of individual DNA shapes on lithographically patterned surfaces. *Nature Nanotechnology* **4**, 557-561 (2009)
21. Wolynes, P. G., Onuchic, J. N. and Thirumalai, D. Navigating the folding routes. *Science* **267**, 1619-1620 (1995)

22. Onuchic, J. N., Wolynes, P. G., Lutheyschulten, Z. and Socci, N. D. Towards an outline of the topography of a realistic protein-folding funnel. *Proc. Natl. Acad. Sci. U.S.A.* **92**, 3626-3630 (1995)
23. Fink, T. M. A. and Ball R.C. How many conformations can a protein remember? *Phys. Rev. Lett.* **87**, 198103 (2001)
24. Jacobsen, J. L. and Kondev, J. Field theory of compact polymers on a square lattice. *Nucl. Phys. B* **532**, 635-688 (1998)
25. Zhang, D. Y. and Winfree, E. Control of DNA strand displacement kinetics using toehold exchange. *J. Am. Chem. Soc.* **131**, 17303-17314 (2009)

Supplementary Information is linked to the online version of the paper at www.nature.com/nature.

Acknowledgements

The authors thank Prof. K.V. Gothelf, Prof. Mingdong Dong, Anne Louise Bank Kodal, Sarah Helmig and Shuai Zhang (Department of Chemistry and Interdisciplinary Nanoscience Centre iNano, Aarhus, Denmark) for assistance with AFM imaging. This research was supported by Engineering and Physical Sciences Research Council grants EP/G037930/1, EP/P504287/1, a Human Frontier Science Program grant RGP0030/2013, a Microsoft Research PhD Scholarship (FD), the ERC Advanced Grant VERIWARE (MK) and a Royal Society–Wolfson Research Merit Award (AJT).

Author contributions

KED performed the experimental work, FD and TEO developed the folding model, JB and AJT devised the experimental strategy. All authors contributed to experimental design, interpretation of the data and preparation of the manuscript.

Competing financial interests

The authors declare no competing financial interests.

Corresponding author

Correspondence to: Jonathan Bath (j.bath@physics.ox.ac.uk) and Andrew Turberfield (a.turberfield@physics.ox.ac.uk).

Figure 1. The monomer tile. **a** 66 body staples (blue) and 5 pairs of seam staples (brown) each hybridize to two non-contiguous domains of the circular template. Edge staples (grey) fill gaps at the top and bottom of the structure. Hybridization of body and seam staples pins the corresponding domains of the template together and determines the unique stable, rectangular fold of this simplified origami tile, as indicated in **b**. **c** Atomic force micrograph of the monomer tile (scale bar 50 nm).

Figure 2. Folding origami tiles with a dimer template. **a** The base sequence of the green section of the template is the same as that of the pink section, so the dimer template can fully hybridize to two copies of each staple. Two identical staples can bind to the template in one of two configurations, binding together pairs of domains within each monomer or connecting domains in different monomers. This gives a vast number of possible configurations, a handful of which are well folded (defined in Fig. 3 and Extended Data Figs 1, 2). Ordered folds of the dimer template comprise two linked rectangular tiles with a characteristic offset on the long or short edges, e.g. **(b)**, **(c)** respectively. Scale bar 50 nm.

Figure 3. Classification of well-folded shapes. **a, b, c** Folds of the dimer origami tile can be classified by the pattern of interactions mediated by the seam staples: these contacts are shown schematically in diagrams in which the dimer template is represented as a circle. Fold $m:n$ has m seam contacts between domains *within* each copy of the monomer sequence and n seam contacts that form connections *between* the two copies (i.e. connecting template domains of different colour). The fold 5:0 can be further divided into shapes that differ in the offset along the long edge of the two tiles (**c**). **d** Tiles observed in folding experiments can be classified according to the fractional offset along the short or long edge of the tile (w/W and l/L respectively). **e** The set of legal folds allowed by the model includes well-folded configurations **a-c** and an additional set of non-planar configurations, one of which is shown (see Extended Data Fig. 2 for the complete set). **f** Seven unique shapes corresponding to well-folded configurations. **g** Gallery of shapes observed in a typical experiment with measured fractional offsets.

Commented [AJT1]: there is an asterisk by $l/L=1/7$ labelling the first shape - this is not used / explained

Figure 4. Folding can be guided by modifying staples to steer the folding pathway.

The reference staple set (**a**) folds to give a distribution of shapes that are characterized by the fractional offset between the two component tiles along the long or short edge. Modifications to the reference staple set were designed to fold into specific target shapes (**b-e**, left-hand panel). The top/left of each target shape is used to highlight modified staples in bold. In the bottom/right rectangle, staples are grouped and coloured according to the distance between the two template domains that the staple links (body staples are blue, seam staples are brown to yellow; lighter shades indicate larger distances). Graphs in the central panels show the calculated fraction of contacts formed for each staple group as a function of temperature during assembly (i.e., on cooling). The right hand panels show the distribution of shapes predicted and observed for each set: a histogram representing the continuous distribution of fitted offset values is plotted above the distribution of discrete shapes predicted by the model. The number of fitted shapes, N , and the yield (fitted shapes as a percentage of candidate structures identified) are shown in the top left corner of each histogram.

Commented [AJT2]: schematic for fig 4a?? (note to self!)

Methods

Experimental Methods

Plasmid pUC19 cut with HindIII and EcoRI was amplified by PCR with the primers

TGACCTAATCCTCAGCAATTCACCTGGCCGTCGTTTACAA and

ACGGACGCGCTGAGGAGCTTGGCGTAATCATGGTCATAG in order to trim the template to the desired length and introduce a unique BbvCI site. The PCR product was cut with BbvCI and ligated to generate pKD1 (2646 bp). A typical monomer plasmid preparation contains a small amount (~1%) of plasmid dimer. The dimer plasmid was obtained by nicking a monomer plasmid preparation with Nt.BbvCI (in order to resolve monomer and dimer more easily), purifying the nicked dimer band from a 0.7% TAE agarose gel, then transforming the purified nicked dimer into the *recA* host DH5 α . The template sequence is given in the Supporting Information.

Single-stranded template was prepared by sequential reaction of either monomer or dimer pKD1 with Nt.BspQI at 50°C and ExoIII at 37°C to digest the non-template strand and leave a covalently-closed single-stranded template.²⁶ Enzymes were removed by phenol:chloroform extraction and the template was recovered by ethanol precipitation; its concentration was then determined by measuring UV absorbance at 260 nm.

DNA origami was designed using caDNAno²⁷ and was assembled by cooling template at 4-10 nM with a ~10-fold excess of staples from 95°C to 25°C at 1°C per minute in a buffer containing 40 mM Tris-acetate (pH8.3) and 12.5 mM magnesium acetate. Excess staples were removed using an S-300 size exclusion spin column.²⁸ Staple sequences for the standard design and variations are given in the Supporting Information.

Commented [AJT3]: correct?

Atomic force microscopy images were acquired using either an Agilent 5500 AFM with Olympus TR400-PSA probes (Fig. 1, 2, 3 and 4a) or a Veeco Dimension 3100 with Bruker SNL-10 probes (all other figures). A few microlitres of sample were added to freshly cleaved mica and the sample was imaged in tapping mode in an imaging buffer containing 12.5 mM magnesium acetate, 4 mM NiCl_2 , 1 mM EDTA and 40 mM Tris-acetate pH8.0-8.3 (the imaging buffer for Fig. 1c lacked NiCl_2 , the imaging buffer for Fig. 2c lacked EDTA).

Folding model.

Our domain-level description of origami assembly is intended to reproduce some aspects of cooperativity. In particular, it accounts for the increase in incorporation rate for a staple when its target domains on the template are held more closely together as a result of the earlier binding of other staples. This effect is most noticeable in the seam where the binding of the first of a pair of seam staples greatly accelerates, and is stabilized by, the binding of the second. The model incorporates a physically reasonable approximation of the entropic cost of closing loops by staple binding, but is far from a complete description of the physics of assembly. It is useful in guiding, and providing insights into, the effects of significant changes to the origami design.

We model the folding of an isolated template in the presence of an excess of staples as an inhomogeneous continuous-time Markov chain. Each transition between states corresponds to the binding or unbinding of a single staple domain. Transition rates between two states are chosen according to an estimate of the free energy difference between the two, in a manner that would reproduce the correct Boltzmann distribution if this free energy difference were calculated exactly. The temperature is updated once per second of simulated time which allows us to use an event-based Gillespie simulation algorithm²⁹ with transition rates fixed over one second intervals. Data on folding processes is collected by simulating multiple

folding trajectories (typically 1600 per experiment).

State Space.

We consider the possible configurations of staples hybridized to the template with domain-level resolution: a domain is either fully hybridized or unhybridized. A staple is called half-bound if only one of its two domains is hybridized to the template and fully bound if both domains are bound. In the model, a staple domain can only hybridize to the complementary template domain; we ignore weaker interactions that result from inevitable partial sequence complementarity between other pairs of domains.

For each type of two-domain staple (and the corresponding two pairs of complementary template domains) there are 34 distinct patterns of domain binding (states) with between zero and four copies of the staple bound to the dimer template. One is an empty state. When one staple is bound to the template there are four states in which the staple is half-bound and four states in which the staple is fully bound. When two staples are bound to the template there are six states in which both staples are half-bound, eight states with one half-bound and one fully bound staple, and two states with two fully bound staples. There are four states with three half-bound staples and another four states with one fully bound and two half-bound staples. Finally there is the possibility that four half-bound staples are attached to the template. For a single-domain staple and the associated pair of template domains there are just four states. There are therefore $34^x \times 4^y$ states of the dimer template with staples, including part-folded states, where x is the number of two-domain staples and y is the number of single-domain staples. Of these, 2^x states consist exclusively of fully-bound staples. Formally, the state space S is given by $p_0 \times p_1 \times \dots \times p_{k-1}$ where p_i denotes the set of possible states for staple i as described above and k is the total number of staples.

Exclusion algorithm.

Two template domains hybridized to a single two-domain staple are held within a few tenths of a nanometre of each other at the staple crossover: many of the folds in S cannot meet this constraint. We provide an algorithm that provides an approximate representation of steric constraints, preventing the model from accessing unrealistic states. This method provides an approximation to the real steric constraints: it does not guarantee that each legal state satisfies the constraints or that all states that satisfy the steric constraints are legal.

We define a connected segment of an origami as a set of hybridized domains such that each domain can be reached from each other domain without leaving the set. Two template domains hybridized to the same staple are defined to be connected, as are two adjacent template domains hybridized to different staples. A partially folded segment of origami is considered stress-free (is legal) when it occurs in one of the set of well-ordered, two-dimensional folds shown in Extended Data Figs 1 or 2. These pre-defined folds satisfy the constraints imposed by finite staple length and steric exclusion.

More formally, we can represent the physical origami in partially folded state $s \in S$ as an abstract graph $G(s) = (V, E)$ such that each boundary between adjacent domains is a vertex $v \in V$ and each template domain and staple crossover is an edge $e \in E$ between the appropriate vertices. Each edge has an intrinsic number of nucleotides and a labelling function $f: E \rightarrow \{\text{single-stranded, double-stranded, crossover}\}$ that assigns an appropriate status. We can draw subgraphs consisting of connected hybridized segments of the graph: for the origami to be in a legal (stress free) state, each of these subgraphs must be present in a single well-ordered fold from the set shown in Extended Data Figs 1 and 2.

Misfolds occur in the model when at least two connected segments would be incapable of satisfying the constraints were they to become connected to each other. At that point, folding cannot advance unless one of the segments unfolds, allowing another to expand. Extended

Commented [AJT4]: is number of nucleotides relevant?

Data Fig. 3c shows a misfolded dimer that has three connected parts that cannot be joined to form a stress-free state. When simulating assembly using the staple set corresponding to Fig. 4a, about half of the simulations end in a misfolded state; for the weakened-seam variant (Fig. 4b) there are only ~1% misfolds.

Rates Model.

We develop a kinetic model of folding based on standard reaction models for hybridization and a method to estimate the effective local concentration of the unhybridized domain of a half-bound staple at its complementary template domain.

Consider complementary strands A and B that can bind reversibly to form duplex AB . Under the assumptions of mass action kinetics, the concentration $[AB]$ is described by

$$\frac{d[AB]}{dt} = k_+[A][B] - k_-[AB] \quad (1)$$

for rate constants k_+ and k_- . The rate constants are constrained by the requirement that the equilibrium concentrations $\{A\}$, $\{B\}$ and $\{AB\}$ are consistent with $\Delta G_{AB}^{0,\text{duplex}}(T)$, the standard change in Gibbs free energy on duplex formation:

$$\frac{\{AB\}}{\{A\}\{B\}} = k_+/k_- = \exp\left(\frac{-\Delta G_{AB}^{0,\text{duplex}}}{RT}\right) \times \text{M}^{-1}, \quad (2)$$

where R denotes the molar gas constant and T temperature.

For staples within a partially folded origami, binding and unbinding rates are similarly constrained by the difference in free energy between states. We approximate the difference in free energy between partially folded states s, s' that differ by the hybridization of a single template domain as

$$\Delta G_{s,s'}^0 = \Delta G_{s,s'}^{0,\text{duplex}} + \Delta G_{s,s'}^{\text{shape}} \quad (3)$$

where $\Delta G_{s,s'}^{0,\text{duplex}}$ is the standard free energy change corresponding to the formation or dissociation of an equivalent isolated duplex and $\Delta G_{s,s'}^{\text{shape}}$ represents the change in entropy corresponding to the geometric constraints on the template that arise when two-domain staples connect non-contiguous template domains ('looping constraints').^{10,27,28} ΔG^{shape} quantifies cooperative effects: when a single staple domain binds or unbinds, ΔG^{shape} depends on the pattern of binding of *other* staples.

Consider a single, isolated origami in partially folded state s_{00} and let staple p bind to the template by a single domain, resulting in state s_{01} . The rate for this reaction is taken to be equal to that for duplex formation between isolated strands:

$$R(s_{00}, s_{01}) = k_+[p], \quad (4)$$

where $R(s, s')$ is the rate of transition from state s to s' . The unbinding rate is then determined by a thermodynamic constraint analogous to Equation 1:

$$\begin{aligned} R(s_{01}, s_{00}) &= k_+ \exp\left(\frac{\Delta G_{s_{00}, s_{01}}^0}{RT}\right) \times M \\ &= k_+ \exp\left(\frac{\Delta G_{s_{00}, s_{01}}^{0, \text{duplex}}}{RT}\right) \times M. \end{aligned} \tag{5}$$

We have set $\Delta G_{s_{00}, s_{01}}^{\text{shape}} = 0$ because transitions $s_{01} \leftrightarrow s_{00}$ do not create or destroy loops in the template. (We do not take into account other ways in which hybridization of a single staple domain affects the free energy of the partly-folded origami, e.g., by changing the mechanical properties and thus the free-energy cost of any pre-existing loop of which it forms part.) For the second domain of the staple, once the first domain is bound, we again fix the unbinding rate to be that of the corresponding isolated duplex. This rate does not depend on the change in entropy that results from the removal of a looping constraint^{30,31} because, immediately after unbinding, the conformation of the template is unchanged:

$$R(s_{11}, s_{01}) = k_+ \exp\left(\frac{\Delta G_{s_{01}, s_{11}}^{0, \text{duplex}}}{RT}\right) \times M \quad (6)$$

where s_{11} denotes the state in which the staple is bound to the template with both domains. The binding rates of the second domain of the staple, once the first domain is bound, can then be found from the thermodynamic constraint

$$\begin{aligned} R(s_{01}, s_{11}) &= R(s_{11}, s_{01}) \exp\left(\frac{-\Delta G_{s_{01}, s_{11}}}{RT}\right) \\ &= k_+ \exp\left(\frac{\Delta G_{s_{01}, s_{11}}^{0, \text{duplex}} - \Delta G_{s_{01}, s_{11}}}{RT}\right) \times M \\ &= k_+ \exp\left(\frac{-\Delta G_{s_{01}, s_{11}}^{\text{shape}}}{RT}\right) \times M. \end{aligned} \quad (7)$$

The free energy penalty $\Delta G_{s, s'}^{\text{shape}}$, that corresponds to the additional geometric constraints associated with the binding of the second staple domain, thus determines the binding rate for the second domain.

Looping constraints.

We approximate $\Delta G_{s_{01}, s_{11}}^{\text{shape}} = \Delta G_{s_{01}, s_{11}}^{\text{loop}}$, where $\Delta G_{s_{01}, s_{11}}^{\text{loop}}$ corresponds to the entropic penalty of closing the new loop that forms in the template when the second domain of a staple binds.

For other transitions, no loop forms and we take $\Delta G^{\text{shape}}=0$. ΔG^{loop} quantifies the difference between the entropic penalties for pinning the template into a loop so that the second staple and template domains can bind and for bringing together two domains unconnected by a loop in a hypothetical ideal system at standard conditions (1M concentration).³⁷ ΔG^{loop} is thus related to the ratio between the probabilities of bringing two domains into contact in the looped system and in the ideal unconnected system:

$$\Delta G^{\text{loop}} = RT \ln \left(P_{v^\phi}^{r_0} / P_{\text{loop}}^{r_0} \right). \quad (8)$$

Here, $P_{\text{loop}}^{r_0}$ is the probability that the origami adopts a confirmation in which the unbound staple arm and the template domain are spontaneously within an interaction radius r_0 of each other, where r_0 is an unspecified small distance necessary for closure of the loop. $P_{v^\phi}^{r_0}$ is the probability that two unconnected molecules would be within r_0 in a hypothetical ideal system of $v^\phi = 1/N_A$ litres, N_A being Avogadro's number. The rate of hybridization of a second staple domain is therefore given by

$$\begin{aligned} R(s_{01}, s_{11}) &= k_+ \left(\frac{P_{\text{loop}}^{r_0}}{P_{v^\phi}^{r_0}} \right) \times M \\ &= k_+ \left(\frac{P_{\text{loop}}^{r_0}}{\frac{4}{3} \pi r_0^3 N_A} \right) \times M \end{aligned} \quad (9)$$

so $\left(\frac{P_{\text{loop}}^{r_0}}{\frac{4}{3} \pi r_0^3 N_A} \right) \times M$ denotes the effective concentration of the opposing domain.

As a first approximation we treat the loop of DNA as a freely-jointed chain comprising two types of link, double-stranded DNA and single-stranded DNA (dsDNA and ssDNA respectively). Let $P(R)$ be the probability density for the end-to-end extension of the chain R . Then $P_{\text{loop}}^{r_0} = \int_0^{r_0} P(R) dR$ is the probability that the two domains are separated by at most r_0 .

The end-to-end distance distribution $P(R)$ of a freely-jointed chain, in the limit of a large number of segments, is

$$P(R) = 4\pi R^2 \left(\frac{3}{2\pi E[R^2]} \right)^{3/2} \exp\left(\frac{-3R^2}{2E[R^2]} \right) \quad (10)$$

where $E[R^2]$ is the mean squared distance between the two ends. The result for a single segment type is a classic result of statistical physics.^{38,39} The following argument shows that the result also holds for a chain with heterogeneous segments. From the central limit theorem, for a large number of segments we expect a Gaussian distribution over the X, Y and Z components of R. Equation 10 is the only Gaussian distribution that also satisfies the symmetry conditions $E[X] = E[Y] = E[Z] = 0$, and $E[XY] = E[XZ] = E[YZ] = 0$.

The internal association rate is therefore given by:

$$\begin{aligned} R(s_{01}, s_{11}) &= k_+ \frac{\int_0^{r_0} 4\pi R^2 \left(\frac{3}{2\pi E[R^2]} \right)^{3/2} \exp\left(\frac{-3R^2}{2E[R^2]} \right) dR}{\frac{4}{3}\pi r_0^3 N_A} \times M \\ &\approx k_+ \frac{\int_0^{r_0} 4\pi R^2 \left(\frac{3}{2\pi E[R^2]} \right)^{3/2} dR}{\frac{4}{3}\pi r_0^3 N_A} \times M \\ &\approx \frac{k_+}{N_A} \left(\frac{3}{2\pi E[R^2]} \right)^{3/2} \times M. \end{aligned} \quad (11)$$

where we have assumed $r_0 \ll E[R^2]$ in the second step.

The loop that is closed by the insertion of a staple into a part-folded origami has, in general, a complex structure comprising multiply connected domains of single- and double-stranded DNA. We approximate this loop by a single path through the origami, the loop with the smallest expected square end-to-end distance $E[R^2]$. This path represents the most important

constraint that leads to the enhancement of the effective local concentration of one end of the loop at the other, and thus provides the most significant enhancement of $R(s_{01}, s_{11})$. In order to identify the dominant loop, each edge $e \in E$ in the implied graph $G(s) = (V, E)$ of the partially folded origami is assigned a weight equal to the contribution to $E[R^2]$ in the freely jointed chain approximation. Dijkstra's shortest path algorithm⁴⁰ is used to determine a loop that minimizes $E[R^2]$ and hence determines $R(s_{01}, s_{11})$.

For the seam staples, which are paired, the loop closed by hybridization of the second staple is particularly small: it consists only of the crossover link. The predictions of the model remain physically sensible: a second staple binding to a seam has an overall ΔG which is ~ 4.4 kcal/mol less favourable (at $T=60^\circ\text{C}$) than a continuous duplex. This destabilization is equal to that expected from a 5-nt bulge within a duplex.³⁰ We note that for the broken seam variant, the model predicts incorporation temperatures for the unbroken staple that are lower than the regular case by 2°C , compared to 2.2°C measured in experiment (Extended Data Fig. 6). It is therefore clear that we do not overestimate the cooperative stabilisation of seam staples.

The approximations made in estimating the change in free energy when a staple domain binds or unbinds are not thermodynamically self-consistent: the value assigned to the difference in free energy between states depends, in general, on the path taken between them. Models of this kind will be presented in a companion paper, in which they are compared to thermodynamically self-consistent approaches for simpler systems (F. Dannenberg, T. E. Ouldridge, K. Dunn, J. Bath, M. Kwiatkowska, and Andrew J. Turberfield, to be published).

Parameterization of the Model

Compared to unbinding rates, the rate of binding of an isolated duplex is known to be weakly dependent on duplex stability.³² We assume k_+ to be independent of temperature, domain sequence, and folding state, and we set $k_+ = 10^6 \text{M}^{-1} \text{s}^{-1}$.^{25,32,33}

The free energy change when each domain binds to its complement, $\Delta G^{0,\text{duplex}}$, is taken to be that of a 16-bp DNA duplex averaged over all possible sequences.³⁴ Buffer conditions of 40 mM [Tris] and 12.5 mM [Mg^{2+}] are assumed, giving an additional entropic penalty (in units of $\text{cal M}^{-1} \text{K}^{-1}$) for duplex formation of:³⁴⁻³⁶

$$\Delta S^{0,\text{salt}} = 0.368 \times \frac{N}{2} \times \ln \left(\frac{1}{2} [\text{Tris}] + 3.3 [\text{Mg}^{2+}]^{1/2} \right) \quad (12)$$

where N is the number of phosphates in the duplex. For ssDNA we use a contour length of $L_{c,ss} = 0.6 \text{ nm}$ per base and a Kuhn length of $\lambda_{ss} = 1.8 \text{ nm}$: a single-stranded domain of 16 bases thus has a contour length of 9.6 nm.⁴¹⁻⁴⁵ For dsDNA we use a contour length of $L_{c,ds} = 0.34 \text{ nm}$ per base⁴⁶ and make the approximation that the persistence length is much longer⁴⁷ than any relevant duplex: a double-stranded domain of 16 bases thus corresponds to a single rigid link of length $\lambda_{ds} = 16 \times 0.34 \text{ nm}$. A crossover link between the two template domains hybridized to a single staple is treated as a single segment of length λ_{ss} .

Example rate calculations.

Consider the half-bound staple shown in Extended Data Fig. 8a that is hybridized to an otherwise empty template. A seam staple, labelled A, is used as an example here. Its second domain can hybridize to either of two sites: the closer is connected by a 448-nt ssDNA chain ($E[R^2] = 480 \text{ nm}^2$) and the further by a composite chain comprising a 2208-nt single-stranded chain and one rigid 16-bp ds segment ($E[R^2] = 2400 \text{ nm}^2$). Following the calculation outlined above, we find that for the closer site the effective local concentration of

the opposing domain $c_{\text{eff}} = 51 \mu\text{M}$, the loop cost $dG^{\text{loop}} = 6.5 \text{ kcal mol}^{-1}$ (at $T=60^\circ\text{C}$) and the hybridization rate $R = 50 \text{ s}^{-1}$. For the further site: $c_{\text{eff}} = 4.6 \mu\text{M}$, $dG^{\text{loop}} = 8.1 \text{ kcal mol}^{-1}$ and $R = 4.5 \text{ s}^{-1}$. The staple is 11 times more likely to bind to the closer domain.

Binding of one staple affects the binding of others by changing the characteristics of the sections of template (or partly-formed origami) that link their two binding domains. We now compute the hybridization rate, loop cost and local concentration for a second seam staple, staple B, in the presence or absence of staple A. In the absence of staple A, the shorter of the two loops that connect two binding domains of the second staple consists of a 864-nt ssDNA chain: $E[R^2] = 980 \text{ nm}^2$, $c_{\text{eff}} = 18 \mu\text{M}$, $dG^{\text{loop}} = 7.2 \text{ kcal mol}^{-1}$, $R = 18 \text{ s}^{-1}$. In the presence of staple A, the loop passes through the link formed by staple A and comprises 384 nt ssDNA, 3 rigid 16-bp dsDNA segments and a staple crossover modelled as a single segment of length λ_{ss} (Extended Data Fig. 8b): for this shortened loop, $E[R^2] = 520 \text{ nm}^2$, $c_{\text{eff}} = 46 \mu\text{M}$, $dG^{\text{loop}} = 6.6 \text{ kcal mol}^{-1}$ and $R = 46 \text{ s}^{-1}$. Insertion of staple A increases the rate of hybridization of the second domain of staple B by a factor of 2.6 by shortening the distance between its binding sites.

References

26. Zhang, P. H. *et al.* Engineering BspQI nicking enzymes and application of N.BspQI in DNA labeling and production of single-strand DNA. *Protein Express Purif.* **69**, 226-234 (2010)
27. Douglas, S. M. *et al.* Rapid prototyping of 3D DNA-origami shapes with caDNAo. *Nucl. Acids Res.* **37**, 5001-5006 (2009)

28. Wickham, S. F. J. *et al.* Direct observation of stepwise movement of a synthetic molecular transporter. *Nature Nanotechnology* **6**, 166-169 (2011)
29. Gillespie, D. T. Exact stochastic simulation of coupled chemical reactions. *J. Phys. Chem.* **81**, 2340-2361 (1977)
30. SantaLucia, J. Jr. and Hicks, D. The thermodynamics of DNA structural motifs. *Annu. Rev. Biophys.* **33**, 415-440 (2004)
31. Jacobson, H. and Stockmayer, W. H. Intramolecular reaction in polycondensations. I. The theory of linear systems. *J. Chem. Phys.* **18**, 1600-1606 (1950)
32. Morrison, L. E. and Stols, L. M. Sensitive fluorescence-based thermodynamic and kinetic measurements of DNA hybridization in solution. *Biochemistry* **32**, 3095-3104 (1993)
33. Gao, Y., Wolf, L. K. and Georgiadis, R. M. Secondary structure effects on DNA hybridization kinetics: a solution versus surface comparison. *Nucl. Acids Res.* **34**, 3370-3377 (2006)
34. SantaLucia, J., Jr. A unified view of polymer, dumbbell, and oligonucleotide DNA nearest-neighbor thermodynamics. *Proc. Natl. Acad. Sci. U.S.A.* **95**, 1460-1465 (1998)
35. N. Peryet, PhD Thesis, Wayne State University (2000).
36. Owczarzy, R., Moreira, B. G., You, Y., Behlke, M. A. and Walder, J. A Predicting stability of DNA duplexes in solutions containing magnesium and monovalent cations. *Biochemistry* **47**, 5336-5353 (2008)
37. Ouldridge, T. E., Louis, A. A. and Doye, J. P. K. Extracting bulk properties of self-assembling systems from small simulations. *J. Phys.: Condens. Matter* **22** 104102 (2010)

38. Lord Rayleigh, O. M. F. R. S On the problem of random vibrations, and of random flights in one, two or three dimensions. *Philos. Mag.* **37**, 321-347 (1919)
39. Chandrasekhar, S. Stochastic problems in physics and astronomy. *Rev. Mod. Phys.* **15**, 1-89 (1943)
40. Dijkstra, E. A note on two problems in connexion with graphs. *Numer. Math.* **1**, 269-271 (1959)
41. Smith, S. B., Cui, Y., and Bustamante, C. Overstretching B-DNA: the elastic response of individual double-stranded and single-stranded DNA molecules. *Science* **271**,795-799 (1996)
42. Rivetti, C. Walker, C. and Bustamante, C. Polymer chain statistics and conformational analysis of DNA molecules with bends or sections of different flexibility *J. Mol. Biol.* **280**, 41-59 (1996)
43. Mills, J. B., Vacano, E. and Hagerman, P. J. Flexibility of single-stranded DNA: use of gapped duplex helices to determine the persistence lengths of poly(dT) and poly(dA). *J. Mol. Biol.* **285**, 245-257 (1999)
44. Murphy, M. C., Rasnik, I., Chang, W., Lohman T. M. and Ha, T. Probing single-stranded DNA conformational flexibility using fluorescence spectroscopy. *Biophys. J.* **86**, 2530-2537 (2004)
45. Chen, H. *et al.* Ionic strength-dependent persistence lengths of single-stranded RNA and DNA. *Proc. Natl. Acad. Sci. U.S.A.* **109**, 799-804 (2012)
46. Saenger, W. Principles of Nucleic Acid Structure (Springer-Verlag, Berlin, 1984).
47. Hagerman, P. J. *Annu. Rev. Biophys. Biophys. Chem.* **17**, 265-286 (1988)

Extended Data Figure 1. The set of well-folded, planar states. **a** Well-folded, planar states can be considered as two adjacent monomer tiles linked by a single reciprocal template crossing at any of the locations marked with a triangle. This gives a set of 6 unique shapes, as indicated. **b** With the exception noted below, there are four ways to make each of these shapes, distinguished by the nucleotide sequence at the template crossing but not resolved by AFM imaging. In the example shown, crossings made at positions 5, 8, 17 and 20, corresponding to fold 4:1 (1:4), all give the same shape with fractional short edge offset w/W of $3/6$. The exception is that there are only two variants of state 5:0i. Configurations formed by linking tiles at positions 1 and 24 are not distinguishable, nor are links at positions 12 and 13. Part **c** is a detailed view of the connection between monomer tiles in these cases. The long-edge offset of these configurations is not precisely defined (it can range from 0 to $2/7$ depending on the conformation of the long edge staple). The set of 22 well-folded, planar states consists two folds for the shape shown in **c** and four folds for each of the other five shapes.

Extended Data Figure 2. Well-folded, non-planar states and an illegal fold. **a, b** The set of legal folds permitted by the model consists of the 22 planar folds defined in Extended Data Fig. 1 and an additional 54 non-planar folds, four for each shape shown here. Shapes in **a** are formed by allowing three reciprocal crossings between two tiles, those in **b** are formed by allowing 5 reciprocal crossings. These non-planar folds form only rarely in simulation. **c** An example of a misfolded shape: the part-folded domains are, individually, well-formed but cannot be joined to give a legal fold.

Extended Data Figure 3. Fitting the shapes of origami tiles observed by AFM. **a** AFM images were flattened by line-by-line subtraction of a second-order polynomial. Image processing and fitting were performed using custom MATLAB programs. **b** A histogram of pixel heights was used to set the threshold for the generation of a binary image. The threshold was found by calculating the average of the means of the two peaks corresponding to background and tiles; if this failed because the image was noisy the threshold was set manually. **c** Well-separated objects in the binary image which have the approximate area of a dimer tile were flagged for fitting (numbered). **d** Tile outlines were generated using a Sobel edge-finding filter. **e** Representative fitted outlines (two equal, offset parallelograms) were used to classify dimer tiles as described in the text (cf. Fig. 3d).

Commented [AJT5]: Katherine - OK?

Commented [AJT6]: I am not sure of what we mean by 'well-folded' and 'legal'. I think they are synonymous, the only distinction being between well-folded, planar and well-folded, non-planar. Is that right?

Extended Data Figure 4. AFM data. **a-e** show a 1.5 μm field of view containing structures folded from each of the five staple sets of Fig. 4 a-e. Shapes that were flagged for fitting are marked with a dot. Successfully fitted shapes are marked with a green dot and the fitted outline is superimposed on the image. **f** The collection of shapes that were not successfully fitted includes crowded areas where shapes are touching and shapes where the two component monomer tiles are distorted, perhaps during deposition on the mica surface, but can be clearly assigned to one of the predicted shapes. Part-folded (or damaged) shapes are also observed, often with one well-folded monomer attached to a part-folded monomer; sometimes a portion of unfolded template can be observed.

Extended Data Figure 5. Strong seam connections influence the folding pathway. The part-folded structure shown is legal, with seam configuration 1:1. If the seam staples remain in place this could progress to fully folded structures with seam configurations 4:1 or 3:2, but not 5:0.

Extended Data Figure 6. Monitoring origami assembly using fluorescence. Assembly of a monomer tile (Fig. 1) was monitored using fluorescently labelled staples. The positions of the labelled strands in the folded tile are shown in **a**: the seam staple was labelled with 5' Cy3 and 3' Black Hole Quencher 2, and the body staple with 5' Cy5 and 3' Black Hole Quencher 2. Reactions containing the monomer template at 50 nM and staples at 100 nM in a buffer containing 12.5 mM MgCl₂, 10 mM Tris-HCl and 0.5 mM EDTA pH8.0 were held at 96°C for 10 min, cooled from 96°C to 25°C at 0.3°C.min⁻¹, held at 25°C for 10 min then heated to 96°C at 0.3°C.min⁻¹. The fluorescence signal for Cy3 and Cy5 was recorded at 0.3°C intervals during cooling and heating cycles. Staple binding increases the separation between fluorophore and quencher and therefore increases the fluorescence intensity. **b** Fluorescence intensities (F) and **c** their derivatives (dF/dT) as functions of temperature during origami annealing and melting. Sharp transitions, corresponding to narrow ranges of staple incorporation temperatures, are consistent with cooperative origami assembly. In the case of the unmodified tile the seam staple is incorporated into the tile at the same temperature as the body staple. Hysteresis (marked *) is consistent with the cooperative binding of the seam staple. When one half of the seam is broken the hysteresis observed for seam staple binding is reduced and the seam staple is incorporated at a lower temperature than the body staple. Weakening the seam has little effect on the incorporation of the body staple.

Extended Data Figure 7. Rearrangement of staples during folding. **a-e** The heat maps show the predictions of the model for the number of reconfiguration events during assembly for each of the staple sets shown in Fig. 4a-e. A ‘reconfiguration event’ occurs when a contact between two template domains is released and replaced by an alternative contact. Domains omitted from the map are those which would generate an illegal fold if reconfigured.

Extended Data Figure 8. Evolving correlations between seam staples in the model during folding. Part **a** corresponds to the original staple set (cf. Fig. 4a) and **b** to the broken-seam variant (Fig. 4b). In each case, average data from 1600 simulations are presented ('all') together with subsets sorted by final fold (5:0, 4:1, 3:2 and misfold). Simulations resulting in well-folded, non-planar structures (NP) are included in 'all' but not presented separately: such structures occurred ~~63-65~~ times in **a** and ~~once-5~~ times in **b**.

Commented [AJT7]: does not add up!

Circular icons with internal connections of different lengths represent links across the seam ('seam links') connecting points on the template spanning (i.e., that are separated by) 28, 56, 84, 112 and 140 template domains. A 'seam link' represents a connection across the seam mediated by at least one seam staple (with the original staple set, part **a**, it may also represent a pair of staples).

~~A single column to the left of each block of data, labelled 'S', represents the average occurrence of links with each of the five possible spans (range 0-4).~~ The square on the right of the figure, labelled 'B', represents the average occupancy for each body-staple domain??? (range 0-2).

Correlations between seam links are represented by three 5×5 blocks. Each pixel is labelled by two icons whose orientation has the same significance as in the 'circle' diagrams of Fig. 3: two icons related by 180° rotation represent one internal link in each of the two halves of the template; a 90° rotation represents one internal link and one cross link. Only relative orientation is significant so, e.g., fully folded state $m:n$ is not distinguished from $n:m$ (Extended Data Fig. 1b). Each pixel represents the average number of *pairs* of links with the specified spans and relative orientations (range 0-8).

For staple set **a** folding is substantially complete at 62°C: at this temperature the patterns of correlation that are characteristic of the fully-folded structures can be seen clearly. For

example, the presence of the longest (140-domain) link with no cross-link to the other half of the template is characteristic of fold 5:0. (A 140-domain with a cross-link only occurs in misfolds.) A 112-domain link with a shorter cross-links is characteristic of 4:1, and the presence of two 56-domain links including a cross link is characteristic of 3:2. These and other correlations that are characteristic of the final folds are already visible in the averaged correlation maps (when simulations are sorted by final fold) at very early stages of folding. The pattern of seam staples at an early stage of folding is therefore predictive of the final fold (Extended Data Table 1).

Commented [AJT8]: or NP structures?

Commented [JB9]: For the time being this table is included at the bottom of Ext. Data Fig. 8

For the broken-seam staple set **b**, intact seam staples are incorporated later in the folding pathway (the 50% incorporation temperature for seam staples is 64.2°C for **a**, 62.3°C for **b**). The 50% body seam incorporation temperature is unchanged (63.9°C for **a**, 64.0°C for **b**). The same characteristic patterns of seam staples that, with the full seam, are associated with different final folds are also visible at high temperatures for the broken-seam staples. However, 90% of broken-seam simulations result in fold 5:0, as designed.

Additional evidence for the influence of strong seam contacts on the folding pathway is provided by the dramatically different yields of misfolds: 53% for full-seam staples **a**, 1% for broken-seam staples **b**. Stable incorporation of incompatible seam staples in **a** prevents the formation of well-folded structures.

For caption to new table:

Seam-staple correlations at very early stages of folding are predictive of the final fold.

c corresponds to the original staple set (cf. Fig. 4a) Data from 1600 simulations are presented.

Three tests, on correlations between seam staples, were applied at the temperature at which, on average, half of all seam staples are incorporated (64.2°C). These tests were designed to discriminate between patterns of seam staples characteristic of different final folds. The table records distribution between final folds of the simulations that satisfy each test.

Test 1: A 140-domain seam link with no cross-link to the other half of the template (characteristic of fold 5:0).

Test 2: A 112-domain link with a shorter cross-link (characteristic of fold 4:1).

Test 3: Two 56-domain links, including one internal link and one cross-link between halves of the template (characteristic of fold 3:2).

Extended Data Figure 9. Example calculations of staple hybridization rates (see Methods).

Annotations are distances along the template measured in nucleotides. **a** In the example shown, the unbound domain of a half-bound seam staple (staple A) can bind to one of two sites on the template. The local concentration of the closer domain, as estimated at the half-bound staple, is 11 times higher than that of the more distant domain with a correspondingly greater hybridization rate. **b** Hybridization of the second domain of a second seam staple (staple B) is accelerated by a factor of 2.6 by the previous insertion of staple A that shortens the link between the two binding sites.

a

template ——— seam ——— body edge ———, ———

b **c**

a **b** **c**

a **b** **c**

a **b** **c**

a **b** **c**

(= body staple, = seam staple)

c

	5:0	4:1	3:2	N.P.	misfold	all
not	117	8	5	5	82	217
and	16	100	28	12	142	298
and	20	19	155	11	176	381
Count:	231	207	268	65	829	1600

a **b**